Heuristic Analysis:

The following three heuristics were used and tested:

Heuristic 1 (AB_Custom): It returns the difference in the number of available moves between the current player and its opponents one ply ahead and is used as the score of the current game state.

```
for move in p_moves:
    own_score += len(game.forecast_move(move).get_legal_moves())
for move in opp_moves:
    opp_score += len(game.forecast_move(move).get_legal_moves())
    return float(own_score - opp_score + len(p_moves) - len(opp_moves))
where,
    p_moves - Player moves
    opp_moves - Opponent's moves
```

Heuristic 2 (AB_Custom_2): Here we uses an empirical factor to reduce opponent moves. This is similar to IM improved but more aggressive in the sense that it weights the opponent legal moves in a ratio to player's legal moves before taking the difference.

```
return float(len(p_moves) - len(2*opp_moves))
p_moves - Player moves
opp_moves - Opponent's moves
```

Heuristic 3 (AB_Custom_3): If player has more options to move than his/her opponent that player has more probability of winning. Here we calculate the ratio of player to opponent moves.

Results:

| | | Win Rate: | 65.7% | | 60.0% | | 47.1% | | 47.1% | | |
|-------|-----|-------------|-------|---|---------------|-----|-----------------|-----|------------------|-----|------------------|
| 7 | | AB_Improved | 5 | 1 | 5 | 3 | 7 | 1 | 9 | 4 | 6 |
| 6 | | AB_Center | 7 | 1 | 3 | 6 | 4 | 5 | 5 | 5 | 5 |
| 5 | | AB_Open | 4 | 1 | 6 | 4 | 6 | 5 | 5 | 5 | 5 |
| 4 | | MM_Improved | 6 | 1 | 4 | 5 | 5 | 4 | 6 | 3 | 7 |
| 3 | | MM_Center | 9 | 1 | 1 | 9 | 1 | 5 | 5 | 5 | 5 |
| 2 | | MM_Open | 5 | 1 | 5 | 7 | 3 | 4 | 6 | 5 | 5 |
| 1 | | Random | 10 | 1 | 0 | 8 | 2 | 9 | 1 | 6 | 4 |
| Match | 1 # | 0pponent | Won | • | roved Lost | Won | ustom Lost | Won | stom_2 Lost | Won | stom_3 Lost |
| | | | | | | | | | | | |

Based on the results, it is recommended to use Heuristic 1 (AB_Custom) and can be justified as follows:

- 1. It is based on the number of moves looking ahead 1 ply in future.
- 2. The running time complexity is comparable to improved heuristic and should not directly effect the maximum depth searched.
- 3. As noted from the tournament results, Heuristic 1 perform better than heuristic 2 and 3.
- 4. Isolation game where L shaped moves are allowed, it is difficult to predict game state by just counting immediately available moves. One ply lookahead strategy can provide more accurate evaluation function.