

# Particles

A particle is an object of class `particle`, which is a subclass of `point`. Essentially, `particle` adds a mass property to `point`, and methods to compute useful quantities such as the linear and angular momentum or the kinetic energy. This tutorial focuses on the specific aspects of `particle`.

Start by importing the Anakin framework into Matlab. Be sure to include Anakin's base directory before you run this line:

```
import anakin.*
```

## Object creation

The default particle has mass 1 and is located at the canonical origin:

```
P = particle% default call
```

```
P =  
Particle with mass:  
    1  
  
canonical position vector components:  
    0  
    0  
    0
```

A particle can be created by passing their mass and its position vector or its canonical coordinates:

```
m = 20;  
rA = tensor([1;2;3])
```

```
rA =  
Vector with canonical components:  
    1  
    2  
    3
```

```
P = particle(m,rA) % as a vector
```

```
P =  
Particle with mass:  
   20  
  
canonical position vector components:  
    1  
    2  
    3
```

```
P = particle(20,[4;5;6]) % as a column array
```

```

P =
Particle with mass:
    20

canonical position vector components:
    4
    5
    6

```

```
P = particle(30,[7,8,9]) % as a row array
```

```

P =
Particle with mass:
    30

canonical position vector components:
    7
    8
    9

```

The components that define the position of the particle can be given in another reference frame. Internally, the point object stores only its coordinates in the canonical reference frame:

```

O1 = point([1;2;3]);
B1 = basis([1;0;0],[0;cos(pi/6);sin(pi/6)],[0;-sin(pi/6);cos(pi/6)]);
S1 = frame(O1,B1);

P = particle(30,[1,1,1],S1)

```

```

P =
Particle with mass:
    30

canonical position vector components:
    2.0000
    2.3660
    4.3660

```

## Basic functionality

The linear, angular momentum and the kinetic energy of the particle in a given reference frame are:

```

O1 = point([1;2;3]);
S1 = frame(O1);
P = particle(1,[1,1,1],S1);

% linear momentum
P.p % use default reference frame: canonical frame

```

```

ans =
Vector with canonical components:
    0
    0

```

0

P.p(S1)

```
ans =  
Vector with canonical components:  
0  
0  
0
```

```
% angular momentum  
P.H(01) % the point about which the angular momentum is computed
```

```
ans =  
Vector with canonical components:  
0  
0  
0
```

P.H(01,S1)

```
ans =  
Vector with canonical components:  
0  
0  
0
```

```
% kinetic energy  
P.T
```

```
ans =  
Scalar with value:  
0
```

P.T(S1)

```
ans =  
Scalar with value:  
0
```

The tensor of inertia of the particle about a point can be easily computed as:

```
inertia = P.inertia
```

```
inertia =  
Second-order tensor with canonical components:  
25.0000  -6.0000  -8.0000  
-6.0000  20.0000 -12.0000  
-8.0000 -12.0000  13.0000
```

## Symbolic particles

Particles with symbolic position or mass have additional functionality (running this requires the Symbolic Math Toolbox installed):

```
syms t xi(t) eta(t) zeta(t) phi(t); % declare symbolic variables
assume([in(t, 'real'), in(xi(t), 'real'), in(eta(t), 'real'), in(zeta(t), 'real'), in(phi(t),
P = particle(2,[xi,eta,zeta]) % a symbolic point
```

```
P =
Particle with mass:
    2

canonical position vector components:
    xi(t)
    eta(t)
    zeta(t)
```

To particularize a symbolic particle at particular values of its parameters, one may use `subs`, by specifying them in a list:

```
P.subs({xi},{6}) % replace xi with 6
```

```
ans =
Particle with mass:
    2

canonical position vector components:
    6
    eta(t)
    zeta(t)
```