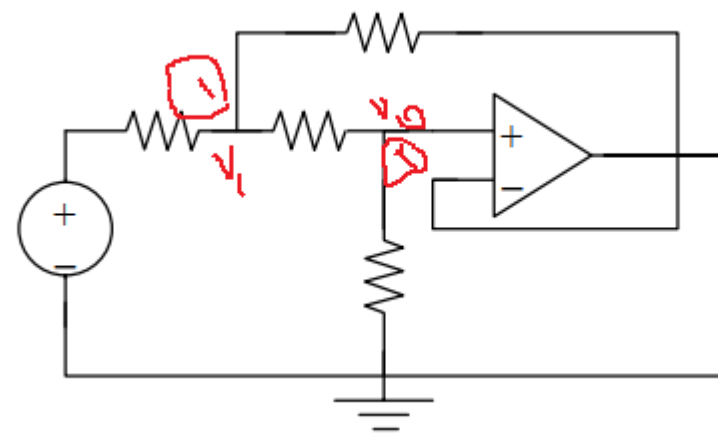
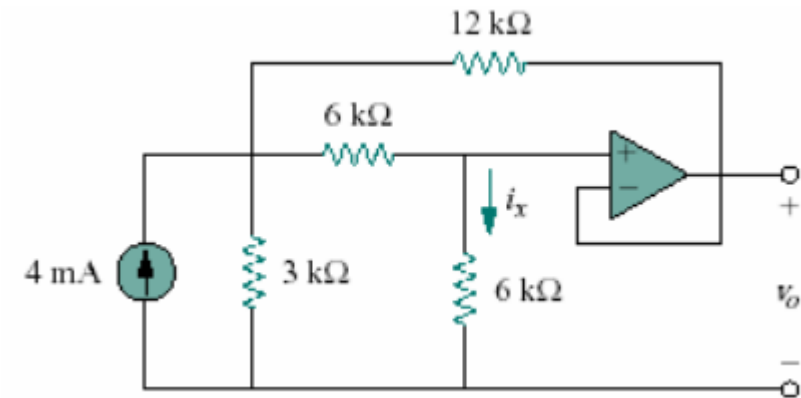


find i_x .



At node 1,

$$\frac{12 - v_1}{3} = \frac{v_1 - v_o}{6} + \frac{v_1 - v_o}{12} \longrightarrow 48 = 7v_1 - 3v_o \quad (1)$$

At node 2,

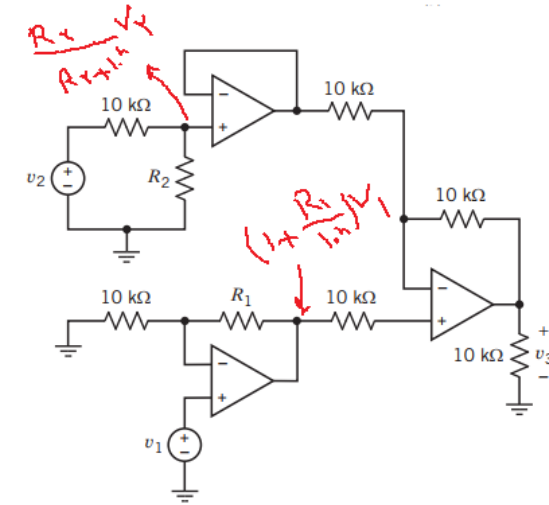
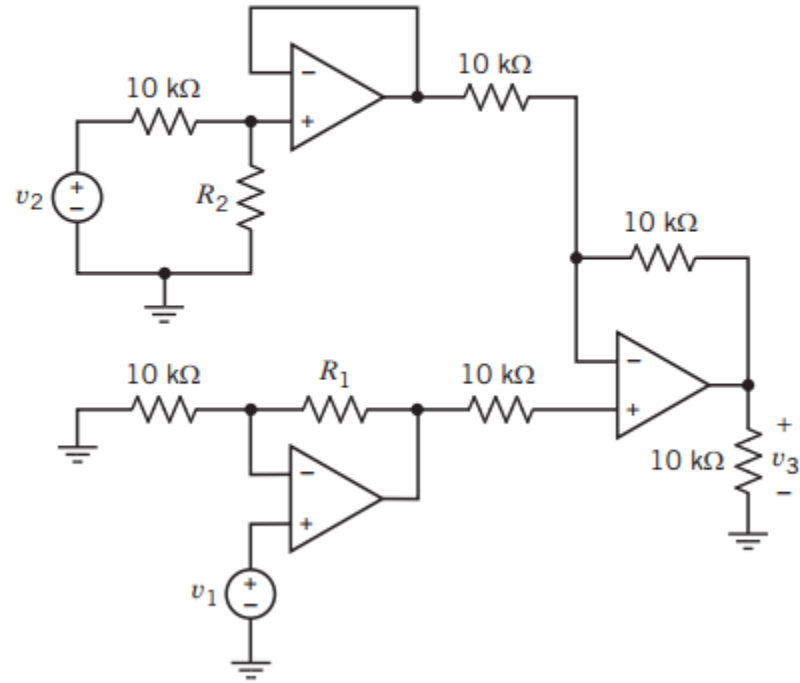
$$\frac{v_1 - v_o}{6} = \frac{v_o - 0}{6} = i_x \longrightarrow v_1 = 2v_o \quad (2)$$

From (1) and (2),

$$v_o = \frac{48}{11}$$

$$i_x = \frac{v_o}{6k} = \underline{\underline{727.2\mu A}}$$

Specify the values of R_1 and R_2 in Figure E 6.6-1 that are required to cause v_3 to be related to v_1 and v_2 by the equation $v_3 = (6)v_1 - (\frac{4}{3})v_2$.



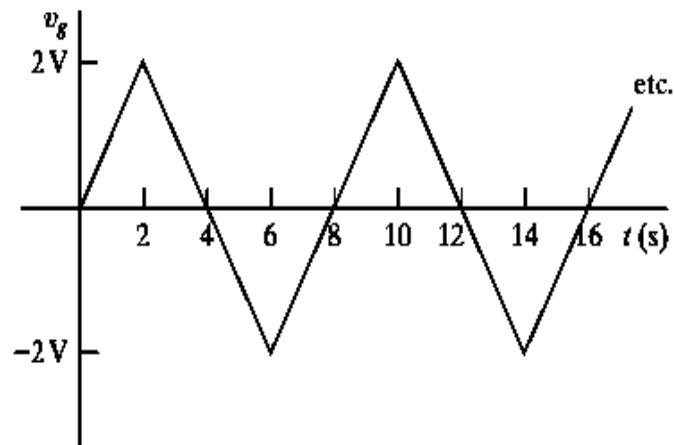
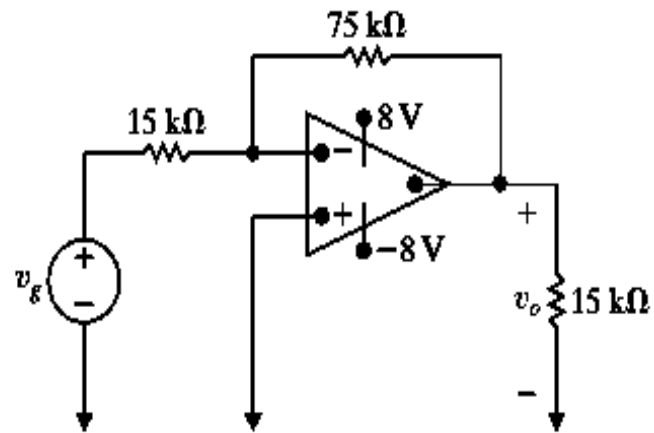
$$V_3 = + \left(1 + \frac{1}{10k} \right) \left(1 + \frac{R_1}{10k} \right) V_1 + \left(- \frac{1}{10k} \right) \frac{R_2}{R_2 + 10k} V_2$$

$$V_3 = \left(1 + \frac{R_1}{10k} \right) V_1 - \frac{R_2}{R_2 + 10k} V_2$$

$$R_1 = 50k$$

$$R_2 = 20k$$

ولتاژ ورودی در مدار شکل زیر نشان داده شده است، نمودار V_o بر حسب زمان را رسم کنید.



It follows directly from the circuit that $v_o = -(75/15)v_g = -5v_g$
From the plot of v_g we have $v_g = 0$, $t < 0$

$$v_g = t \quad 0 \leq t \leq 2$$

$$v_g = 4 - t \quad 2 \leq t \leq 6$$

$$v_g = t - 8 \quad 6 \leq t \leq 10$$

$$v_g = 12 - t \quad 10 \leq t \leq 14$$

$$v_g = t - 16 \quad 14 \leq t \leq 18, \text{ etc.}$$

Therefore

$$v_o = -5t \quad 0 \leq t \leq 2$$

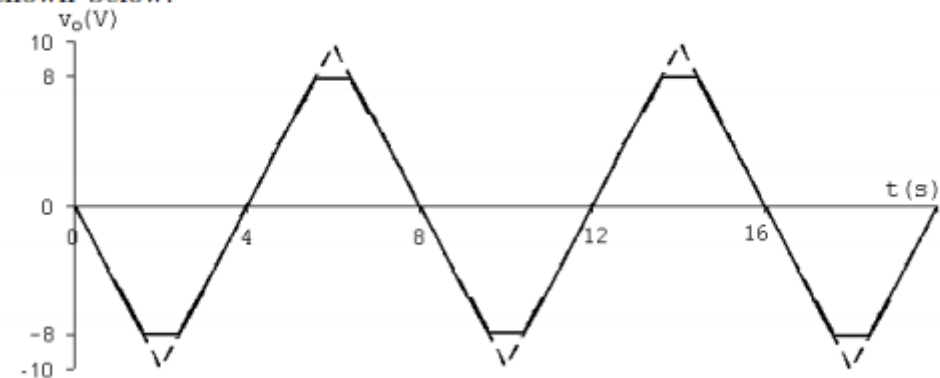
$$v_o = 5t - 20 \quad 2 \leq t \leq 6$$

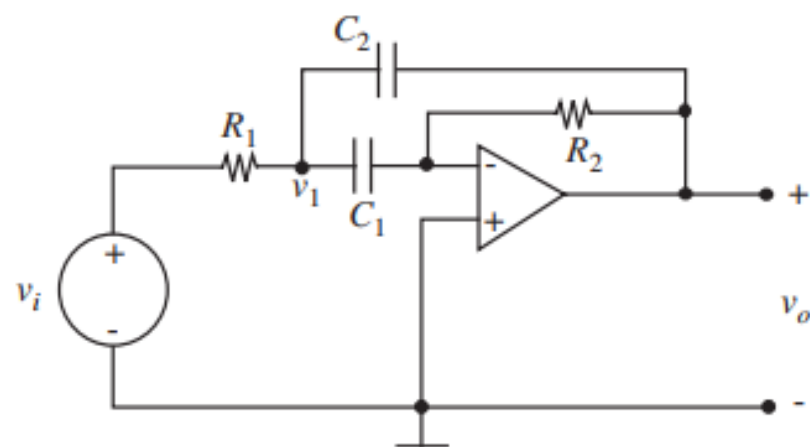
$$v_o = 40 - 5t \quad 6 \leq t \leq 10$$

$$v_o = 5t - 60 \quad 10 \leq t \leq 14$$

$$v_o = 80 - 5t \quad 14 \leq t \leq 18, \text{ etc.}$$

These expressions for v_o are valid as long as the op amp is not saturated. Since the peak values of v_o are ± 9 , the output is clipped at ± 9 . The plot is shown below.





For Node v_1 ,

$$(v_i - v_1)g_1 - C_1 \frac{dv_1}{dt} + C_2 \frac{d(v_o - v_1)}{dt} = 0$$

and for Node v^-

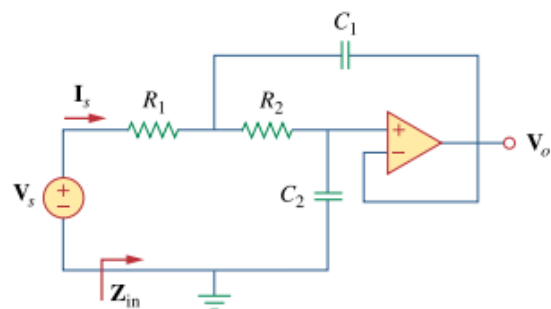
$$C_1 \frac{dv_1}{dt} + v_o g_2 = 0.$$

$$v_i g_1 = g_1 v_1 + (C_1 + C_2) \frac{dv_1}{dt} - C_2 \frac{dv_o}{dt}$$

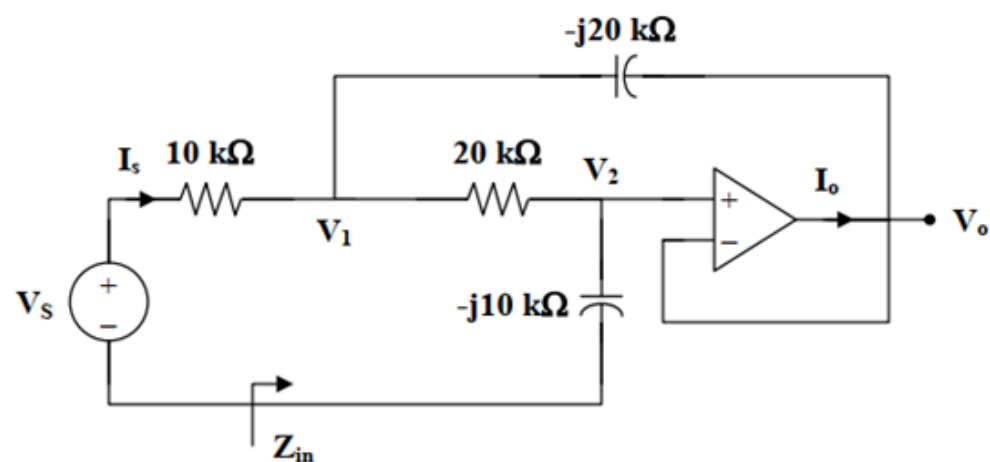
$$0 = C_1 \frac{dv_1}{dt} + v_o g_2.$$

$$\frac{d^2 v_o}{dt^2} + g_2 \frac{C_1 + C_2}{C_1 C_2} \frac{dv_o}{dt} + \frac{g_1 g_2}{C_1 C_2} v_o = -\frac{g_1}{C_2} \frac{dv_i}{dt}.$$

If the input impedance is defined as $Z_{in} = V_s / I_s$, find the input impedance of the op amp circuit in Fig. 10.116 when $R_1 = 10 \text{ k}\Omega$, $R_2 = 20 \text{ k}\Omega$, $C_1 = 10 \text{ nF}$, and $\omega = 5000 \text{ rad/s}$.



Consider the circuit in the frequency domain as shown below.



As a voltage follower, $V_2 = V_o$

$$C_1 = 10 \text{ nF} \longrightarrow \frac{1}{j\omega C_1} = \frac{1}{j(5 \times 10^3)(10 \times 10^{-9})} = -j20 \text{ k}\Omega$$

$$C_2 = 20 \text{ nF} \longrightarrow \frac{1}{j\omega C_2} = \frac{1}{j(5 \times 10^3)(20 \times 10^{-9})} = -j10 \text{ k}\Omega$$

At node 1,

$$\frac{V_s - V_1}{10} = \frac{V_1 - V_o}{-j20} + \frac{V_1 - V_o}{20}$$

$$2V_s = (3 + j)V_1 - (1 + j)V_o$$

(1)

At node 2,

$$\frac{V_1 - V_o}{20} = \frac{V_o - 0}{-j10}$$

$$V_1 = (1 + j2)V_o$$

(2)

Substituting (2) into (1) gives

$$2V_s = j6V_o \quad \text{or} \quad V_o = -j\frac{1}{3}V_s$$

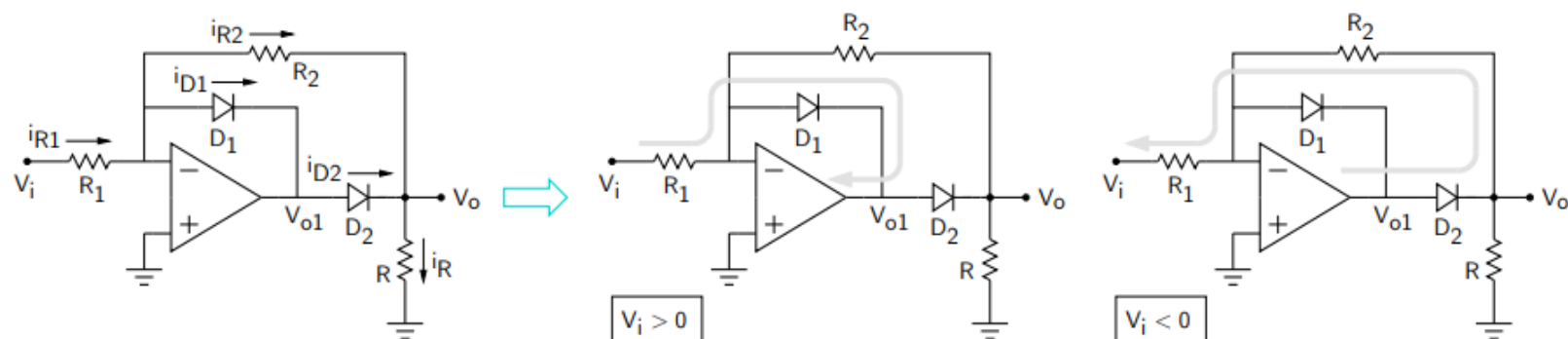
$$V_1 = (1 + j2)V_o = \left(\frac{2}{3} - j\frac{1}{3}\right)V_s$$

$$I_s = \frac{V_s - V_1}{10\text{k}} = \frac{(1/3)(1 + j)V_s}{10\text{k}}$$

$$\frac{I_s}{V_s} = \frac{1 + j}{30\text{k}}$$

$$Z_{in} = \frac{V_s}{I_s} = \frac{30\text{k}}{1 + j} = 15(1 - j)\text{k}$$

$$Z_{in} = \underline{\underline{21.21 \angle -45^\circ \text{ k}\Omega}}$$



(i) D_1 conducts: $V_- = V_+ = 0 \text{ V}$, $V_{o1} = -V_{D1} \approx -0.7 \text{ V}$.

D_2 cannot conduct (show that, if it did, KCL is not satisfied at V_o).

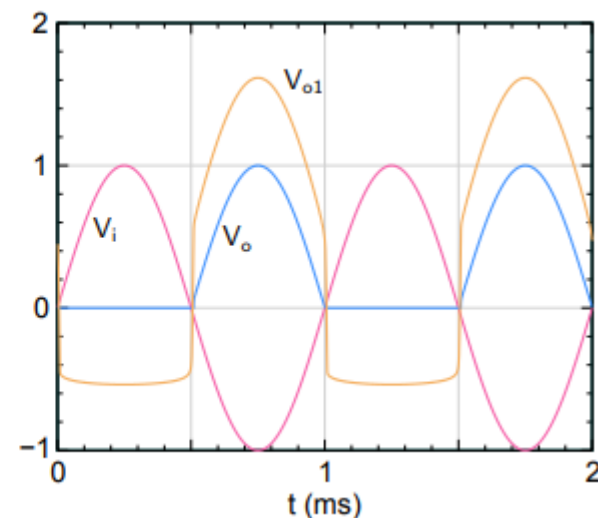
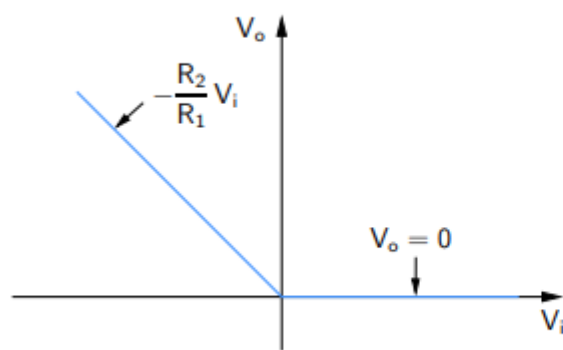
$\rightarrow i_{R2} = 0$, $V_o = V_- = 0 \text{ V}$.

$i_{R1} = i_{D1}$ which can only be positive $\Rightarrow V_i > 0 \text{ V}$.

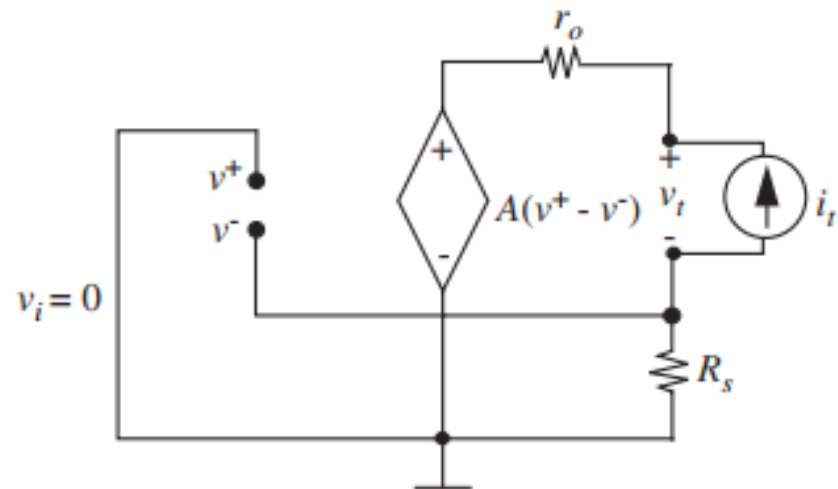
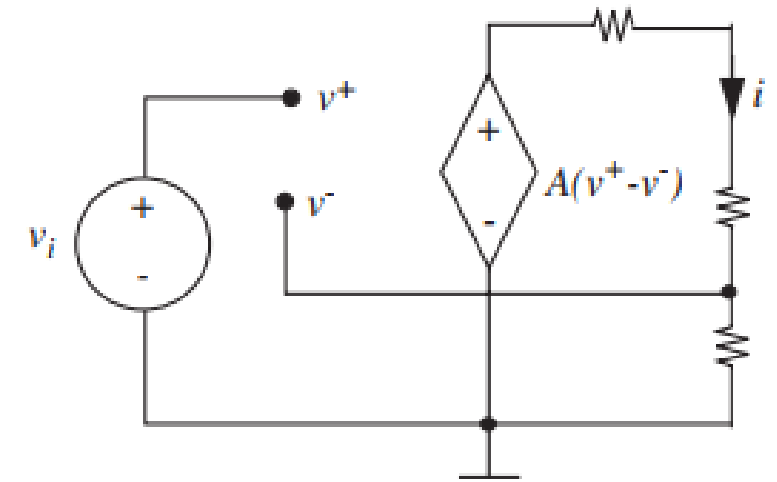
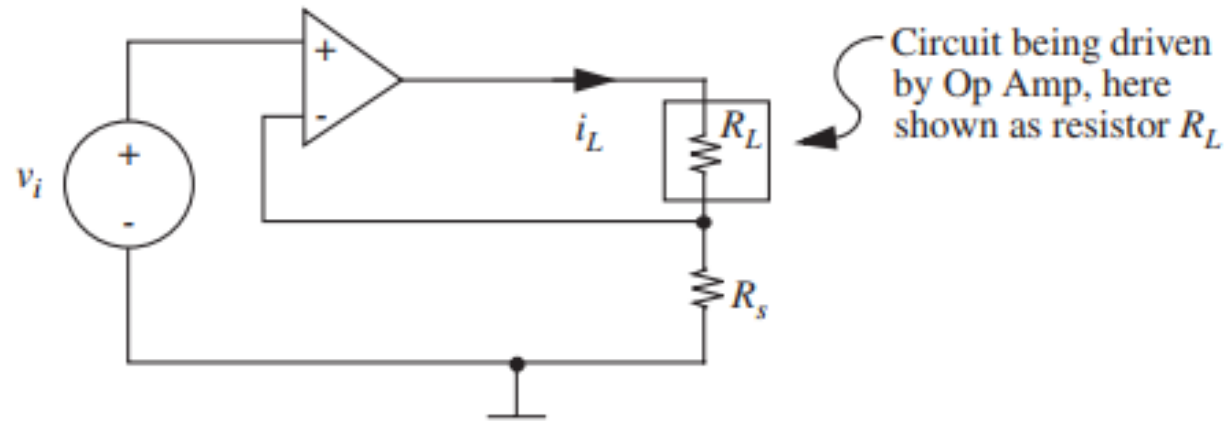
(ii) D_1 is off; this will happen when $V_i < 0 \text{ V}$.

In this case, D_2 conducts and closes the feedback loop through R_2 .

$$V_o = V_- + i_{R2}R_2 = 0 + \left(\frac{0 - V_i}{R_1} \right) R_2 = -\frac{R_2}{R_1} V_i.$$



مقاومت معادل از دید R_L (آپ-امپ غیرایده‌آل)



$$v^- = -i_t R_s$$

$$v^+ = 0$$

$$v_t = A(v^+ - v^-) + i_t r_o - v^-$$

$$= (1 + A)i_t R_s + i_t r_o$$

$$R_o = \frac{v_t}{i_t} = (1 + A)R_s + r_o.$$