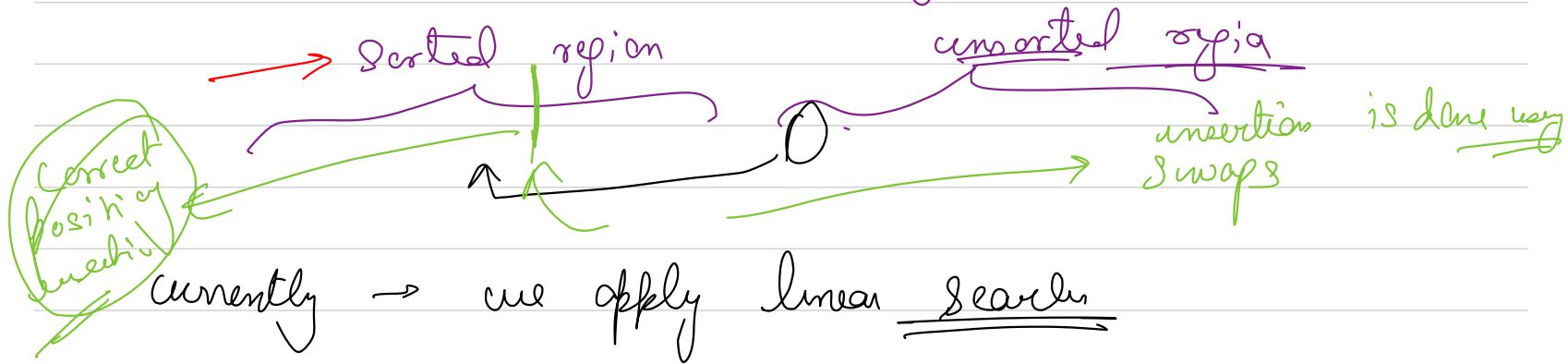


⇒ Insertion sort → from the unsorted region, pick any element & search for its best position in the sorted region & insert.



↳ optimize it by binary search ??

a)  $n$

b)  $n \log n$

c)  $n^2$

d)  $n^2 \log n$



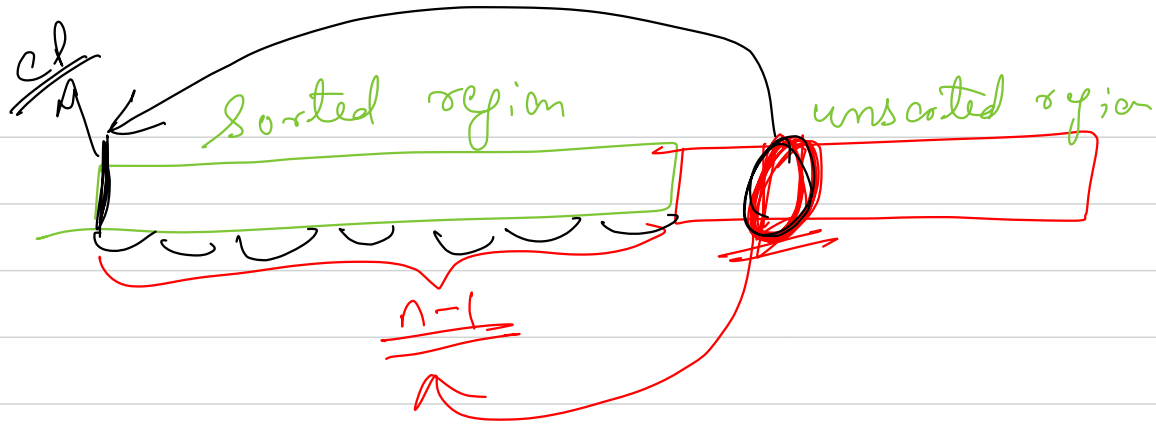
$O(n^2)$



$O(\underline{n}(\log n + n))$

$O(\underline{n \log n} + \underline{n^2})$

$O(n^2)$



$$\underline{O(n(\log n + n))} \approx \underline{O(n^2)}$$

search the  
correct

pos

actually insert by shifting

Q → Given a sorted list and an integer  $x$ .  
find the first <sup>index</sup> value in the list which is  
greater than or equal to  $x$ .

→ [2, 3, 5, 6, 8, 10]  <sub>$n$</sub>

$x = 9$

$a[index] \geq x$

first  
value

$n \leq 10^8$

ans → 3

Linear Search

→  $O(n)$

if  $a[mid] \geq X$   $\rightarrow$  then there is a possibility  
ans  $a[mid]$  can be or cannot be  
the first value  
possible candidate

if  $a[mid] < X$   $\rightarrow$  Neither mid nor left of mid  
can be ans even

bisect library in python  $\rightarrow$  to use binary search

$\rightarrow$  bisect-left(t)  $\rightarrow$  the leftmost possible index to insert  
in the list such that list is still sorted.

$\rightarrow$  bisect-right(t)  $\rightarrow$  the rightmost possible index

$\hookrightarrow$  element

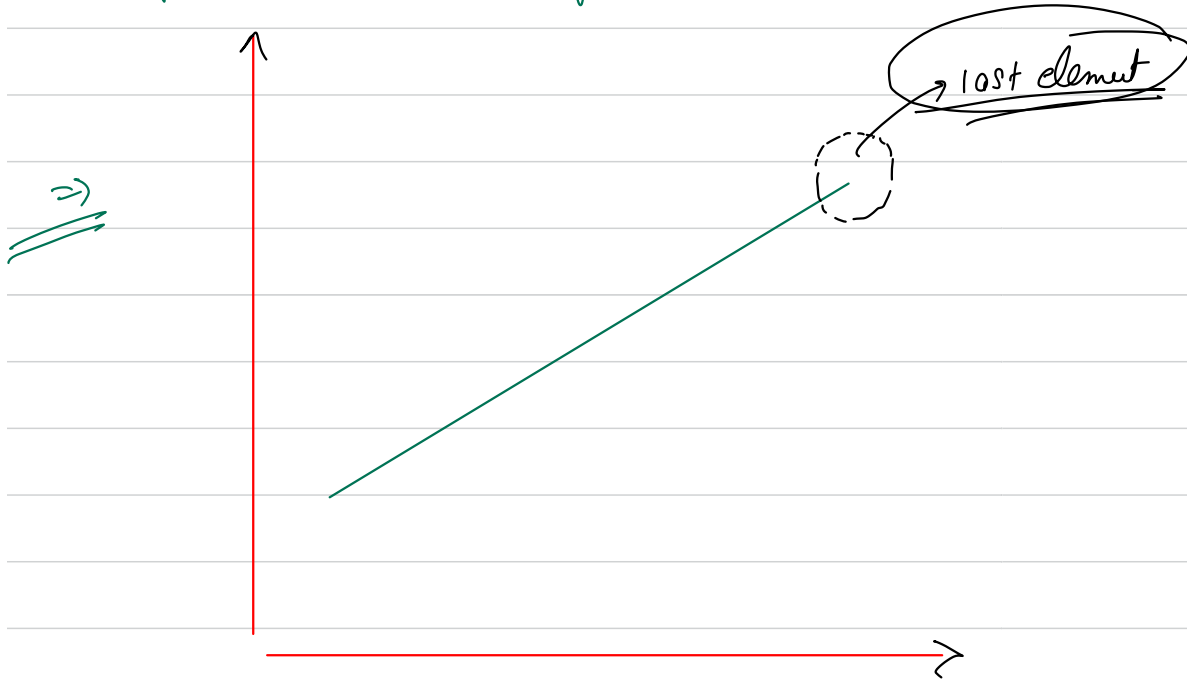
Q Given an unsorted list, find any element  $a[i]$  such that  $a[i] > a[i-1]$  and  $a[i] > a[i+1]$ .  
There can be multiple  $a[i]$ , find any one of them.  
Return the index.

(1, 2, 3, 1)

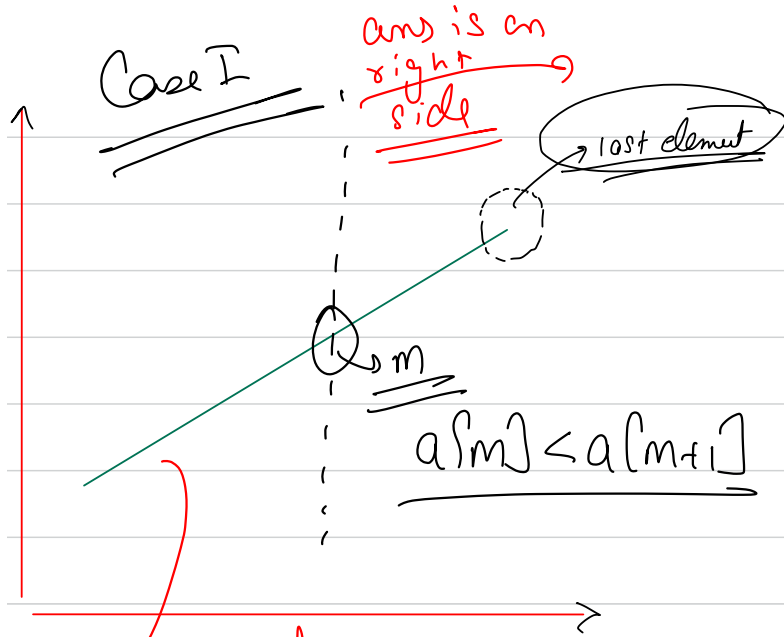
ans  $\rightarrow$  2  $\leftarrow$  index

do something better than  $O(n)$

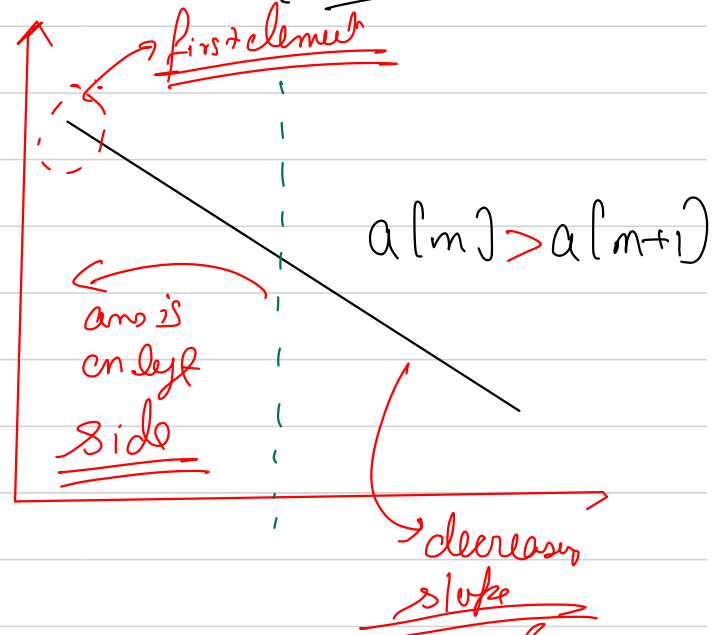
Whether we are able to divide our search  
space into 2 parts based on some property or not.







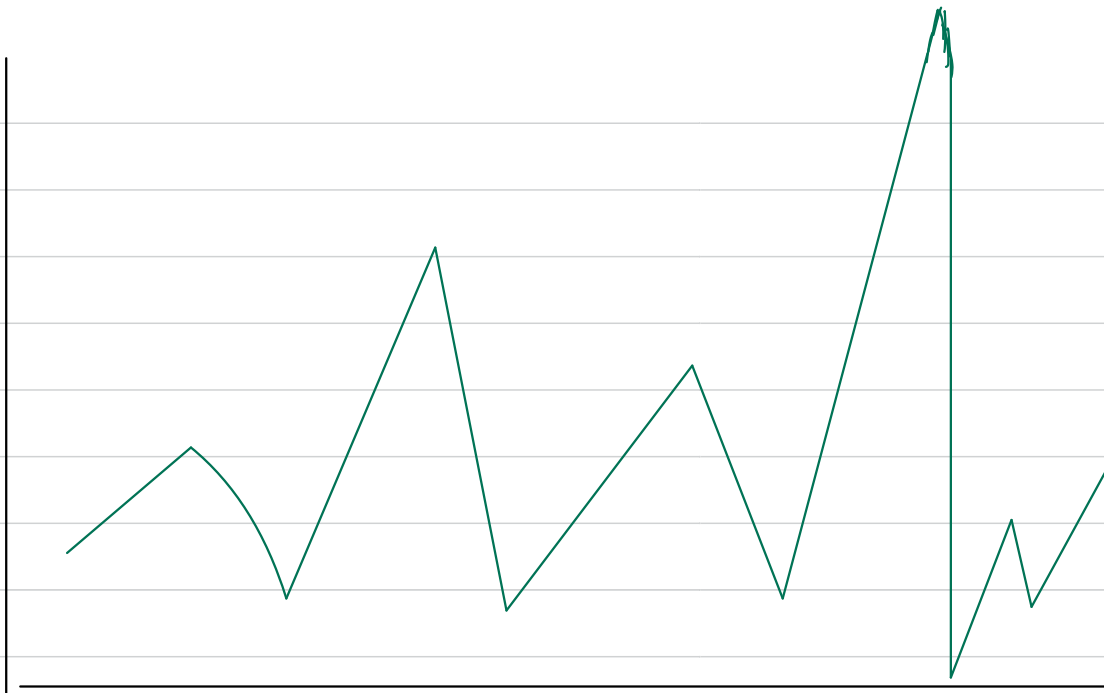
increasing slope



it's neighbors

find an element viz bigger than

$$\underline{O(\log_2 n)} \approx \underline{O(\log_2 r)}$$



$2 \times 10^5$   
 0 1 2 3 4 5 6  
 1 2 1 3 5 6 4



$lo = 0, hi = 6$

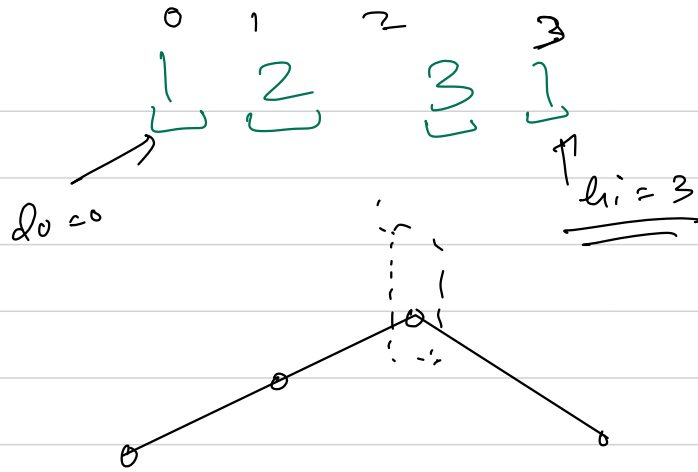
$mid \rightarrow 3$   $\rightarrow$   $lo = 4, hi = 6$

$mid \rightarrow 5$   $\rightarrow$   $lo = 4, hi = 5$

$\underline{mid} \rightarrow 4$   
 $\rightarrow lo = 5, hi = 5$   
 $hi = mid - 1 \rightarrow \underline{hi = mid}$

$lo \rightarrow mid$

$hi \rightarrow mid-1$



$mid \rightarrow 1$

$lo = 1$      $hi = 3$

$mid \rightarrow 2$

$lo = 1$      $hi = 2$

$mid \rightarrow 1$

$lo = 1$      $hi = 2$