

1)

```
def sum_lst(lst):
```

```
    if len(lst) == 1:
        return lst[0];
```

$\theta(n)$

```
    else
```

```
        rest = sum_lst(lst[1:])
```

```
        sum = lst[0] + rest
```

```
        return sum
```



-----

$n \quad \theta(k)$

$\downarrow$   
 $n-1 \quad \theta(k)$

$\downarrow$   
 $n-2 \quad \theta(k)$

$\downarrow$   
 $n-3 \quad \theta(k)$

$\vdots$

$n-(n) \quad \theta(k)$



$k = \text{slice size}$

$n$  levels of  $\theta(n)$

Time Complexity:

$\theta(n^2)$

```
def sum1st2(lst, low, high):
```

```
    if (low == high):  
        return lst[low]
```

```
    else:
```

$\theta(1)$



```
        rest = sum1st2(lst, low+1, high);
```

```
        sum = lst[low] + rest
```

```
        return sum
```

---

n	$\theta(1)$
---	-------------

1	$\theta(1)$
n-1	$\theta(1)$

1	$\theta(1)$
n-2	$\theta(1)$

$\vdots$	
n-(n)	$\theta(1)$

Also n levels  
of  $\theta(1)$  each

Time Complexity

$\theta(n)$

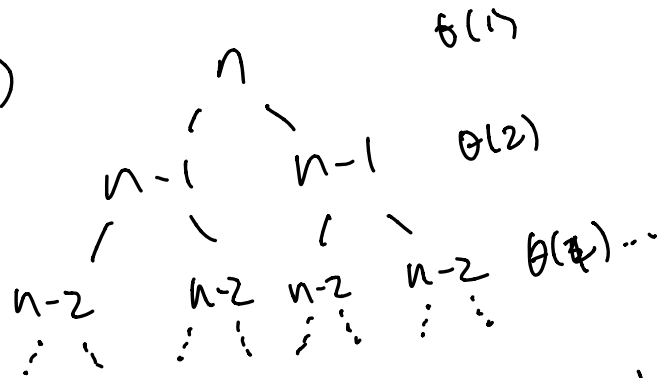
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Implementation 2

is faster.

2)

a)



$n$  levels of constant time

$$\Rightarrow \Theta(n)$$

b)



$\log_2(n)$  levels of constant time

$$\Rightarrow \Theta(\log(n))$$

c)

$n$	$\theta(n)$
$1$	
$n/2$	$\theta(k)$
$1$	
$n/4$	$\theta(k)$
$1$	
$n/8$	$\theta(k)$

$\log_2(n)$  levels of

$$\theta(k): n + n/2 + n/4 + \dots$$

$$\Rightarrow \theta(n \log(n))$$