PROBLEM SET 2

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1. Let $\Sigma = \{a, b, c\}$ and $L = \{a^i b^j c^k \mid i, j, k \ge 0 \text{ and if } i = 1, \text{ then } j = k\}$. Show that L is not regular using the pumping lemma.

Hint: You must show both cases where when w = xyz that $x = \lambda$ and where x is composed of some characters.

- 2. Let $\Sigma = \{0, 1, +, =\}$ and $ADD = \{u + v = w \mid u, v, w \in \{0, 1\}^* \text{ and } u + v = w \text{ is a valid addition operation}\}$. Show that ADD is not regular using the pumping lemma.
- 3. For each of the following grammars, determine if they are ambiguous or unambiguous. If they are ambiguous, prove that by giving two parse trees for one same string.

a)
$$S \to XY \mid W$$

 $X \to aXb \mid \lambda$

$$Y \to cY \mid \lambda$$

$$W \rightarrow aWc \mid Z$$

$$Z \to bZ \mid \lambda$$

b)
$$S \to XX$$

$$X \to aXb$$

$$Y \to cY \mid \lambda$$

c)
$$S \to aXY \mid bYX \mid \lambda$$

$$Z \rightarrow aZ \mid a$$

$$X \to aXY \mid a\lambda$$

$$Y \to bYZ \mid b \mid \lambda$$

4. Construct a CFG for the following language over $\Sigma = \{ a, b \}$:

$$L = \{ x_1 \# x_2 \# ... \# x_k \mid k \ge 1, \text{ each } x_i \in \Sigma^* \text{ and for some } i \text{ and } j, x_i = x_j^R \}$$