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### **Arpa's blog**

## [Tutorial] Sack (dsu on tree)

By Arpa, history, 3 years ago, , ,

Changes are available in history section.

Hi!

Most of the people know about dsu but what is the "dsu on tree"?

In Iran, we call this technique "Guni" (the word means "sack" in English), instead of "dsu on tree".

I will explain it and post ends with several problems in CF that can be solved by this technique.

# What is the dsu on tree?

With dsu on tree we can answer queries of this type:

How many vertices in the subtree of vertex v has some property in  $\mathcal{O}(nlogn)$  time (for all of the queries)?

For example:

Given a tree, every vertex has color. Query is **how many vertices in subtree of vertex** v are colored with color c?

### → Pay attention

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```
Let's see how we can solve this problem and similar problems.
```

First, we have to calculate the size of the subtree of every vertice. It can be done with simple dfs:

```
int sz[maxn];
void getsz(int v, int p){
    sz[v] = 1;    // every vertex has itself in its subtree
    for(auto u : g[v])
        if(u != p){
            getsz(u, v);
            sz[v] += sz[u]; // add size of child u to its parent(v)
        }
}
```

Now we have the size of the subtree of vertex [v] in [sz[v]].

The naive method for solving that problem is this code(that works in O(N ^ 2) time)

```
int cnt[maxn];
void add(int v, int p, int x){
    cnt[ col[v] ] += x;
    for(auto u: g[v])
        if(u != p)
            add(u, v, x)
}

void dfs(int v, int p){
    add(v, p, 1);
    //now cnt[c] is the number of vertices in subtree of vertex v that has color c.
You can answer the queries easily.
    add(v, p, -1);
    for(auto u : g[v])
        if(u != p)
            dfs(u, v);
}
```

5	wxhtxdy	3293
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Now, how to improve it? There are several styles of coding for this technique.

# 1. easy to code but $O(n \log^2 n)$ .

```
map<int. int> *cnt[maxn];
void dfs(int v, int p){
    int mx = -1, bigChild = -1;
    for(auto u : a[v])
       if(u != p){
           dfs(u, v):
           if(sz[u] > mx)
               mx = sz[u], biaChild = u:
    if(bigChild != -1)
        cnt[v] = cnt[biaChild];
    else
        cnt[v] = new map<int, int> ();
    (*cnt[v])[ col[v] ] ++;
    for(auto u : q[v])
       if(u != p \&\& u != bigChild){
           for(auto x : *cnt[u])
               (*cnt[v])[x.first] += x.second;
    //now (*cnt[v])[c] is the number of vertices in subtree of vertex v that has color
c. You can answer the queries easily.
```

# 2. easy to code and $O(n \log n)$ .

```
vector<int> *vec[maxn];
int cnt[maxn];
void dfs(int v, int p, bool keep){
   int mx = -1, bigChild = -1;
```

```
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during a contest? ©
```

```
for(auto u : g[v])
       if(u != p \&\& sz[u] > mx)
           mx = sz[u], bigChild = u;
    for(auto u : g[v])
       if(u != p \&\& u != bigChild)
           dfs(u, v, 0);
    if(bigChild != -1)
        dfs(bigChild, v, 1), vec[v] = vec[bigChild];
    else
        vec[v] = new vector<int> ();
    vec[v]->push back(v);
    cnt[ col[v] ]++;
    for(auto u : q[v])
       if(u != p \&\& u != bigChild)
           for(auto x : *vec[u]){
               cnt[ col[x] ]++;
               vec[v] -> push back(x);
   //now (*cnt[v])[c] is the number of vertices in subtree of vertex v that has color
c. You can answer the queries easily.
   // note that in this step *vec[v] contains all of the subtree of vertex v.
    if(keep == 0)
        for(auto u : *vec[v])
            cnt[ col[u] ]--;
}
3. heavy-light decomposition style O(n \log n).
int cnt[maxn];
bool big[maxn];
void add(int v, int p, int x){
    cnt[ col[v] ] += x;
    for(auto u: g[v])
        if(u != p && !big[u])
```

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prophet\_ov\_darkness → [GYM] 2018 Battle of
Brains Replay

Detailed →

15

15

```
15
```

```
add(u, v, x)
}
void dfs(int v, int p, bool keep){
    int mx = -1, bigChild = -1;
    for(auto u : g[v])
       if(u != p \&\& sz[u] > mx)
          mx = sz[u], bigChild = u;
    for(auto u : g[v])
        if(u != p \&\& u != bigChild)
            dfs(u, v, 0); // run a dfs on small childs and clear them from cnt
    if(bigChild != -1)
        dfs(biqChild, v, 1), biq[biqChild] = 1; // biqChild marked as big and not
cleared from cnt
    add(v, p, 1);
   //now cnt[c] is the number of vertices in subtree of vertex v that has color c.
You can answer the queries easily.
    if(bigChild != -1)
        big[bigChild] = 0;
    if(keep == 0)
        add(v, p, -1);
}
```

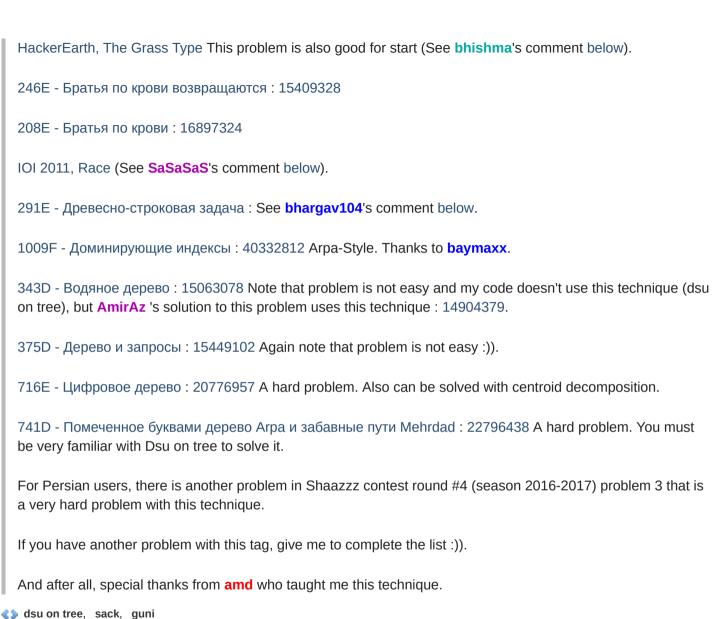
### 4. My invented style $O(n \log n)$ .

This implementation for "Dsu on tree" technique is new and invented by me. This implementation is easier to code than others. Let st[v] dfs starting time of vertex v, ft[v] be it's finishing time and ver[time] is the vertex which it's starting time is equal to time.

```
int cnt[maxn];
void dfs(int v, int p, bool keep){
   int mx = -1, bigChild = -1;
   for(auto u : g[v])
   if(u != p && sz[u] > mx)
        mx = sz[u], bigChild = u;
```

```
1
```

```
for(auto u : g[v])
         if(u != p \&\& u != bigChild)
              dfs(u, v, 0); // run a dfs on small childs and clear them from cnt
    if(bigChild != -1)
         dfs(bigChild, v, 1); // bigChild marked as big and not cleared from cnt
    for(auto u : q[v])
         if(u != p \&\& u != bigChild)
              for(int p = st[u]; p < ft[u]; p++)</pre>
                  cnt[ col[ ver[p] ] ]++:
    cnt[ col[v] ]++;
    //now cnt[c] is the number of vertices in subtree of vertex v that has color c.
You can answer the queries easily.
    if(keep == 0)
         for(int p = st[v]; p < ft[v]; p++)</pre>
              cnt[ col[ ver[p] ] ]--;
}
But why it is O(n \log n)? You know that why dsu has O(q \log n) time (for q queries); the code uses the
same method. Merge smaller to greater.
If you have heard heavy-light decomposition you will see that function add will go light edges only.
because of this, code works in O(n \log n) time.
Any problems of this type can be solved with same dfs function and just differs in add function.
Hmmm, this is what you want, problems that can be solved with this technique:
(List is sorted by difficulty and my code for each problem is given, my codes has heavy-light style)
600E - Lomsat gelral: heavy-light decomposition style: Link, easy style: Link. I think this is the
easiest problem of this technique in CF and it's good to start coding with this problem.
570D - Деревянные запросы: 17961189 Thanks to Sorasorasora; this problem is also good for start coding.
Squ507 (SGU is unavailable, read the problem statements here) This problem is also good for the start.
```







A2OJ's DSU Section has quite a few tree DSU problems.

Thank you for this post, it explains the theory well and is very easy to read.

→ Reply



2 years ago, # \_ | 🏠 بدك تضل تتمنيك عكل بوستات الخرا ؟



What does the variable "keep" denote?

→ Reply



3 years ago, # \_^ | 😭

← Rev. 4

+3

-6

\_ 0 V

The way I understand HLD here is basically if a child is the big child, we don't want to recompute answer for it to reduce computation. So we just store the answer for it in the cnt array already so that it's parent doesn't need to re-dfs this subtree. keep denotes whether or not this child is that big child. Please correct me if I'm wrong. :) → Reply



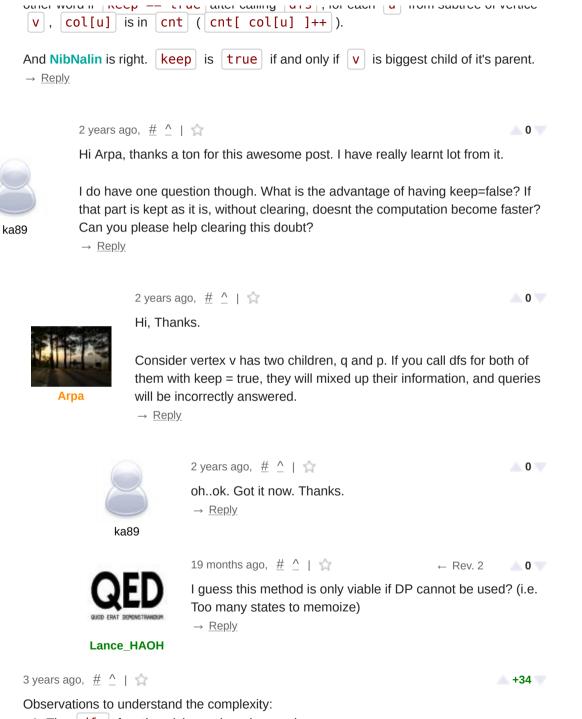
← Rev. 3 **0** 

Look at last two lines:

It means that if keep == false after dfs clear v s subtree information from cnt . And if keep == true , don't clear v s subtree information from cnt . In

other word if keen == true after calling dfs for each up from subtree of vertice

**Arpa** 



1 The Afe function visits each node exactly once



belakor

- 1. THE | UIS | TUHCHOH VISILS EACH HOUR EXACTLY OFFEE.
- 2. The problem might seem with the add function. You might think that it is making the algorithm n^2. Note that in the add function, we only go down from a vertex to its children if the edge connecting the vertex to the child is a light edge.

You can think of it in this way, each vertex v will be visited by a call to the add function for any ancestor of v that is connected to a light edge. Since there are at most log(n) light edges going up from any vertex to the root, each vertex will be visited at most log(n) times.

So the algorithm is: Say you are at a vertex v, first you find the bigchild, then you run dfs on small childs, passing the value of keep as 0. Why? So they are cleared from cnt. Then you run a dfs on bigchild, and you do not clear it from cnt. Now, cnt stores the results for all vertices in the subtree of bigchild (since we cleared cnt for small childs and didn't do so for the bigchild), so we call the add function to "add" the information of children of current vertex that are connected to it via a light edge. Now we are ready to compute the answer

→ Reply





gogateiiit

As you said "add" function goes down using only light edges, Don't these two lines <code>if(bigChild != -1) big[bigChild] = 0;</code> of heavy light decomposition implementation would affect it as if you call "add" after all dfs are done and returned to the root then we only have one heavy edge marked that of root itself others are zero so as "add" goes below it traverses whole tree. Help me here.

→ Reply



gogateiiit



19 months ago, #  $^{\wedge}$  |  $^{\wedge}$ 

I OF ITOSE WHO HAD SAITE GOADI AS FHAD. FHSLICIS AHACISIAHA

why it is wrong to remove it.consider you are at particular node(let it be called A) in recursion, above line is not there, you have 3 children one of them is big child(3rd) while others are normal so you traversed inside 1st and came back to A then you traversed inside 2nd child if you do not have above line then while going inside this children you would have all answer for big children of 1st child which would mess your answer. Now let's understand why complexity is  $O(n(\log(n))$ :

Note 1: To calculate complexity you need to measure how many times add function visits the ever y node.

Note 2: For first add called at a node: A node will visited by add only through its ancestors which are connected by light edges so n nodes log(n) light edges above it this gives us O(n(log(n)))

Note 3: For second add called at a node: Now somebody may protest that that after above mentioned line(big[bigChild]=0) we are unmarking heavy edge and also calling add after that which may mess up complexity as it travels every node below it which is O(n) but keep==0 condition ensures that for each node there atmost log(n) nodes above in ancestor which have keep=0 function is called.which again gives  $O(n(\log(n))$ .

Giving us finally O(n(log(n))) complexity. Follow this link to understand heavy light decomposition's properties: https://blog.anudeep2011.com/heavy-light-decomposition/ → Reply

0



3 years ago, # | 😭

In second easy with O(n\*lg n)

Why if(keep==false) we delete only vertex from main vector

```
IVI (auto u . 'Vec[v]/
                cnt[ col[u] ]--;
  but we don't delete vertex from cnt which we changed here:
  for(auto u : g[v])
          if(u != p && u != bigChild){
              for(auto u : *vec[u])
                   cnt[ col[u] ]++;
   → Reply
          3 years ago, # ^ | 😭
                                                                        ← Rev. 2 0
           There was a mistake in writing. I'm sorry.
           Thanks for reporting this problem.
           code should be:
                  if(u != p && u != bigChild){
                       for(auto x : *vec[u])
                           cnt[ col[x] ]++;
                   }
           Instead of:
Arpa
                  if(u != p \&\& u != bigChild){
                       for(auto u : *vec[u])
                           cnt[ col[u] ]++;
                   }
          I have edited that.
           → Reply
  3 years ago, # | 🏠
                                                                                   0
```

can someone tell me how 200F is solved with this technique? thanks a lot





3 years ago, # ^ | 🏠

A 0

You need to compute for each pair  $|\mathbf{v}|\mathbf{p}|$  the p-th cousin of v. That is equivalent to finding the number of p-th descendants of the p-th ancestor of v - 1.



So for each query, replace  $[v \ p]$  with  $[p \ th \ ancestor \ of \ v \ p]$ . Now you need to store in cnt the number of nodes at a certain depth. In other words, cnt[x] should be equal to number of nodes at depth | x | in the current subtree.

Code for Reference: http://codeforces.com/contest/208/submission/17513471

→ Reply



3 years ago, # \_^ | 😭

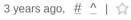
0

can't understand why for every vertex v we ans[depth[v]] increase by 1 when we call add function, why must we do it?or why it must be ans[deth[v]] when depth[v] means distance from root to v?

→ Reply



**Arpa** 



← Rev. 2



ans[h] is equal to number of vertices with height h, (with distance h from root).

Let par, p'th ancestor of v, the answer to query is:

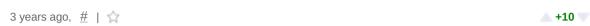
Consider only subtree of vertice par, print ans [height[v]] - 1.

So with method above we can process all of the queries.

See my code for better understanding.

→ Reply





ALV.

If i haven't read this article, i wouldn't get ac on this problem. It is another problem which can be solved easily by dsu.

here is my code in HLD-style.

Thanks!

→ Reply



3 years ago,  $\# \land | \diamondsuit$ Thanks! Added to list ;)

→ Reply

Arpa

3 years ago, # | 😭

← Rev. 3 +12

**△** 0 ▼

I can't understand why the second code is correct...

Batman

Consider this example:

We wanna calculate the cnt for Vertex 8. These are the steps:

Going to Vertex 1

Going to Vertex 2 by keep=0

Going to Vertex 3 by keep=0,Vec[3]={3}

Going to Vertex 4 by keep=1,Vec[4]={4},Cnt[color[4]]=1

Going back to Vertex 2,Vec[2]={2,4},Cnt[color[4]]=0,Cnt[color[3]]=1

And then when we go to Vertices 5,6,7,8 still Cnt[color[3]]=1.

Also sorry if I did the steps wrong...

**UPD** Thank you for editing the blog. My problem fixed.

→ Reply



3 years ago, # | 😭

← Rev. 4

0

Great post. If you explained the idea before showing the code, it would be better to understand. Also commenting the variables meaning in the code would be of great help.

Also, it would be nice to post hints about the solutions.

Proving explicitly why it is nlogn would be good too (ie. as each node's subtree set gets merged into one set of size equal or greater, and the base set has size 1 and the last set has size n, then we take logn steps to go from 1 to n. Summarizing, each node gets merged logn times, so the total complexity is O(nlogn)).

Here's my solution to 343D, maybe it will be of help to someone: 18958875. A lot easier to code than the one in the tutorial.

→ Reply

3 years ago, # ^ | 😭

Thanks for your suggestions first!



Arpa

I proved that it is O(nlogn): You know that why dsu has O(q log n) time (for q queries); the code uses same method. Merge smaller to greater.

And about your code (18958875), anyone has a different opinion!

→ Reply

Thanks for the reply!



Yeah, you did prove. People who remember DSU's proof will most likely understand. I stated a more extensive proof would be better thinking about people who don't exactly know the proof. Don't take me wrong, but they may get a little confused reading this proof.

I mentioned my code exactly because everyone has a different opinion,. Maybe it'll help a later reader, that's all.

→ Reply



pivorics

complexity of the heavy-light decomposition style one in O(nlogn)?

In the case where each node has at most two children: Denote the root node of the tree as u, which is of size s. The child of u connected to the lighter edge is of size at most  $\frac{s}{2}$ . So the total number of nodes on which we run the "add" function would be at most  $\frac{s}{2} + \frac{s}{4} + \cdots = s$ . So I don't understand where the log(n) factor comes from.

The online tutorial for HLD says a new chain is built when we arrive at a child node via a lighter edge, where each chain is stored as a segment tree, and so I can see there is indeed a O(logn) factor involved.

Regardless can you perhaps elaborate a little bit more on the time complexity of the dsu structure? Thank you!

→ Reply



Arpa

```
2 years ago, # ^ | a
```

The online tutorial for HLD says a new chain is built when we arrive at a child node via a lighter edge, where each chain is stored as a segment tree, and so I can see there is indeed a O(logn) factor involved.

As you know, if you use segment tree in heavy-light decomposition, each query time complexity will be  $O(log^2(n))$ . Because in each query you will go O(log(n)) chains and in each chain it will spend O(log(n)) time.

Now, I will proof that "heavy-light decomposition style implementation" of "dsu on tree" is O(n.log(n)):

Consider a complete binary tree with n vertices. In dfs function you will run another dfs function in child (T(n/2)\*2) and you will call add function and it will

spand  $\Omega(n/2)$  time So

15 \_\_\_\_\_\_ 2 years ago, # ^ | �

A 0



You know that why dsu has O(q log n) time (for q queries); the code uses same method. Merge smaller to greater.

Pardon me, but I don't follow. Which dsu are you talking about? The one with inverse-Ackermann function?

→ Reply

2 years ago, # ^ | ^

No. Dsu with size compare. Like this:

```
A STATE OF
```

Arpa

```
int find(int x){
    return par[x] == x ? x : find(par[x]);
}
void merge(int v, int u){
    v = find(v), u = find(u);
    if(v == u) return;
    if(size[v] < size[u]) swap(v, u);
    par[u] = v;
    size[v] += size[u];
}
→ Reply</pre>
```

2 years ago, # | 🏠

← Rev. 2





In easy to code but O(nlog^ 2), I cant't understand why do we store the size of subtrees of vertices in array sz and use it as the criteria for choosing the big child, I think we should store in the array "sz" the number of distinct colors in the subtree of any node v, because that is what we actually iterate on when transferring the map from v to u, why is this wrong?

→ Reply

15

13



**Arpa** 

2 years ago, # \_^ | 🏠

Hi!

It isn't wrong! Both of your method and mine have the same worst case. But your average is better.

→ Reply



← Rev. 2

A 0

A 0



Ahh, thanks gabrielsimoes, for anyone struggling to understand: n\*log^2n is about answering queries OFFLINE right during the dfs. After the dfs has finished the cnt[v] will no longer be a valid map for vertices that were chosen as bigChild.

→ Reply



2 years ago, # | 🏠

+8



http://codeforces.com/problemset/problem/291/E 291E - Древесно-строковая задача **Arpa** This problem can also be done by dsu on trees. Calculate hash value for each suffix value of target string. Then for each suffix of an edge if it is a valid prefix of the target string we would just need the frequency of the hash value of the remaining suffix of the target string in its subtree which can be maintained by this technique. The case when the entire string occurs in an edge can be dealt with separately.

→ Reply



2 years ago, # \_ | 🏠

+5

Thanks added to list, but it can be solved very easier : 19827525, just use KMP.  $\rightarrow$  Reply

**Arpa** 



18 months ago, # ^ | 😭

0

Just use hashes :) http://codeforces.com/contest/291/submission/29431526

→ Reply

**Dalgerok** 



10 months ago, # ^ | 🏠

0

Please send me a code of the solution with this techinque)



2 years ago, # | 🏠

Actually, in China, we call this method as "Heuristic Merge" which always merge the smaller to the bigger. Not hard to understand each vertex will be visited in O(log n) times because when we visited a vertex, then the size of tree which the vertex is in doubled.

→ Reply

2 years ago, # | 🏠 ▲ +1 ▼

Hey Arpa,



In your my invented style I'm unable to understand that why in third loop are you not checking for u not being parent of v. Why are you only checking for just u not being the big child.

Thanks in Advance

→ Reply



2 years ago, # \_^ | 🏠

← Rev. 3

+13

Sorry, fixed. It's because I've copied my code from 741D - Помеченное буквами дерево Arpa и забавные пути Mehrdad, input for this problem was a rooted tree.

→ Reply

2 years ago, # ^ | 😭

+2

<u>0</u>



Thanks a lot,

Also, I think there is one more mistake. You never added col[v] to the array. Am I missing something. Thanks in advance.

→ Reply



0

You are right, I'm very thankful to you. I was careless while coping the code from polygon.

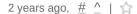
. Danly



hhichma

2 years ago, # | 🔷

In the easy to code O(nlogn) method vec[v] stores all the vertices in the the subtree rooted at v. How will this fit into memory if we are not deleting the vec of child after merging it with the parent  $\rightarrow$  Reply



♣ +1 ▼



Arns

Used memory is always less than or equal to time complexity, so when time complexity is  $\mathcal{O}(n \cdot \log n)$ , used memory is less than or equal to  $\mathcal{O}(n \cdot \log n)$ . In this case, used memory is  $\mathcal{O}(n \cdot \log n)$ . Although if you delete useless vec's the memory become  $\mathcal{O}(n)$ .

→ Reply



hhishma

A 0

Thanks for the reply . I think this problem can also be solved using your approach. (The Grass Type HackerEarth)

→ Reply

2 years ago, # ^ | 😭

← Rev. 3

▲ +1 ▼

I'll add this problem to the post if I find it related, I'm thankful anyway.



**Arpa** 

**Edit**: Note that this is not **my** approach, but I'm the first man who publishes a tutorial about this (not sure), Sack has been used in INOI, IOI and ACM several times, so it isn't a new thing, invented be me.

Edit: Added.

→ Reply



2 years ago, # ^ | 😭

A 0

Can you mention probelms from the IOI that are solved with sack?

 $\rightarrow Reply$ 







I'll add one of them tonight.

Edit: Added.

**Arpa** 

→ Reply



2 years ago, # ^ | ^ Wow, I didn't think of solving it with

sack.Thx → Reply

2 years ago, # | 😭 A 0



Hi Arpa, I can not understand, why is this approach called dsu on tree? This approach has a nice trick to reduce complexity by saving data about "big child". I can't see any special similarity with general dsu approach. In general dsu problems, we merge 2 subset into 1 set by linked list approach. But, in your tutorial there is no "merge" function. Am I missing something?

Also I see that, in your 600E's solution 14554536 you used merge function. I can't understand, could you please explain that code?

→ Reply



2 years ago, # ^ | 🏠

A 0

A 0

In fact we are merging information of small children with big child. Think more.

In that code, mrg function merges information in u into v.

→ Reply

2 years ago, # | 🏠

♣ +1 ▼

Hi Arpa! Thanks for making this tutorial.

beAwesome

(\* (sad() == true) { med().mtcp();

> I just want to make sure my understanding is correct: this merging smaller maps into larger ones takes logarithmic time because when a vertex is merged, the new map it is in at least twice its size.

Honce marging can only happen log(n) times for each of the nivertices, leading to a total runtime of

FIGURE, THEIGHING CALLOTHY HAPPEH LOGINI HITTES FOR EACH OF THE IT VEHICES, TEAUTING TO A TOTAL HUMBING OF O(nlogn)? Thanks! → Reply 2 years ago, # ^ | � <u>0</u> Yes, but note that if you use map, it's  $O(n \cdot \log^2 n)$ . → Reply **Arpa** 2 years ago, # ^ | 🏠 A 0 med()\_mtcp(); If you use unordered map, does it become  $O(n \cdot log n)$ , then? → Reply beAwesome A 0 Unordered\_map is theoretically O(n) per query. But you can suppose that it's O(1) per query in code. → Reply **Arpa** 2 years ago, # | 😭 A 0 This 758E.Read this comment on how to use it. → Reply 23 months ago, # | 🏠 A 0 Why do we need to iterate through the children of v after add(v, p, -1) in the naive approach? → Reply A 0



surajghosh

**HUECTRUM1** 

23 months ago, # \_ | 😭

dfs() solves the problem for all the nodes, not just one. So, after you've gotten the answer

for v, it will calculate the answer for its children.



23 months ago, # | 😭 +8

101 Hack 47 Summing Tree was solved using this technique by satyaki3794 Submission

→ Reply

vatsal



23 months ago, # | 😭

+3

also 778С - Петрович --- полиглот is solvable with a similar tecnique: is that DSU on tree?

→ Reply

lukecavabarrett



23 months ago, # ^ | 😭

+3

yes

→ Reply





20 months ago, # | 😭

+6

Can anyone give me a link to "Shaazzz contest round #4 (season 2016-2017) problem 3" or tell me where can I find it? Thanks.

→ Reply



20 months ago, # ^ | ^

+5

It's a Persian contest.

→ Reply

Arpa



20 months ago, # ^ | �

+6

Can you tell me where can I find it? I searched for it just now but didn't get it.

→ Reply



20 months ago, # ^ | ☆

Thank you!

→ Reply



tak fate

20 months ago, # |  $\diamondsuit$ 

I can AC easily Problem 375D by the 3th way ,but WA by the 4th way.... WA on the test 4.. why...  $\rightarrow \frac{\text{Reply}}{2}$ 



19 months ago, # | 😭

A +11 V

APIO 2016 Fireworks uses this, but is a much harder problem.

→ <u>Reply</u>

rielsimoes

18 months ago, # |  $\diamondsuit$ 



Arpa, in the Easy to code but  $O(nlog^2n)$  section code you have written a commented line that is: //now (\*cnt)[c] is the number of vertices in subtree of vertex v that has color c. You can answer the queries easily. But I think it would be //now (\*cnt[v])[c] is the number of vertices in subtree of vertex v that has color c. You can answer the queries easily. Will (\*cnt)[c] changed with (\*cnt[v])[c] ?

Reply



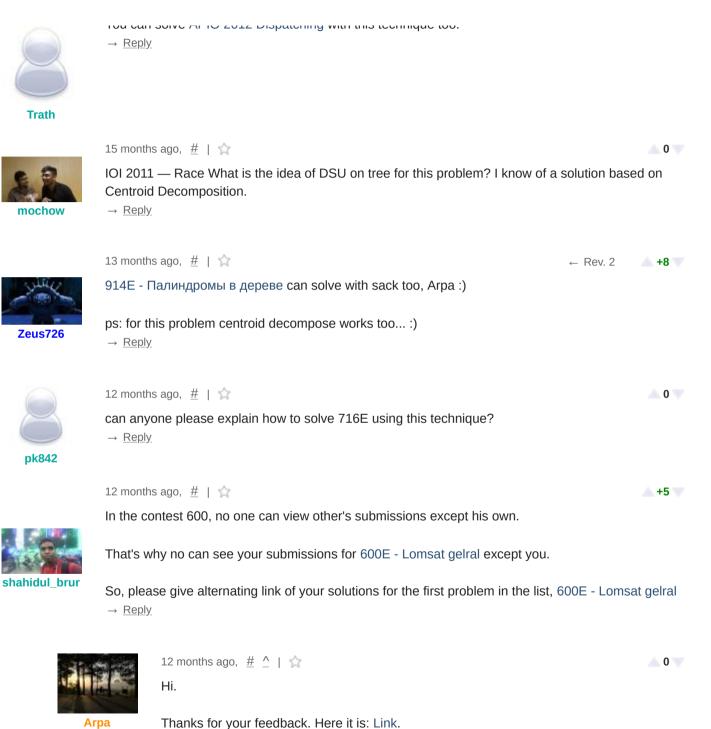
18 months ago, # \_^ | 🏠

0

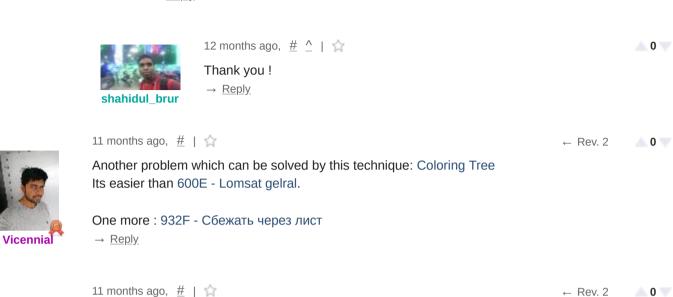
Hi. Thanks. Edited.

→ Reply

**Arpa** 



. Panly





Izoi hhn

Hi, I would like to ask you about the code in heavy-light decomposition style. Why the bigChild is cleared before clearing the subtree at the end of the code? From my perspective, in add function bigChild will be visited and the array "big" doesn't make sense. Can you explain it in detail? Thanks a lot.

→ Reply



11 months ago, # |  $\diamondsuit$ 

<u>-7</u>

No good explanation! Only code! Worst tutorial.

→ Reply



11 months ago, # \_ | 😭

<u>0</u>

+5

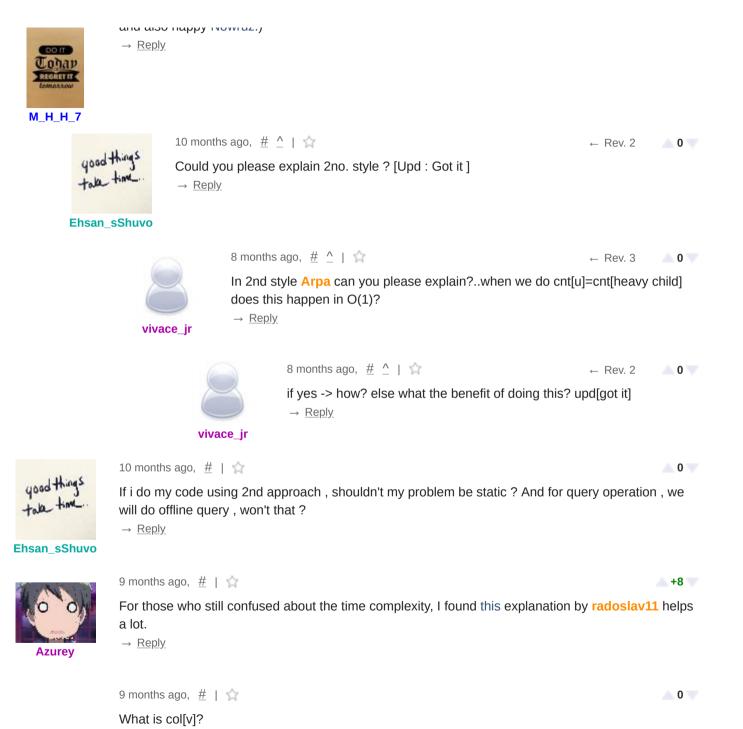
If you have a doubt why not ask in the comments rather than whining about how bad the tutorial is.

→ Reply

11 months ago, # |  $\diamondsuit$ 

Nice tutorial!

and also hanny Nowrus.)



. Donly



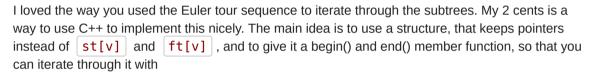


Color of the v-th vertex



**Azurey** 

8 months ago, # | 🏠





Na2Th

for(int u : T[i]) cout << u << " is in the subtree of " << i << "\n";</pre>

To actually solve the problem, maybe in a Heavy-Light style, I kept also for each vertices a pointer to the leaf of its heavy-path, so that I could only change the answer in the leaf.

My full implementation of lomsat gelral can be found here

→ Reply



8 months ago, # | 🏠

Hi, Arpa, I used this technique to solve 600E - Lomsat gelral, its a very neat technique.. but wont this get a MLE? I am getting a MLE with the O(nlog^2n0 method ... I saw your solution and I see its the same as mine, but mine gets MLE.. My solution :- 39325497

→ Reply

8 months ago, # ^ | 🏠

← Rev. 3

+5

0

A 0

<u>0</u>

Solutions for Educational Codeforces Round 2 is private, nobody can't see your code. Perhaps you do not use pointers, dynamic memory allocation, and memory cleanup. In this

technique it is forbidden to convibure containers



dmkozyrev

I solved this problem with Euler tour on tree and Mo algorithm in  $O(n \cdot \sqrt{n})$  time and O(n) memory. Code.

→ Reply



7 months ago, # | 🏠

A 0

Great blog but I am not able to understand the logic behind the O(nlogn) solution it would be a great help if anyone can explain it.

→ Reply

7 months ago, # | 🏠

A 0

I have a question for style 3 i.e HLD style.

I'm not so sure what's happening in there, I have 2 assumptions. Both of them are wrong, so it would great if someone could point out the mistake and explain what's right.

We are in root.



i ne\_woitpac

- 1. We first go down the light edges of root and when we finish with them, we clear the cnt array, so there is absolutely nothing left in it and then we proceed to the heavy child of the root and then we just update cnt array.
  - Now we go back to the light edges of the root and (here's the problem) as the cnt array only contains information for the heavy child of the root, we must go through EVERY vertex in subtrees of light children of the root. If we don't go to the heavy children in the subtrees (as it proposes in tutorial?), then the answer is wrong, as we didn't count them (remember that we cleared the cnt array).
- 2. We first go down the light edges of the root, but this time, for every heavy child, we keep the information.
  - But then as we proceed to the heavy child of the root, the array cnt won't be empty and the answer for heavy child will be incorrect.

→ Reply



7 months ago, #  $^{\wedge}$  |  $^{\wedge}$ 

+9

Consider you entered vertex v, let it's heavy child h. First, go to all child of v except h and calculate the answer for them and each time clear the cnt array. Then go to h and

**Arpa** 

CAICUIALE LITE ATIONET ATIU UUTTI CIEAL LITE CITE ATIAY. TITETI LIAVETSE AII UL LITE SUDLIEE UL V except subtree of h, and add them to cnt.

→ Reply



+13

I got it, thanks for the quick reply!

→ Reply

The Wolfpack

7 months ago, # | 🏠

7 months ago, # | 🏠

+18



**Tanmoy Datta** 

Another problem can be solved with this technique. Arpa please add this one in the list.

http://codeforces.com/contest/1009/problem/F (Dominant Indices)

→ Reply



A 0

Can someone explain why this solution 40510312 is getting TLE on problem 600E - Lomsat gelral. I'm using style 4.

→ Reply

light--stars--dark



Irvideckis

7 months ago, # \_^ | 🏠

+8

Can't view your submission

→ Reply



+5

Firstly, thank you for reaching out to help:). I got my mistake.

→ Reply

light--stars--dark



7 months ago, # | 🏠

0

#### ChandyShot

THE CONTRIBUTION OF SECTION OF CONTRIBUTION OF SECTION OF SECTION

blog practice problem) while implementing through DSU similar to what is given here. Submission Id: 40780911, can somebody make a look over this and provide hint to optimize it.

→ Reply



new, 3 weeks ago, # ^ | \$

A 0

My solution passed the time limit after replacing endl with "\n".

→ Reply

m0nk3ydluffy

6 months ago, # | 🏠

A 0



rajarshi basu

This blog was a bit code-heavy for me when I first read this. Hence I have tried to simplify the concept a bit more in a more textual fashion in my own tutorial spin-off. I have tried to provide the intuition behind small-to-large merging including small to large on trees, also knows as DSU on trees.

However I. haven't provided any code as the code given by the OP is more than enough. DSU-on-Tree-Intuition

→ Reply





sagarthecoder2

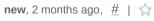
**new**, 2 months ago, # |  $\diamondsuit$ 

Method -3

WHy here use bigchild??

and why use "keep==0 "??

→ Reply



0



mra232200°

sorry but you absolutely wrong about the complexity, i know the trick merge smaller to greater but it works when you don't for(i = 0; i < greater.size(); i++) again, but here in O(nlogn ^ 2) you use cnt[v] = cnt[bigchild], it equal to "for(int i = 0; i < cnt[bigchild].size(); i++) {} ", so it's not O(nlogn ^2)

→ Reply



new, 2 months ago, # ^ | \$

Note that cnt[v] is a pointer.

→ Reply



new, 2 months ago, # ^ | 🏠

you mean that it take O(logn) time?

→ Reply



new, 2 months ago, # ^ | 😭

**0** 

A 0

A 0

O(1). → Reply

Arpa



new, 2 months ago, # ^ | 🏠

**0** 

got it, but how about the vector in your O(nlogn) time?

→ Reply



new, 2 months ago, # ^ | 🏠

A 0

It's pointer too, isn't it? → Reply

**Arpa** 



new, 2 months ago, # ^ | 🏠 thanks a lot, I got it.

→ Reply

mra2322001



new, 2 weeks ago, # | 🏠

Can someone explain, why will the complexity of the first code will be O(nlog^2n)?

→ Reply

tanmay28

**new**, 2 weeks ago, # ^ | 😭

+3

Every vertex will appear in 100 n cnt's every time we want to insert a vertex it costs

Every vertex will appear in was meant o, every time we want to insert a vertex it costs  $\log n$ , so the whole time complexity is  $\mathcal{O}(n \log^2 n)$ .



→ Reply

tanmay28

A 0

- 1. That means, if I use unordered\_map my complexity will reduce to O(nlogn)?
- 2. How can you say that every vertex will appear in log(n) cnt's?
- → Reply



**Arpa** 



- 1. Yes.
- 2. Read the proof of that for each vertex there is at most  $\log n$  light edges in the path between this vertex to root: Link.
- → Reply



new, 2 weeks ago, # ^ | 😭

A 0

Thanks:)

→ Reply

tanmay28



savinov

```
new, 2 weeks ago, # | 🏠
```

← Rev. 2



This particular problem can be solved in linear time:

```
int cnt[maxn];
```

```
void dfs(int v, int p){
    // Subtract cnt[c] for query here, e.g. answer[query] -= cnt[c];
    cnt[col[v]]++;
    for(auto u : g[v])
        if(u != p)
            dfs(u, v);
```

```
// Add cnt[c] for query here, e.g. answer[query] += cnt[c]; } \rightarrow \underline{\text{Reply}}
```

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