

Experiment – 1.4

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Semester: 5th

Date: 09-09-25

Subject Name: ADBMS

Subject Code: 23CSP-333

Aim: To analyze given relations with functional dependencies, determine candidate keys, classify prime and non-prime attributes, remove redundant dependencies, and identify the highest normal form of the relation schemas.

Objective: The objective of this work is to analyze functional dependencies in given relations to determine candidate keys and classify attributes as prime or non-prime. It also focuses on minimizing functional dependencies by removing redundancy and evaluating the highest normal form achieved by each relation.

Q1:

For relation $R(A,B,C,D)$ with FDs $\{AB \rightarrow C, C \rightarrow D, D \rightarrow A\}$, find candidate keys, prime and non-prime attributes. Also state the highest normal form.

Dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A$

Solution:

- Candidate Keys: **AB, BC, BD**
- Prime Attributes: **A, B, C, D**
- Non-Prime Attributes: \emptyset

Explanation:

$AB^+ = \{A,B,C,D\}$, $BC^+ = \{B,C,D,A\}$, $BD^+ = \{B,D,A,C\}$. All attributes are prime.

Highest Normal Form = **3NF** ($C \rightarrow D$ violates BCNF but is allowed in 3NF since D is prime).

Q2:

For relation $R(A,B,C,D,E)$ with FDs $\{A \rightarrow D, B \rightarrow A, BC \rightarrow D, AC \rightarrow BE\}$, find candidate keys, prime and non-prime attributes. Also state the highest normal form.

Dependencies: $A \rightarrow D, B \rightarrow A, BC \rightarrow D, AC \rightarrow BE$

Solution:

- Candidate Keys: **AC, BC**
- Prime Attributes: **A, B, C**
- Non-Prime Attributes: **D, E**

Explanation:

$AC^+ = \{A,B,C,D,E\}$, $BC^+ = \{B,C,A,D,E\}$. Both are keys. Non-primes $\{D,E\}$ depend only on part of key (A), so violates 2NF.

Highest Normal Form = **1NF**.

Q3:

For relation $R(A,B,C,D,E)$ with FDs $\{B \rightarrow A, A \rightarrow C, BC \rightarrow D, AC \rightarrow BE\}$, find candidate keys, prime and non-prime attributes. Also state the highest normal form.

Dependencies: $B \rightarrow A, A \rightarrow C, BC \rightarrow D, AC \rightarrow BE$

Solution:

- Candidate Keys: **A, B**
- Prime Attributes: **A, B**
- Non-Prime Attributes: **C, D, E**

Explanation:

$A^+ = \{A,C,B,E,D\}$, $B^+ = \{B,A,C,D,E\}$. Both generate full set. Since all LHS are keys, no violations.

Highest Normal Form = **BCNF**.

Q4:

For relation $R(A,B,C,D,E,F)$ with FDs $\{A \rightarrow BCD, BC \rightarrow DE, B \rightarrow D, D \rightarrow A\}$, find candidate keys, prime and non-prime attributes. Also state the highest normal form.

Dependencies: $A \rightarrow BCD, BC \rightarrow DE, B \rightarrow D, D \rightarrow A$

Solution:

- Candidate Keys: **AF, BF, DF**
- Prime Attributes: **A, B, D, F**
- Non-Prime Attributes: **C, E**

Explanation:

$A^+ = \{A,B,C,D,E\}$, missing $F \rightarrow AF$ is key. Similarly BF and DF . Partial dependencies ($A \rightarrow C, E$) mean it fails 2NF.

Highest Normal Form = **1NF**.

Q5:

For relation $R(W,X,Y,Z)$ with FDs $\{X \rightarrow Y, WZ \rightarrow X, WZ \rightarrow Y, Y \rightarrow W, Y \rightarrow X, Y \rightarrow Z\}$, find candidate keys, prime and non-prime attributes, minimal cover, and highest normal form.

Dependencies: $X \rightarrow Y, WZ \rightarrow X, WZ \rightarrow Y, Y \rightarrow W, Y \rightarrow X, Y \rightarrow Z$

Solution:

- Minimal Cover: **$\{X \rightarrow Y, WZ \rightarrow X, Y \rightarrow W, Y \rightarrow Z\}$**
- Candidate Keys: **X, Y, WZ**
- Prime Attributes: **W, X, Y, Z**
- Non-Prime Attributes: **\emptyset**
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Explanation:

$Y^+ = \{Y,W,X,Z\}$, $X^+ = \{X,Y,W,Z\}$, $WZ^+ = \{W,Z,X,Y\}$. All attributes are prime.

Highest Normal Form = **BCNF** (all FDs have LHS as key).

Q6:

For relation $R_1(A,B,C,D,E,F)$ with FDs $\{A \rightarrow BC, A \rightarrow D, BC \rightarrow D, D \rightarrow E\}$, find candidate keys, prime and non-prime attributes. Also state the highest normal form.

Dependencies: $A \rightarrow BC$, $A \rightarrow D$, $BC \rightarrow D$, $D \rightarrow E$

Solution:

- Candidate Key: **AF**
- Prime Attributes: **A, F**
- Non-Prime Attributes: **B, C, D, E**

Explanation:

$A^+ = \{A, B, C, D, E\}$, missing $F \rightarrow AF$ is key. Non-primes depend only on part of key, violating 2NF.

Highest Normal Form = **1NF**.

Learning Outcomes

After completing these questions, students will be able to:

1. Apply closure method to find candidate keys.
2. Differentiate prime and non-prime attributes in a relation.
3. Detect and eliminate redundant functional dependencies.
4. Identify the highest normal form of a given relation schema.
5. Improve conceptual clarity of normalization for efficient database design.