Program Structures and Algorithms

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NAME: Ashish Nevan Gade

NUID: 002889005

GITHUB LINK: https://github.com/AshishNevan/INFO6205

**Task:**

1. Implement height-weighted Quick Union with Path Compression
2. Using your implementation of UF\_HWQUPC, develop a UF ("union-find") client that takes an integer value n from the command line to determine the number of "sites." Then generates random pairs of integers between 0 and n-1, calling connected to determine if they are connected and union) if not. Loop until all sites are connected then print the number of connections generated.
3. Determine the relationship between the number of objects (n) and the number of pairs (m) generated to accomplish this (i.e. to reduce the number of components from n to 1). Justify your conclusion in terms of your observations and what you think might be going on.

**Relationship Conclusion:**

The relationship between the number of objects (n) and the number of pairs (m) generated to connect all objects and reduce the number of components to 1 is linear. For 'n' objects, 'n-1' pairs are generated. This linear relationship is expected because each pair of objects (sites) forms one union operation, and 'n-1' such operations are required to connect all objects into one component.

**Evidence to support that conclusion:**

In the union-find algorithm, we aim to connect all the objects (sites) until they form a single component. We repeatedly generate pairs of integers and use the connected() and union() operations to connect them until there is only one component left.

Each time we call union() operation, it merges two components into one. Initially, we have 'n' components (one component for each object). As we perform union operations, the number of components decreases until there is only one component left, indicating that all objects are connected.

The number of pairs (m) generated to accomplish this can be analyzed as follows:

* Initially, we have 'n' components.
* With each union() operation, the number of components decreases by 1.
* So, after 'n-1' union operations, there will be only one component left.
* Therefore, the number of pairs (m) generated to reduce the number of components from 'n' to 1 is 'n-1'.

A table with numbers and text

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Figure 1: Number of components vs Number of connections

A screenshot of a computer

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Figure 2: Union Find Client

**Unit Test Screenshots:**

A screenshot of a computer

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