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Assignment-1

EE:1205 (SignalsSystems)
Indian Institute of Technology, Hyderabad

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Question 10.5.3.12:

Find the sum of the first 40 positive integers divisible by 6.

Solution:

Parameter	Description	Value
x(0)	First Term	6
d	Common Difference	6

TABLE 0 Parameter Table

We can observe that there only a repeated pole at z=1.

$$\implies R = \frac{1}{(m-1)!} \lim_{z \to a} \frac{d^{m-1}}{dz^{m-1}} \left((z-a)^m f(z) \right) \quad (11)$$

$$= \frac{1}{(2)!} \lim_{z \to 1} \frac{d^2}{dz^2} \left((z - 1)^3 \frac{6z^{41}}{(z - 1)^3} \right) \tag{12}$$

$$= 3\lim_{z \to 1} \frac{d^2}{dz^2} \left(z^{41} \right) \tag{13}$$

$$=4920$$
 (14)

$$\therefore y(39) = 4920 \tag{15}$$

$$x(n) = (6 + 6n) u(n)$$
 (1)

$$\implies X(z) = \frac{x(0)}{(1-z^{-1})} + \frac{dz^{-1}}{(1-z^{-1})^2}$$
 (2)

$$=\frac{6}{1-z^{-1}}+\frac{6z^{-1}}{\left(1-z^{-1}\right)^2}\tag{3}$$

$$\implies X(z) = \frac{6}{(1 - z^{-1})^2}, |z| > 1 \tag{4}$$

$$y(n) = x(n) * u(n)$$
 (5)

$$\implies Y(z) = X(z) U(z) \tag{6}$$

$$=\frac{6}{(1-z^{-1})^2}\frac{1}{(1-z^{-1})}\tag{7}$$

$$=\frac{6}{(1-z^{-1})^3}, |z| > 1$$
 (8)

(5) (6) (7) (8)

Stem Plot of x(n) vs n

Fig. 0. Plot of x(n) vs n

Using contour integration to find the inverse Z-transform:

$$\implies y(39) = \frac{1}{2\pi j} \oint_C Y(z) \ z^{38} \ dz \tag{9}$$

$$= \frac{1}{2\pi j} \oint_C \frac{6z^{38}}{(1-z^{-1})^3} dz \qquad (10)$$