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GATE MA-28(2022)

EE:1205-Signals and Systems Indian Institute of Technology, Hyderabad

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Question

The radius of convergence of the series

$$\sum_{n=0}^{\infty} 3^{n+1} z^{2n}, \quad z \in \mathbb{C}$$

is?

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Solution:

Parameter	Description	Value
X(z)	Given Sum	$\sum_{n=0}^{\infty} 3^{n+1} z^{2n}, z \in \mathbb{C}$
x(n)	Inverse Z transform of $X(z)$?

TABLE 1: GATE MA-28(2022)

On comparing X(z) with Z-transform formula

$$x(n) = \begin{cases} 0 & \text{, odd } n \\ 3^{\frac{n+1}{2}} & \text{, even } n \end{cases}$$
 (1)

Now,

$$X(z) = 3 \sum_{n=0}^{\infty} 3^n z^{2n}, \quad z \in \mathbb{C}$$

$$= 3 \sum_{n=0}^{\infty} (3z^2)^n$$
(3)

$$=3\sum_{n=0}^{\infty} (3z^2)^n \tag{3}$$

For Radius of Convergence,

$$|3z^2| < 1 \tag{4}$$

$$|z| < \frac{1}{\sqrt{3}} \tag{5}$$

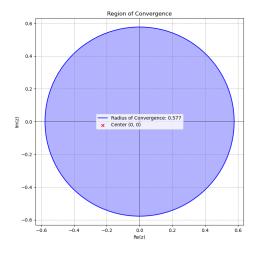


Fig. 1: ROC - $|z| < \frac{1}{\sqrt{3}}$