ساختمان داده و الگوريتم ها (CE203)

جلسه هشتم: ليست و پشته

سجاد شیرعلی شهرضا پاییز 1401 شنبه، 30 مهر 1401

اطلاع رساىي

- بخش مرتبط كتاب براى اين جلسه: 10
- أمتحانكُ دوم (كه در حقيقت اولين امتحانك است!): ٥ دوشنبه هفته آينده، 9 آبان 1401

 - در طی ساعت کلاس به صورت حضوری

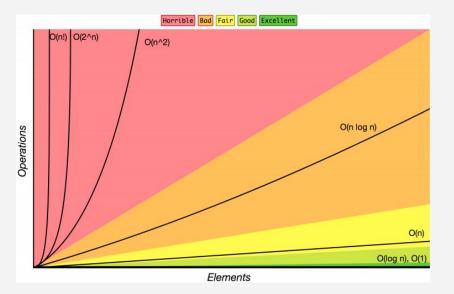
لیست

مجموعه ای ترتیب دار از اشیاء

Complexity Class

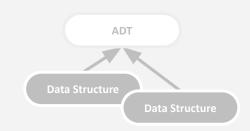
• Complexity Class: a category of algorithm efficiency based on the algorithm's relationship to the input size N

Complexity Class	Big-O	Runtime if you double N
constant	0(1)	unchanged
logarithmic	O(log ₂ N)	increases slightly
linear	O(N)	doubles
log-linear	O(N log ₂ N)	slightly more than doubles
quadratic	O(N ²)	quadruples
exponential	O(2 ^N)	multiplies drastically



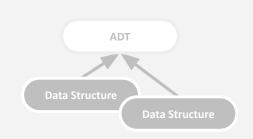
ADTs: Abstract Data Types

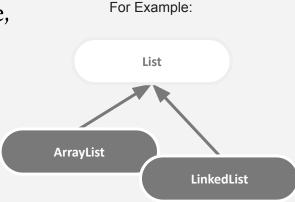
- Abstract Data Type (ADT): a data type that does not specify any one implementation.
 - o An agreement about what is provided, but not how



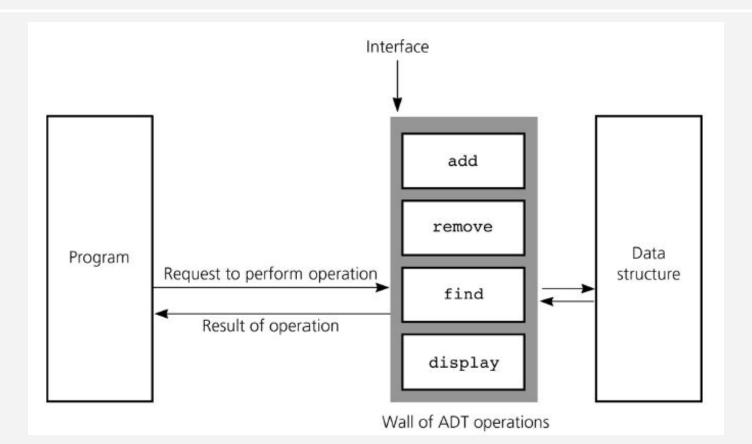
ADTs: Abstract Data Types

- Abstract Data Type (ADT): a data type that does not specify any one implementation.
 - An agreement about what is provided, but not how
- Data Structures implement ADTs
 - Resizable array can implement List, Stack, Queue,Deque, PQ, etc.
 - Linked nodes can implement List, Stack, Queue,
 Deque, PQ, etc.





Another View of ADT



List ADT

- **List**: a collection storing an ordered sequence of elements.
 - Each item is accessible by an index.
 - A list has a variable size defined as the number of elements in the list
 - Elements can be added to or removed from any position in the list
- Relation to code/mental image of a list:

List Implementations

LIST ADT

State

Set of ordered items Count of items

Behavior

get(index) return item at index
set(item, index) replace item at index
add(item) add item to end of list
insert(item, index) add item at index
delete(index) delete item at index
size() count of items

[88.6, 26.1, 94.4]

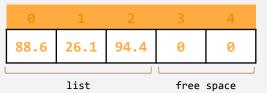
ArrayList<E>

State

data[] size

Behavior

get return data[index]
set data[index] = value
add data[size] = value, if out
of space grow data
insert shift values to make hole
at index, data[index] = value,
if out of space grow data
delete shift following values
forward
size return size



LinkedList<E>

State

Node front; size

Behavior

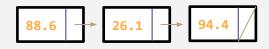
get loop until index, return node's
value

set loop until index, update node's
value

<u>add</u> create new node, update next of last node

insert create new node, loop until
index, update next fields

delete loop until index, skip node
size return size



ArrayList Storage

- Stores elements inside an array
 - Has a fixed capacity
 - Typically has more space than currently used
- Stores all of these elements at the front of the array
 - Keeps track of how many items added

```
List View ArrayList View ("Paul", "Leona", "Ryan", null, null, null, null]
```

ArrayList Insert

ArrayList<E>

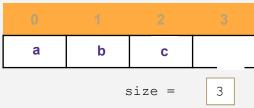
State

data[] size

Behavior

get return data[index]
set data[index] = value
add data[size] = value, if out
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insert shift values to make hole
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delete shift following values
forward
size return size

insert(element, index) with shifting



ArrayList Insert

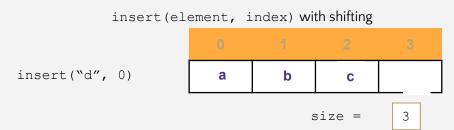
ArrayList<E>

State

data[]
size

Behavior

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ArrayList Insert

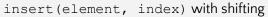
ArrayList<E>

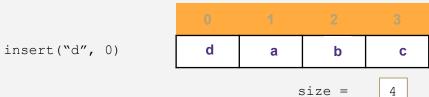
State

data[]
size

Behavior

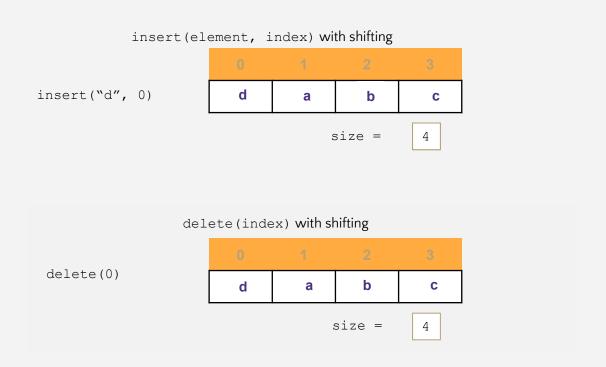
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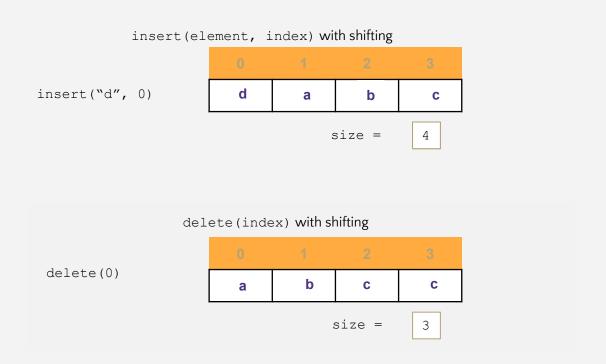
ArrayList Delete

ArrayList<E> State data[] size Behavior get return data[index] set data[index] = value add data[size] = value, if out of space grow data insert shift values to make hole at index, data[index] = value, if out of space grow data <u>delete</u> shift following values forward <u>size</u> return size



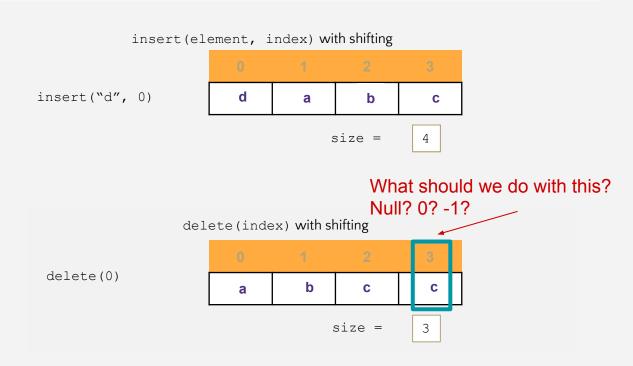
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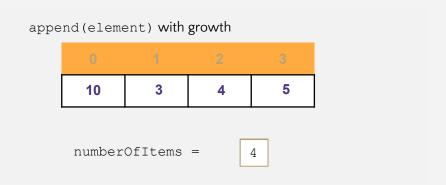
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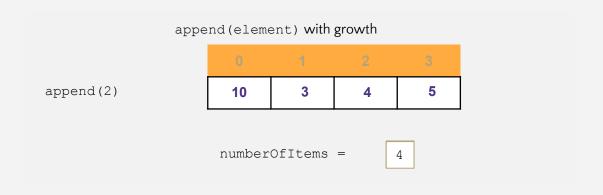
ArrayList Insert - with Expansion

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ArrayList Insert - with Expansion

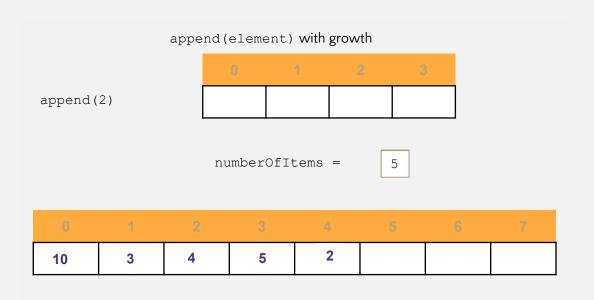
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What should we do?

ArrayList Insert - with Expansion

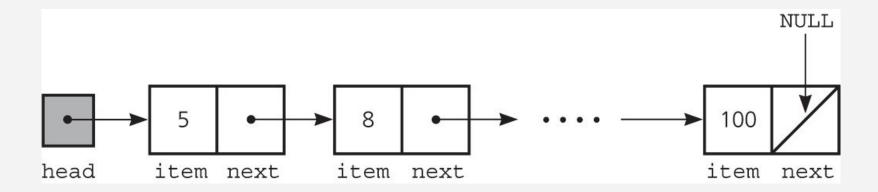
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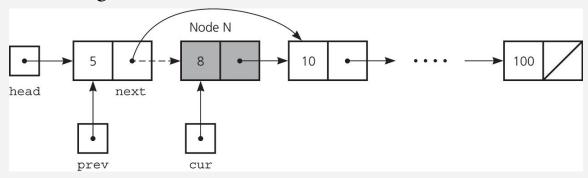
لیست پیوندی

Sample Linked List

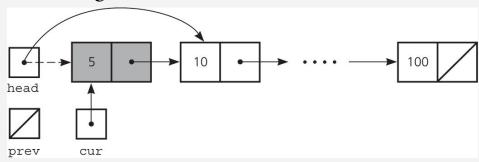


Delete from a Linked List

Deleting a node in the middle

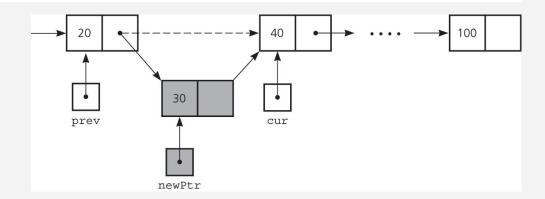


Deleting the first node

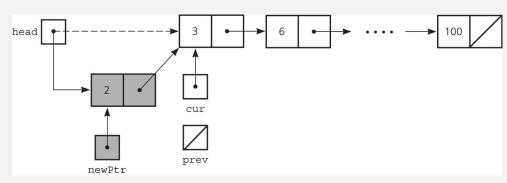


Insert into a Linked List

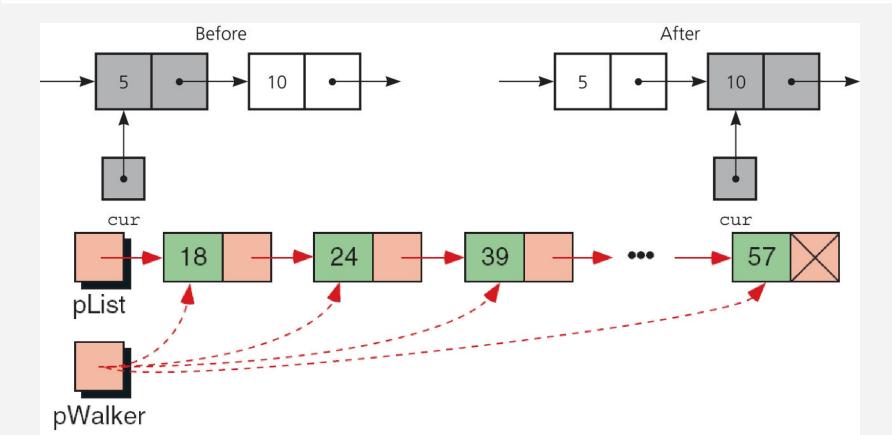
• Insert between two nodes



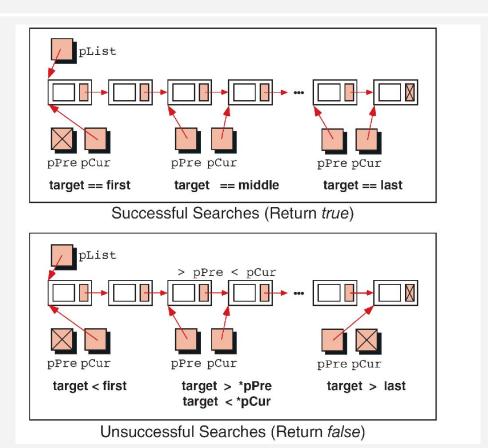
• Insert at the beginning



Traverse a Linked List

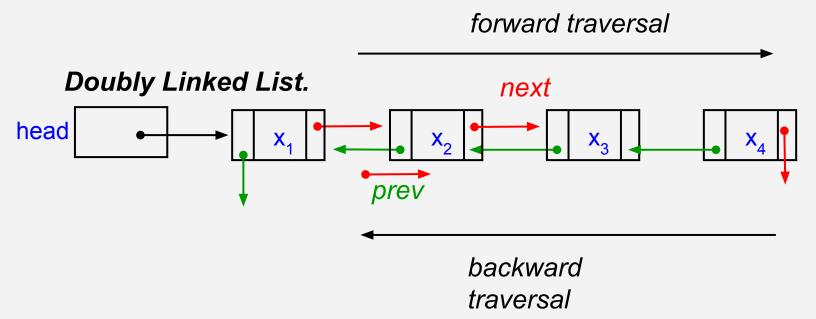


Search in Sorted Linked List



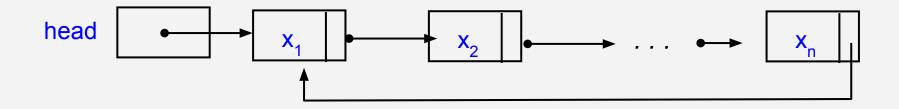
Doubly Linked Lists

• Sometimes we need to traverse a sequence in BOTH directions efficiently



Circular Linked List

- May need to cycle through a list repeatedly
 - E.g., round robin system for a shared resource





انتخاب ساختمان داده مناسب

Design Decisions

- For every ADT, many ways to implement
- Based on our situation we should consider:
 - Speed vs Memory Usage
 - Generic/Reusability vs Specific/Specialized
 - One Function vs Another
 - Robustness vs Performance
- Our job is selecting **the best** ADT implemention by making **the right design tradeoffs!**
 - A common topic in interview questions

Example Problem

- Akbar Joojeh is implementing a new system to manage orders
- A new order comes in -> place it at the end of orders
- Food is prepared in approximately the same order it was requested
 - Sometimes orders are fulfilled out of order



Example Problem

- Akbar Joojeh is implementing a new system to manage orders
- A new order comes in -> place it at the end of orders
- Food is prepared in approximately the same order it was requested
 - Sometimes orders are fulfilled out of order

- Let's represent tickets using the List ADT
 - What implementation should we use?
 - ∘ Why?



What implementation should we use? Why?

- ArrayList
 - Creating a new order is very fast (as long as we don't have to resize)
 - Cooks can see any given order easily
- LinkedList
 - Creating an order is slower (have to iterate through whole list)
 - We'll mostly be removing from the front of the list, which is fast because it requires no shifting

Comparing ADT Implementations: List

	ArrayList	LinkedList
add (front)	linear	constant
remove (front)	linear	constant
add (back)	(usually) constant	linear
remove (back)	constant	linear
get	constant	linear
put	linear	linear

Comparing ADT Implementations: List

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remove (back)	constant	linear
get	constant	linear
put	linear	linear

- Important to be able to come up with this, and understand why
- But only half the story: to be able to make a design decision, need the context to understand which of these we should prioritizea

Conclusion

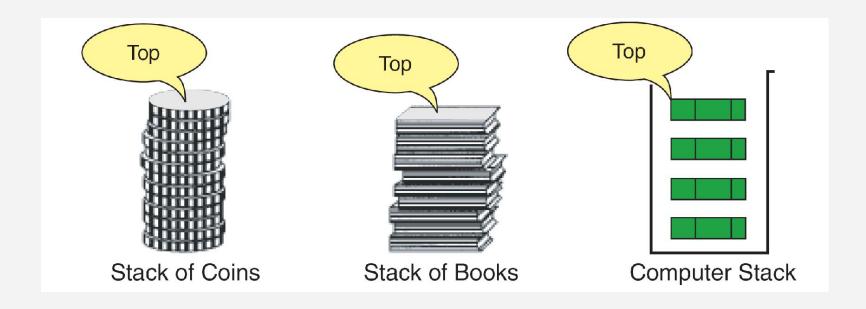
- Both ArrayList and LinkedList have pros and cons
 - Neither is strictly better than the other
- The Design Decision process:
 - Evaluate pros and cons
 - Decide on a design
 - Defend your design decision
- This is a major objective of the course!





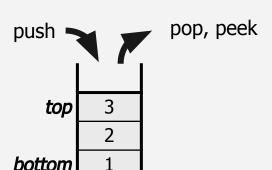
مجموعه ای از اشیاء روی هم قرار گرفته

Idea



Stack ADT

- An ADT representing an ordered sequence of elements
- Elements can only be added & removed from one end.
- Last-In, First-Out (LIFO)
- Elements stored in order of insertion
 - Don't think of them as having indices
- Clients can only add/remove/examine the "top"



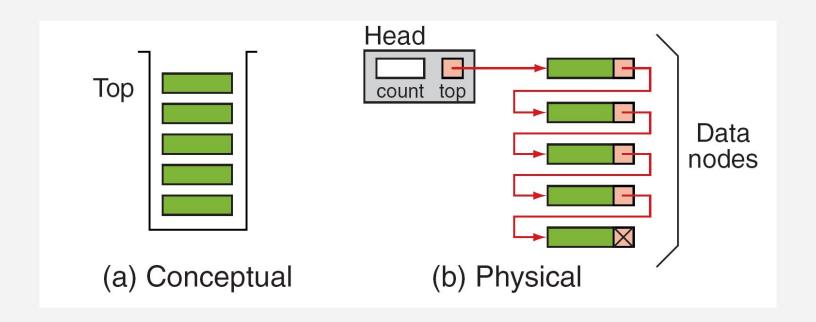
STACK ADT

State

Collection of ordered items Count of items

Behavior

push(index) add item to top pop() return & remove item at top peek() return item at top size() count of items isEmpty() is count 0?



STACK ADT

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LinkedStack<E>

State

Node top size Behavior

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top ----

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push(3)



STACK ADT

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LinkedStack<E>

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Node top size Behavior

push add new node at top
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push(3)
push(4)



STACK ADT

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push(3)
push(4)

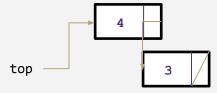
LinkedStack<E>

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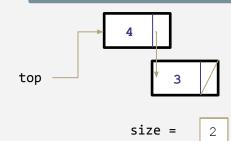
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push(3)
push(4)
pop()



STACK ADT

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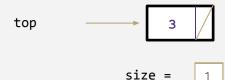
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LinkedStack<E>

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Node top size Behavior

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```
Big-Oh Analysis
```

pop()

peek()

size()

isEmpty()

push()

```
push(3)
push(4)
pop()
```



STACK ADT

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LinkedStack<E>

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Node top size Behavior

push add new node at top
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size return size

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```
Big-Oh Analysis
```

pop() O(1) Constant

peek()

size()

isEmpty()

push()

```
push(3)
push(4)
pop()
```



size =

1

STACK ADT

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Collection of ordered items Count of items

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LinkedStack<E>

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Big-Oh Analysis

pop() O(1) Constant

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LinkedStack<E>

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Big-Oh Analysis

pop() O(1) Constant

peek() O(1) Constant

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isEmpty()
push()

push(3)
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top ______ 3

STACK ADT

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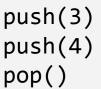
pop() O(1) Constant

peek() O(1) Constant

size() O(1) Constant

isEmpty() O(1) Constant

push() O(1) otherwise







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STACK ADT

State

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Behavior

push(index) add item to top pop() return & remove item at top peek() return item at top size() count of items isEmpty() is count 0?

ArrayStack<E>

State

```
data[]
size
Behavior

push data[size] = value, if
out of room grow data
pop return data[size - 1],
size -= 1
peek return data[size - 1]
size return size
```

isEmpty return size == 0

STACK ADT

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push(index) add item to top pop() return & remove item at top peek() return item at top size() count of items isEmpty() is count 0?

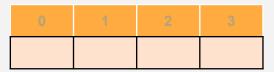
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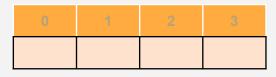
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ArrayStack<E> State data[] size Behavior push data[size] = value, if out of room grow data pop return data[size - 1], size -= 1 peek return data[size - 1] size return size



isEmpty return size == 0

STACK ADT

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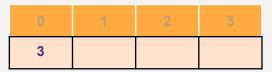
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0	1	2	3
3			

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pop return data[size - 1],
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peek return data[size - 1]
size return size
isEmpty return size == 0

0	1	2	3
3	4		

STACK ADT

State

Collection of ordered items
Count of items

Behavior

push(index) add item to top
pop() return & remove item
at top
peek() return item at top
size() count of items
isEmpty() is count 0?

push(3)
push(4)
pop()

ArrayStack<E>

State

data[] size

Behavior

push data[size] = value, if
out of room grow data
pop return data[size - 1],
size -= 1
peek return data[size - 1]
size return size
isEmpty return size == 0

1	

STACK ADT

State

Collection of ordered items Count of items

Behavior

push(index) add item to top
pop() return & remove item
at top
peek() return item at top
size() count of items
isEmpty() is count 0?

push(3)
push(4)
pop()

ArrayStack<E>

State

data[]
size

Behavior

push data[size] = value, if
out of room grow data
pop return data[size - 1],
size -= 1
peek return data[size - 1]
size return size
isEmpty return size == 0

3	0 1 2 3
3	

STACK ADT

State

Collection of ordered items Count of items

Behavior

push(index) add item to top
pop() return & remove item
at top
peek() return item at top
size() count of items
isEmpty() is count 0?

push(3)
push(4)
pop()
push(5)

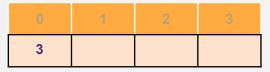
ArrayStack<E>

State

data[]
size

Behavior

push data[size] = value, if
out of room grow data
pop return data[size - 1],
size -= 1
peek return data[size - 1]
size return size
isEmpty return size == 0



size =

1

STACK ADT

State

Collection of ordered items Count of items

Behavior

push(index) add item to top
pop() return & remove item
at top
peek() return item at top
size() count of items
isEmpty() is count 0?

push(3)
push(4)
pop()
push(5)

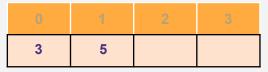
ArrayStack<E>

State

data[] size

Behavior

push data[size] = value, if
out of room grow data
pop return data[size - 1],
size -= 1
peek return data[size - 1]
size return size
isEmpty return size == 0



size =

2

STACK ADT

State

Collection of ordered items Count of items

Behavior

push(index) add item to top
pop() return & remove item
at top
peek() return item at top
size() count of items
isEmpty() is count 0?

push(3)
push(4)
pop()
push(5)

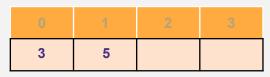
ArrayStack<E>

```
State

data[]
size

Behavior

push data[size] = value, if
out of room grow data
pop return data[size - 1],
size -= 1
peek return data[size - 1]
size return size
isEmpty return size == 0
```



```
size =
```

2

```
Big-Oh Analysis
pop()
peek()
size()
isEmpty()
```

push()

STACK ADT

State

Collection of ordered items Count of items

Behavior

push(index) add item to top
pop() return & remove item
at top
peek() return item at top
size() count of items
isEmpty() is count 0?

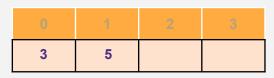
push(3) push(4) pop() push(5)

ArrayStack<E>

```
State

data[]
size
Behavior

push data[size] = value, if
out of room grow data
pop return data[size - 1],
size -= 1
peek return data[size - 1]
size return size
isEmpty return size == 0
```



```
size = 2
```

```
Big-Oh Analysis
pop() O(1) Constant
peek()
size()
isEmpty()
push()
```

STACK ADT

State

Collection of ordered items Count of items

Behavior

push(index) add item to top
pop() return & remove item
at top
peek() return item at top
size() count of items
isEmpty() is count 0?

push(3)
push(4)
pop()
push(5)

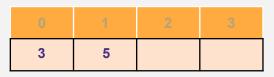
ArrayStack<E>

```
State

data[]
size

Behavior

push data[size] = value, if
out of room grow data
pop return data[size - 1],
size -= 1
peek return data[size - 1]
size return size
isEmpty return size == 0
```



```
size =
```

2

```
Big-Oh Analysis
pop() O(1) Constant
peek() O(1) Constant
size()
isEmpty()
push()
```

STACK ADT

State

Collection of ordered items Count of items

Behavior

push(index) add item to top
pop() return & remove item
at top
peek() return item at top
size() count of items
isEmpty() is count 0?

push(3)
push(4)
pop()
push(5)

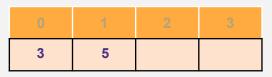
ArrayStack<E>

State

data[]
size

Behavior

push data[size] = value, if
out of room grow data
pop return data[size - 1],
size -= 1
peek return data[size - 1]
size return size
isEmpty return size == 0



```
size = 2
```

```
Big-Oh Analysis
pop() O(1) Constant
peek() O(1) Constant
size() O(1) Constant
isEmpty()
push()
```

STACK ADT

State

Collection of ordered items Count of items

Behavior

push(index) add item to top
pop() return & remove item
at top
peek() return item at top
size() count of items
isEmpty() is count 0?

push(3)
push(4)
pop()
push(5)

ArrayStack<E>

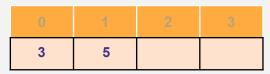
State

data[]
size

Behavior

push data[size] = value, if
out of room grow data
pop return data[size - 1],
size -= 1
peek return data[size - 1]
size return size

isEmpty return size == 0



size =

2

Big-Oh Analysis

pop() O(1) Constant

peek() O(1) Constant

size() O(1) Constant

isEmpty() O(1) Constant

push()

STACK ADT

State

Collection of ordered items Count of items

Behavior

push(index) add item to top
pop() return & remove item
at top
peek() return item at top
size() count of items
isEmpty() is count 0?

push(3)
push(4)
pop()
push(5)

ArrayStack<E>

State

data[]
size

Behavior

push data[size] = value, if
out of room grow data
pop return data[size - 1],
size -= 1

peek return data[size - 1]
size return size

<u>isEmpty</u> return size == 0

0	1	2	3
3	5		

size =

2

Big-Oh Analysis

pop() O(1) Constant

peek() O(1) Constant

size() O(1) Constant

isEmpty() O(1) Constant

push() What is your guess?

STACK ADT

State

Collection of ordered items Count of items

Behavior

push(index) add item to top
pop() return & remove item
at top
peek() return item at top
size() count of items
isEmpty() is count 0?

push(3) push(4) pop() push(5)

ArrayStack<E>

State

data[]
size

Behavior

push data[size] = value, if
out of room grow data
pop return data[size - 1],
size -= 1

peek return data[size - 1]
size return size

isEmpty return size == 0

0	1	2	3
3	5		

size =

2

Big-Oh Analysis

pop() O(1) Constant

peek() O(1) Constant

size() O(1) Constant

isEmpty() O(1) Constant

push() O(n) linear if you have to resize,

O(1) otherwise

