#### 1

# Assignment-1

EE:1205 (SignalsSystems)
Indian Institute of Technology, Hyderabad

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### Question 10.5.3.12:

Find the sum of the first 40 positive integers divisible by 6.

#### Solution:

Parameter	Description	Value
x(0)	First Term	6
d	Common Difference	6

TABLE 0 Parameter Table

$$x(n) = (6 + 6n)(u(n))$$
 (1)

$$\implies X(z) = \frac{6}{1 - z^{-1}} + \frac{6z^{-1}}{(1 - z^{-1})^2} \quad (??) \quad (2)$$

$$\implies X(z) = \frac{6}{(1 - z^{-1})^2}, \quad |z| > 1 \tag{3}$$

$$y(n) = x(n) * u(n)$$
 (4)

$$\implies Y(z) = X(z) U(z) \tag{5}$$

$$= \frac{6}{(1 - z^{-1})^3}, \quad |z| > 1 \tag{6}$$

Using contour integration to find the inverse Z-transform:

$$\implies y(39) = \frac{1}{2\pi i} \oint_C Y(z) \ z^{38} \ dz \tag{7}$$
$$= \frac{1}{2\pi i} \oint_C \frac{6z^{41}}{(z-1)^3} \ dz \tag{8}$$

We can observe that there is only a three times repeated pole at z=1,

$$\implies R = \frac{1}{(m-1)!} \lim_{z \to a} \frac{d^{m-1}}{dz^{m-1}} \left( (z-a)^m f(z) \right) \tag{9}$$

$$= \frac{1}{(2)!} \lim_{z \to 1} \frac{d^2}{dz^2} \left( (z - 1)^3 \frac{6z^{41}}{(z - 1)^3} \right) \tag{10}$$

$$= 3 \lim_{z \to 1} \frac{d^2}{dz^2} \left( z^{41} \right) \tag{11}$$

$$=4920$$
 (12)

$$\therefore y(39) = 4920 \tag{13}$$

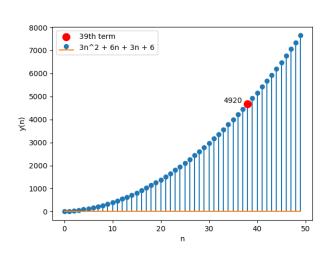


Fig. 0. Plot of y(n) vs n