NCERT 11.9.2 Q7

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Question: Find the sum of n terms of the A.P. whose kth term is $5k + 1$.

Symbol	Value	Parameter
$x(0)$	1	First Term
$x(n)$	$(5n+1)u(n)$	kth Term
d	5	Common Difference
$y(n)$	?	Sum of N terms

TABLE 0
GIVEN PARAMETERS

Expression	Z-Transform	ROC
$nu[n]$	$\frac{z^{-1}}{(1-z^{-1})^2}$	$\|z\| > 1$
$n(n-1)u[n]$	$\frac{2z^{-1}}{(1-z^{-1})^3}$	$\|z\| > 1$

TABLE 0
Z TRANSFORM PAIRS

Apply the Z-transform to $x(n)$:

$$X(z) = \frac{5z^{-1}}{(1-z^{-1})^2} + \frac{1}{(1-z^{-1})} \quad |z| > 1 \tag{1}$$

Sum of First n Terms:

$$y(n) = x(n) * u(n) \tag{2}$$

Applying Z transform on both sides:

$$Y(z) = X(z)U(z) \tag{3}$$

$$= \frac{1}{(1-z^{-1})^2} + \frac{5z^{-1}}{(1-z^{-1})^3} \tag{4}$$

Rewriting the expression:

$$= \frac{1}{(1-z^{-1})^2} + \frac{5}{2} \cdot \frac{2z^{-1}}{(1-z^{-1})^3} \tag{5}$$

On referring the above table we can obtain the Z trnasform inverse as follows:

$$y[n] = nu[n] + \frac{5}{2}n(n-1)u[n] \tag{6}$$

Therefore we have got the sun of n terms as:

$$y[n] = [n + \frac{5}{2}n(n-1)]u[n] \tag{7}$$

The stem plot is given as