

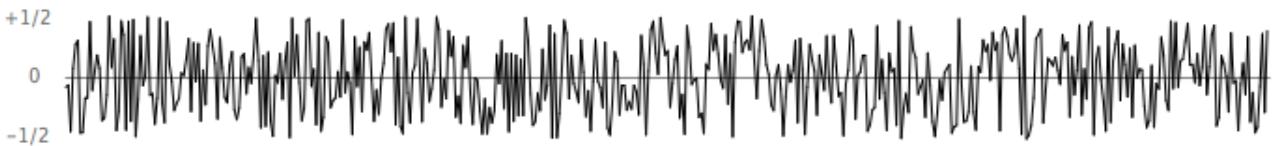
This document only contains the project problems. For the programming exercises on concepts needed for the project, please refer to the project checklist [↗](#).

The purpose of this project is to write a program to simulate the plucking of a guitar string using the *Karplus-Strong* algorithm. This algorithm played a seminal role in the emergence of physically modeled sound synthesis, where a physical description of a musical instrument is used to synthesize sound electronically.

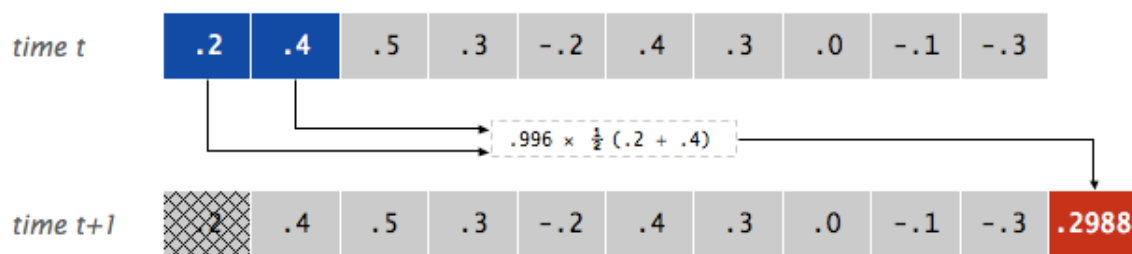
Simulate the Plucking of a Guitar String When a guitar string is plucked, the string vibrates and creates sound. The length of the string determines its *fundamental frequency* of vibration. We model a guitar string by sampling its displacement (a real number between $-1/2$ and $+1/2$) at N equally spaced points in time. The integer N equals the *sampling rate* (44,100 Hz) divided by the desired fundamental frequency, rounded **up** to the next integer.



- *Plucking a String* The excitation of the string can contain energy at any frequency. We simulate the excitation with white noise: set each of the N displacements to a random real number between $-1/2$ and $+1/2$.



- *The Resulting Vibrations* After the string is plucked, the string vibrates. The pluck causes a displacement that spreads wave-like over time. The Karplus-Strong algorithm simulates this vibration by maintaining a ring buffer of the N samples: the algorithm repeatedly deletes the first sample from the buffer and adds to the end of the buffer the average of the deleted sample and the first sample, scaled by an energy decay factor of 0.996. For example:



The Karplus-Strong update

Why it Works? The two primary components that make the Karplus-Strong algorithm work are the ring buffer feedback mechanism and the averaging operation.

- *The Ring Buffer Feedback Mechanism* The ring buffer models the medium (a string tied down at both ends) in which the energy travels back and forth. The length of the ring buffer determines the fundamental frequency of the resulting sound. Sonically, the feedback mechanism reinforces only the fundamental frequency and its harmonics (frequencies at integer multiples of the fundamental). The energy decay factor (.996 in this case) models the slight dissipation in energy as the wave makes a round trip through the string.

function	description
<code>create(frequency)</code>	create and return a guitar string of the given frequency, using a sampling rate given by SPS, a constant in <code>guitar_string.py</code>
<code>create_from_samples(init)</code>	create and return a guitar string whose size and initial values are given by the list <i>init</i>
<code>pluck(string)</code>	pluck the given guitar string by replacing the buffer with white noise
<code>tic(string)</code>	advance the simulation one time step on the given guitar string by applying the Karplus-Strong update
<code>sample(string)</code>	current sample from the given guitar string

Some details about the functions:

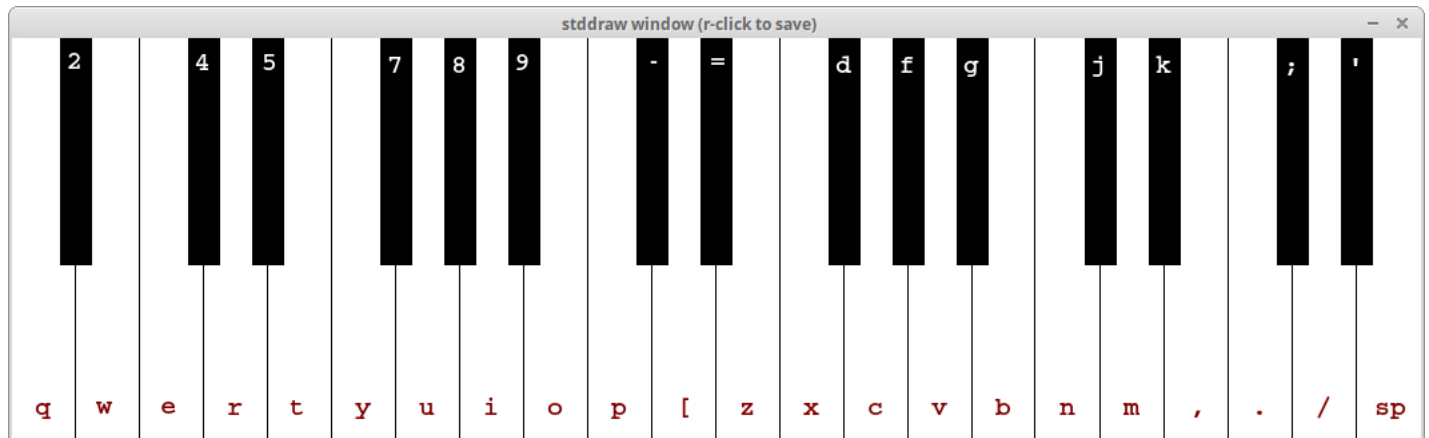
- `create(frequency)` creates and returns a ring buffer of capacity N (sampling rate 44,100 divided by `frequency`, rounded **up** to the nearest integer), and initializes it to represent a guitar string at rest by enqueueing N zeros. A guitar string is represented as a ring buffer of capacity N , with all values initialized to 0.0
- `create_from_samples(init)` creates and returns a ring buffer of capacity equal to the size of the given list `init`, and initializes the contents of the buffer to the values in the list. In this assignment, this function's main purpose is for debugging and grading.
- `pluck(string)` replaces the N items in the ring buffer `string` with N random values between -0.5 and 0.5.
- `tic(string)` applies the Karplus-Strong update: deletes the sample at the front of the ring buffer `string` and adds to the end of the ring buffer the average of the first two samples, multiplied by the energy decay factor.
- `sample(string)` returns the value of the item at the front of the ring buffer `string`.

```
$ python3 guitar_string.py 25
0    0.2000
1    0.4000
2    0.5000
3    0.3000
4   -0.2000
5    0.4000
6    0.3000
7    0.0000
8   -0.1000
9   -0.3000
10   0.2988
11   0.4482
12   0.3984
13   0.0498
14   0.0996
15   0.3486
16   0.1494
17  -0.0498
18  -0.1992
19  -0.0006
20   0.3720
21   0.4216
22   0.2232
23   0.0744
24   0.2232
```

Let's Rock The program `guitar_sound_synthesis.py` is a visual client that uses your `guitar_string.py` (and `ring_buffer.py`) modules to play a guitar in real-time, using the keyboard to input notes. When the user types the appropriate characters, the program plucks the corresponding string. Since the combined result of several sound waves is the superposition of the individual sound waves, the program plays the sum of all string samples.

The keyboard arrangement imitates a piano keyboard: the “white keys” are on the `qwerty` and `zxcv` rows and the “black keys” on the `12345` and `asdf` rows of the keyboard.

```
$ python3 guitar_sound_synthesis.py
```



Acknowledgements This project is an adaptation of the Guitar assignment developed at Princeton University by Andrew Appel, Jeff Bernstein, Maia Ginsburg, Ken Steiglitz, Ge Wang, and Kevin Wayne.