

## Bitwise Operators

Check kth bit is set ✓

Count set bits ✓

Power of two ✓

Find only odd occurring numbers ✓

Find two odd appearing numbers ✓

Power set using bitwise Operators

Find the two non-repeating elements in an array of repeating elements ✓

Count number of bits to be flipped to convert A to B

Count total set bits in all numbers from 1 to n

Calculate square of a number without using  $*$ ,  $/$  and  $\text{pow}()$

Divide two integers without using multiplication, division and mod operator

Find position of the only set bit

set the ith bit ✓

Clear the ith bit ✓

Toggle the ith bit

A

B

Bitwise Operators

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Count set bits

Power of two

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Divide two integers without using multiplication, division  
and mod operator

Find position of the only set bit

set the ith bit

Clear the ith bit

Toggle the ith bit

Naive  
Solution

```
void isSet(int n, int k)
```

```
{  
    int x = 1;
```

```
    for (int i = 0; i < (k-1); i++)
```

```
        x = x * 2;
```

```
    if ((n & x) != 0)
```

```
        print("yes")
```

```
    else
```

```
        print("No")
```

$n = 5$  (0...0101)

$k = 3$

After loop:

$x = 4$  (0...0100)

0 ... 0101

& 0 ... 0100

0 ... 0100



Representation



Naive  
Solution

```
void isSet(int n, int k)
```

```
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```

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    int x = 1;
```

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        print("yes")
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```
}
```

$n = 5$  (0...0101)

$x = 3$

After loop:

$x = 4$  (0...0100)

0 ... 0101

& 0 ... 0100

0 ... 0100



Representation  
of 4.

Alternate

Naive sol<sup>n</sup>

We Reduce

$n$  to  $\lfloor n/(2^{k-1}) \rfloor$

Time:  $\Theta(k)$

void isSet(int n, int k)

{

for(int i=0; i<(k-1); i++)

$n = n/2;$

if((n <> 0) != 0)

print("yes")

else

print("No")

}

$n = 5$  (0..0101)

$k = 3$

After loop

$n = 1$  (0..0001)

## Efficient Method I

void isKthSet(int n, int k)

{

int x = (1 << (k-1)); //  $2^{k-1}$

if ((n & x) != 0)

print("yes");

else

print("No");

}

n=5 (00...0101)

k=3

x=4 (00...0100)

00...0101

2 00...0100

00...0100

## Efficient Method II

(int n, int k)



## Efficient Method II

void isKthSet(int n, int k)

{  
int x = (n >> (k-1)); //  $\lfloor n / 2^{k-1} \rfloor$

if ((x & 1) != 0)

print("yes")

else

print("No")

}

00 ... 0100

$n = 5$  (00 ... 0101)

$k = 3$

$x = 1$  (00 ... 0001)

00 ... 0001     $x$

& 00 ... 0001    1

00 ... 0001

Ans

## Count Set Bits

I/P:  $n=5$

O/P: 2

$n=5$

101

Binary  
Representation.

$$\begin{array}{r} 101 \\ \underline{2} \\ 2 \\ \underline{2} \\ 5 \end{array} \Rightarrow 1$$

Count  $\rightarrow 0$

1

2

I/P:  $n=7$

O/P: 3

$n=7$

111

$$\begin{array}{r} 111 \\ \underline{2} \\ 1 \\ \underline{2} \\ 3 \end{array} \Rightarrow 0$$

I/P:  $n=13$

O/P: 3

$n=13$

1101

$$\begin{array}{r} 1101 \\ \underline{2} \\ 1 \\ \underline{2} \\ 3 \end{array} \Rightarrow 1$$

Naive Solution

$n=0$

Last bit



```
int countSetBits(int n)
```

```
{  
    int res = 0;
```

```
    while(n > 0)
```

```
    {  
        if (n % 2 == 1)
```

```
            res++;
```

```
        n = n / 2;
```

```
    }  
    return res;
```

Time =  $\Theta(d)$

n = 5 (00...0101)

res = 0

Ist Iteration -

res = 1, n = 2 (00...010)

IInd Iteration -

res = 1, n = 1 (00...001)

III<sup>rd</sup> Iteration -

res = 2, n = 0 (00...000)

int CountSetBits (int n)

{

int res=0;

while(n>0)

{ if (n%2 == 1) {  
res++;

res = res + (n & 1);

n = n/2;

return res;

n  
5

n = 101 →

run  
5 × 2 = 10  
1 + 1

run

0

101

001

001

10

01

00

1

1

Ques 1

Brian  
Kerningham's  
Algorithm

Idea:

Traverse through  
only the set bits.

Time:  $\theta(\text{set bits})$

```
int countSetBits(int n)
{
    int res = 0;
    while (n > 0)
```

{  
  $n = n \& (n - 1)$  → This expression should make the last set bit as 0.  
  $res = res + 1;$

$n = 40 (101000)$

After 1<sup>st</sup> Iteration

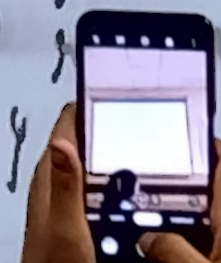
$n = 32 (100000)$

After 2<sup>nd</sup> Iteration

$n = 16 (010000)$

$n = 10 - 1010 \rightarrow$   
 $(n-1) = 9 - 1001$   
 $\begin{array}{r} 1010 \\ - 1001 \\ \hline 0011 \end{array}$   
 $8 \leftarrow 1000$   
 $7 \leftarrow 0111$   
 $\begin{array}{r} 1000 \\ - 0111 \\ \hline 0001 \end{array}$

$res$   
2





Time:  $O(\text{set bits})$  Return ans; }  
After II<sup>nd</sup> Iteration

int CountSetBits (int n)

{ int ans = 0;

while (n > 0)

{ ans += (n & 1);

n = n >> 1;

}

```
int CountSetBits(int n)
```

```
{
```

```
    int res = 0;
```

```
    while (n > 0)
```

```
    {
```

```
         $n = n \& (n-1);$ 
```

```
        res = res + 1;
```

```
    }
```

```
    return res;
```

```
}
```

$$n = 40 : 101000$$

$$(n-1) = 39 : 100111$$

$$n \& (n-1) = 32 : 100000$$

$$n = 32 : 100000$$

$$n-1 = 31 : 011111$$

$$n \& (n-1) = 0 : 000000$$

If we subtract a number by 1 and do it bitwise & with itself ( $n \& (n-1)$ ), we must the rightmost set bit

## Power of Two

naïve

Ip:  $n=9$

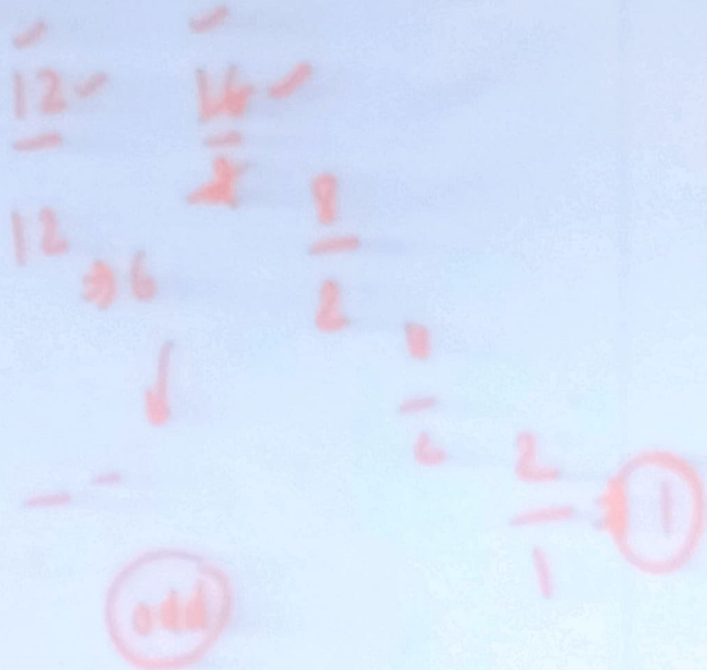
Op: True

Ip:  $n=6$

Op: False

Ip:  $n=1$

Op: True



## Naive Solution

1) Explicitly Hand



4) Repeating

$$n=6$$

I<sup>st</sup> Iteration:  $n=3$

II<sup>nd</sup> Iteration: return false

$$n=8$$

I<sup>st</sup> Iteration:  $n=4$

II<sup>nd</sup> Iteration:  $n=2$

III<sup>rd</sup> Iteration:  $n=1$

return true

bool isPow2(int n)

{

if ( $n==0$ )

return false;

while ( $n!=1$ )

{

if ( $(n/2 != 0)$ )

return false;

$n = n/2;$

}

return true;

$$16$$

$$9$$

$$⑧ \frac{16}{8} \rightarrow 0 \quad 64 \rightarrow$$

$$8$$

$$32$$

$$8$$

$$8$$

$$8$$

$$8$$

$$4$$

$$2$$

$$2$$

$$① \frac{4}{2} \rightarrow 0$$

4: 00...0100

$n=4$ : 00...0100

$k(n-1)=3$ : 00...0010

00...0000

$n=6$ : 00...0110

$k(n-1)=5$ : 00...0101

00...0100

bool isPow2(int n)

{  
  if(n==0)  
    return 0;

  return ((n & (n-1)) == 0);

}  
  
return (n & ((n & (n-1)) == 0))

Find the only Odd Occurring Number

I/p: arr[] = {4, 3, 4, 4, 4, 5, 5}

O/p: 3

I/p: arr[] = {8, 7, 7, 8, 8}

O/p: 7

Naive  
Solution

int find (int arr[], int n)

100  
011  
111  
100  
011  
100  
111  
100  
011  
101  
110  
101  
011 → ③



Naive

Solution

int findOdd(int arr[], int n)

{  
for(int i=0; i<n; i++)

{  
int count=0;

for(int j=0; j<n; j++)

if(arr[i] == arr[j])

count++;

if(count % 2 != 0)

return arr[i];

}

}

1 0 1  
0 1 1 → ③

```
int findodd(int arr[], int n)
```

```
{
```

```
    int res = arr[0];
```

```
    for(int i=1; i<n; i++)
```

```
        res = res ^ arr[i];
```

```
    return res;
```

```
}
```

Time:  $\Theta(n)$

Aux space:  $O(1)$

arr =

{4, 4, 7, 4, 8, 7, 7, 8}

$4 \wedge 4 \wedge 7 \wedge 4 \wedge 8 \wedge 7 \wedge 7 \wedge 8$

$= (4 \wedge 4 \wedge 4) \wedge (7 \wedge 7 \wedge 7) \wedge (8 \wedge 8)$

$= 4 \wedge 0 \wedge 0$

$= 4 \wedge 0$

$= 4$

$4 \wedge 4 \wedge 7 \wedge 4 \wedge 8 \wedge 7 \wedge 7 \wedge 8$

1) XOR of any num

2) XOR of any num

$n \wedge n = 0$

$0 \wedge 0 = 0$

## Find Two Odd Appearing Numbers

I/p: arr[] = {3, 4, 3, 4, 5, 4, 4, 6, 7, 7}

O/p: 5 6

I/p: arr[] = {1, 3, 2, 3, 3, 1}

O/p: 2 3

### Naive Solution

Traverse through the array, Count Occurrences of every number. If count is odd, print the



```
void printodd(int arr[], int n)
```

```
{
```

```
    for(int i=0; i<n; i++)
```

```
    {
```

```
        int count=0;
```

```
        for(int j=0; j<n; j++)
```

```
            if(arr[i] == arr[j])
```

```
                count++;
```

```
            if(count % 2 != 0)
```

```
                print(arr[i]);
```

```
    }
```

```
}
```

```
Void printodd(int arr[], int n)
```

```
{
```

```
for(int i=0; i<n; i++)
```

```
{
```

```
int count=0;
```

```
for(int j=0; j<n; j++)
```

```
if(arr[i] == arr[j])  
    count++;
```

```
if(count % 2 != 0)
```

```
    print(arr[i]);
```

```
}
```

```
}
```

Void oddAppearing(int arr[], int n)

{

int x = arr[0];

for(int i=1; i<n; i++)

x = x ^ arr[i];

//right set bit

int x = (x & (~(x-1)));

int res1 = 0, res2 = 0;

for(int i=0; i<n; i++)

{ if ((arr[i] & x) != 0)

res1 = res1 ^ arr[i];

else

res2 = res2 ^ arr[i];

}

printf("res1, res2");

}

x=3: 00.... 0011

x-1=2: 00.... 0010

~(x-1): 11.... 1101

x & ~(x-1): 00.... 0001

arr = {1, 6, 5, 6, 6, 1}

x = 1 ^ 6 ^ 5 ^ 6 ^ 6 ^ 1 = 3

x = 1

res1 = 1 ^ 5 ^ 1 = 5

res2 = 6 ^ 6 ^ 6 = 6

10 → 1010

~9 → 1001

0110

5 → 0101

6 → 0110

10 → 1010

6 → 0110

10 → 1010

6 → 0110

3 → 0011

3 → 0011