

This question paper contains 4 printed pages]

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S. No. of Question Paper : 52

Unique Paper Code : 32341502

Name of the Paper : Theory of Computation

Name of the Course : B.Sc. (H.) Computer Science

Semester : V

Duration : 3 Hours

Maximum Marks : 75

(Write your Roll No. on the top immediately on receipt of this question paper.)

Instructions for Candidates :

- (1) All questions from Part A are compulsory. Attempt any four questions from Part B.
- (2) Assume  $\Sigma = \{a, b\}$  is the underlying alphabet unless mentioned otherwise. Parts of a question must be answered together.

**Part A**

1. (a) Prove that for all sets  $S$ ;  $(S^+)^* = S^*$ . 2
- (b) Give regular expression for the language of all strings that do not end with double letter. 2

P.T.O.



- (c) Show that  $(ab)^*a$  and  $a(ba)^*$  defines the same language over alphabet  $\{a, b\}$ . 3
- (d) Build an FA that accepts only those words that have exactly four letters. 4
- (e) Build an FA that accepts only those words that do not end with  $ba$ . 4
- (f) Find a CFG for the language  $\text{Trailing count} = \{sa^{\text{length}(s)} \mid s \in (a+b)^*\}$  for all  $s$  in  $(a+b)^*$ . 4
- (g) Use the pumping lemma to show that the language  $\text{Square} = \{a^n \mid n \text{ is a square}\}$  is non-regular. 4
- (h) Show that if  $L_1$  and  $L_2$  are regular language then so are  $L_1 + L_2$ ,  $L_1 L_2$  and  $L_1^*$ . 4
- (i) Construct a PDA for the language  $L = \{a^n b^{2n} \mid n = 0, 1, 2, 3, \dots\}$ . 4
- (j) Design a right shifting turing machine. 4



## Part B

2. (a) Define Regular Expression. 2
- (b) Build a regular expression for all words that have odd no. of b's. 3
- (c) Build an FA that accepts all strings that start and end with different letters. 5
3. (a) For languages,  $L_1 = (a+b)^*a$  and  $L_2 = (a+b)^*aa(a+b)^*$ , find the deterministic finite automata for  $L_1 + L_2$ . 6
- (b) Show that the following context free grammar is ambiguous : 4
- $$S \rightarrow aSb \mid Sb \mid Sa \mid a.$$
4. (a) Use the pumping lemma to show that the language  $a^n b a^n$  where  $n=1, 2, 3, \dots$  is non-regular. 4
- (b) For the given,  $L_1 = (a+b)^*a$  and  $L_2 = b(a+b)^*$ , find the automata and regular expression for  $L_1 \cap L_2$ . 6
5. (a) Construct a PDA for the language  $a^n b^m a^n$  where  $m, n \geq 1$ . 6
- (b) Construct a CFG for the language  $(ba+ab)^*$ . 4

P.T.O.



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6. (a) Prove that a recursive language is also recursively enumerable. 6
- (b) Using pumping lemma prove that the language  $a^n b^n a^n b^n$  for  $n=1, 2, 3, \dots$  is non-context free. 4
7. (a) Design a turing machine for the language  $a^n b^n c^n$  where  $n=1, 2, 3, \dots$  6
- (b) Describe "Universal Turing Machine". 4

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