

Look-ahead Filter

Hypothesis:

look-ahead filter:

Let a be the number a frames to look ahead, the hypothesis:

$$v(k+a) = v(k-1) \cdot v\Delta(k)^{a+1}$$

and $v\Delta(k)$ can be updated:

$$v\Delta(k) = \text{slerp}(v\Delta(k+a), v\Delta(k), \gamma)$$

forward filter

$$v\Delta(k) = \text{slerp}(p\Delta(k), v\Delta(k-1), \alpha)$$

Data Structure

the data structure have to fit both forward filter and look-ahead filter, as look-ahead number $a=0$, which means forward filter.

there are queues in the filter to buffer history data:

- **p_cam_orien queue**
physical camera orientation buffer, include knee points orientation of each frame.
- **v_cam_orien queue**
virtual camera orientation buffer
- **v Δ queue**
virtual camera velocity buffer
- **frame queue**
frame buffer

Queue	0	1	2	3	4
p_cam_orien_buffer					
v_cam_orien_buffer					
v_cam_velocity_buffer					
frame_buffer					

Queue Handler

let set $a = 5$, so each queue size would be 5

Initialization:

```
# initialize buffer
v_cam_orien_buffer = deque(maxlen=a)
p_cam_orien_buffer = deque(maxlen=a)
v_cam_velocity_buffer = deque(maxlen=a)
frame_buffer = deque(deque(maxlen=a))
# initialize camera orientation and velocity
prev_v_cam_orien = Quaternion()
prev_p_cam_orien = Quaternion()
prev_v_cam_velocity = Quaternion()
```

- **i = 0**

$$p[0] = \text{intergrate}(p_{prev}, \omega[0], \Delta t)$$

$$p\Delta[0] = p[0] \cdot p_{prev}^*$$

$$v\Delta[0] = \text{slerp}(p\Delta[0], v\Delta_{prev}, \alpha)$$

$$v[0] = v_{prev} \cdot v\Delta[0]$$

push to buffer:

$$frame[0], v[0], v\Delta[0]$$

$$p_{prev} = p[0]$$

$$v_{prev} = v[0]$$

$$v\Delta_{prev} = v\Delta[0]$$

Queue	0	1	2	3	4
p_cam_orien_buffer	$p[0]$				
v_cam_orien_buffer	$v[0]$				
v_cam_velocity_buffer	$v\Delta[0]$				
frame_buffer	frame[0]				

- i = 1

- i = 2

- i = 3

...

- **i = 4**

$$p[4] = \text{intergrate}(p_{prev}, \omega[4], \Delta t)$$

$$p\Delta[4] = p[4] \cdot p_{prev}^*$$

$$v\Delta[4] = \text{slerp}(p\Delta[4], v\Delta_{prev}, \alpha)$$

$$v[4] = v_{prev} \cdot v\Delta[4]$$

push to buffer:

$$frame[4], v[4], v\Delta[4]$$

$$p_{prev} = p[4]$$

$$v_{prev} = v[4]$$

$$v\Delta_{prev} = v\Delta[4]$$

Queue	0	1	2	3	4
p_cam_orien_buffer	$p[0]$	$p[1]$	$p[2]$	$p[3]$	$p[4]$
v_cam_orien_buffer	$v[0]$	$v[1]$	$v[2]$	$v[3]$	$v[4]$
v_cam_velocity_buffer	$v\Delta[0]$	$v\Delta[1]$	$v\Delta[2]$	$v\Delta[3]$	$v\Delta[4]$
frame_buffer	frame[0]	frame[1]	frame[2]	frame[3]	frame[4]

- **i = 5**

$$p[5] = \text{intergrate}(p_{prev}, \omega[5], \Delta t)$$

$$p\Delta[5] = p[5] \cdot p_{prev}^*$$

$$v\Delta[5] = \text{slerp}(p\Delta[5], v\Delta_{prev}, \alpha)$$

$$v[5] = v_{prev} \cdot v\Delta[5]$$

if (queue.size() >= a)

{

$$v\Delta[0] = \text{slerp}(v\Delta[0], v\Delta[5], \gamma)$$

$$v[1] = v[0] \cdot v\Delta[0]$$

$$\text{trans_matrices}[1] = \text{cal_trans_matrices}(v[1], p[1])$$

}

push to buffer:

$$\text{frame}[5], v[5], v\Delta[5]$$

$$p_{prev} = p[5]$$

$$v_{prev} = v[5]$$

$$v\Delta_{prev} = v\Delta[5]$$

Queue	0	1	2	3	4
p_cam_orien_buffer	p[1]	p [2]	p [3]	p [4]	p [5]
v_cam_orien_buffer	v[1]	v [2]	v[3]	v[4]	v[5]
v_cam_velocity_buffer	$v\Delta[1]$	$v\Delta[2]$	$v\Delta[3]$	$v\Delta[4]$	$v\Delta[5]$
frame_buffer	frame[1]	frame[2]	frame[3]	frame[4]	frame[5]

Pseudo code:

```
# integrate physycal camera orientation
p_cam_orien = integrate_p_cam_orien(prev_p_cam_orien, angular_veclooty, timestamp)
# calculate physical camera velocity
p_cam_velocity = p_cam_orien*prev_p_cam_orien.conjugate
# virtual camera velocity calculation in foward direction
current_v_cam_velocity= slerp(p_cam_velocity, prev_v_cam_velocity, alpha)
```

```

# virtual camera velocity calculation in look-ahead direction
if len(v_cam_velocity_buffer) >= a:

    foward_v_cam_velocity = v_cam_velocity_buffer[0]
    foward_v_cam_velocity =
    slerp(current_v_cam_velocity, foward_v_cam_velocity, gamma)

    # virtual camera orientation integration
    v_cam_orien_buffer[1] = v_cam_orien_buffer[0] * forward_v_cam_velocity
    trans_matrices =
    cal_trans_matrices(v_cam_orien_buffer[1], p_cam_orien_buffer[1])

# push orientation and velocity to buffer
p_cam_orien_buffer.push_back(p_cam_orien)
v_cam_orien_buffer.push_back(v_cam_orien)
v_cam_velocity_buffer.push_back(current_v_cam_velocity)

# store current to previous orientation and velocity
prev_v_cam_orien = v_cam_orien
prev_p_cam_orien = p_cam_orien
prev_v_cam_velocity = current_v_cam_velocity

```