

# **Geometric Constructions** through Python



G V V Sharma\*

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Abstract—This manual shows how to construct geometric figures using Python. The problems are based on NCERT math textbooks of Class 9 and 10.

## 1 Triangle

1.1 Consider  $\triangle ABC$  with BC = a, CA = b and AB = c. Let

$$\mathbf{A} = \begin{pmatrix} p \\ q \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} a \\ 0 \end{pmatrix} \tag{1}$$

Find the p and q.

**Solution:** Since

$$\mathbf{p^2} + \mathbf{q^2} = c^2 \tag{2}$$

$$(\mathbf{p} - \mathbf{a})^2 + \mathbf{q}^2 = b^2, \tag{3}$$

we obtain

$$p = \frac{a^2 + c^2 - b^2}{2a}, q = \sqrt{c^2 - p^2}$$
 (4)

- 1.2 Write a program to compute p and q when a = 8, b = 11 and c = 13.
- 1.3 Plot  $\triangle ABC$  for a = 8, b = 11 and c = 13.

**Solution:** The following program plots  $\triangle ABC$ in Fig. 1.3

#Code by GVV Sharma #March 26, 2019 #released under GNU GPL import numpy as np import matplotlib.pyplot as plt

\*The author is with the Department of Electrical Engineering, Indian Institute of Technology, Hyderabad 502285 India e-mail: gadepall@iith.ac.in. All solutions in this manual is released under GNU GPL. Free and open source.

```
#if using termux
import subprocess
import shlex
#end if
#Generate line points
def line gen(A,B):
```

len = 10x AB = np.zeros((2,len))lam 1 = np.linspace(0,1,len)for i in range(len): temp1 = A + lam 1[i]\*(B-A)x AB[:,i] = temp1.Treturn x AB

#Triangle sides

a = 8

b = 11

c = 13

p = (a\*\*2 + c\*\*2-b\*\*2)/(2\*a)

q = np.sqrt(c\*\*2-p\*\*2)

#Triangle vertices

A = np.array([p,q])

B = np.array([0,0])

C = np.array([a,0])

#Generating all lines

x AB = line gen(A,B)

 $x_BC = line_gen(B,C)$ 

 $x_CA = line gen(C,A)$ 

#Plotting all lines

plt.plot(x AB[0,:],x AB[1,:],label='\$AB\$')plt.plot(x BC[0,:],x BC[1,:],label='\$BC\$')plt.plot(x CA[0,:],x CA[1,:],label='\$CA\$')

plt.plot(A[0], A[1], 'o')

1

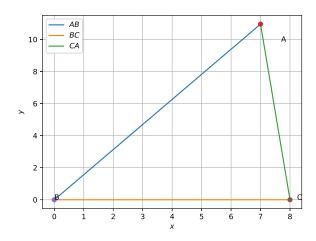


Fig. 1.3

```
plt.text(A[0] * (1 + 0.1), A[1] * (1 - 0.1),
    A')
plt.plot(B[0], B[1], 'o')
plt.text(B[0] * (1 - 0.2), B[1] * (1), 'B')
plt.plot(C[0], C[1], 'o')
plt.text(C[0] * (1 + 0.03), C[1] * (1 - 0.1),
    'C')
plt.xlabel('$x$')
plt.ylabel('$y$')
plt.legend(loc='best')
plt.grid() # minor
#if using termux
plt.savefig('../figs/triangle.pdf')
plt.savefig('../figs/triangle.eps')
subprocess.run(shlex.split("termux-open ../
    figs/triangle.pdf"))
#else
#plt.show()
```

1.4 In  $\triangle ABC$ ,  $a = 7, \angle B = 75^{\circ}$  and b + c = 13. If

$$a^2 + c^2 - b^2 = 2ac\cos B$$
 (5)

find b and c and sketch  $\triangle ABC$ .

- 1.5 In  $\triangle ABC$ , a = 8,  $\angle B = 45^{\circ}$  and c b = 3.5. Sketch  $\triangle ABC$ .
- 1.6 In  $\triangle ABC$ , a = 6,  $\angle B = 60^{\circ}$  and b-c = 2. Sketch  $\triangle ABC$ .
- 1.7  $\triangle ABC$  is right angled at **B**. If a = 12 and b+c = 18, find a, b, c and draw the triangle.
- 1.8 In  $\triangle ABC$ , given that a + b + c = 11,  $\angle B = 45^{\circ}$  and  $\angle C = 45^{\circ}$ , find a, b, c.

**Solution:** We have

$$a = b\cos C + c\cos B \tag{6}$$

$$b\sin C = c\sin B \tag{7}$$

$$a + b + c = 11$$
 (8)

Solving the equivalent matrix equation gives the desired answer.

1.9 Draw  $\triangle ABC$ , given that a+b+c=11,  $\angle B=30^{\circ}$  and  $\angle C=90^{\circ}$ , find a,b,c.

## 2 Circle

2.1 Draw a circle with centre **B** and radius 6. If **C** be a point 10 units away from its centre, construct the pair of tangents *AC* and *CD* to the circle.

**Solution:** From the given information,  $AC \perp BC$ , a = 10 and c = 6.

$$b = \sqrt{a^2 - c^2} \tag{9}$$

The following code draws the circle and tangents in Fig. 2.1

#Code by GVV Sharma #March 26, 2019 #released under GNU GPL import numpy as np import matplotlib.pyplot as plt

#if using termux import subprocess import shlex #end if

#Generate line points
def line\_gen(A,B):
 len =10
 x\_AB = np.zeros((2,len))
 lam\_1 = np.linspace(0,1,len)
 for i in range(len):
 temp1 = A + lam\_1[i]\*(B-A)
 x\_AB[:,i]= temp1.T
 return x AB

#Triangle sides a = 10 c = 6 b = np.sqrt(a\*\*2-c\*\*2)

```
p = (a**2 + c**2-b**2)/(2*a)
q = np.sqrt(c**2-p**2)
#Triangle vertices
A = np.array([p,q])
B = np.array([0,0])
C = np.array([a,0])
D = np.array([p,-q])
#Generating all lines
x AB = line gen(A,B)
x_BC = line_gen(B,C)
x_CA = line_gen(C,A)
x CD = line gen(C,D)
#Plotting all lines
plt.plot(x AB[0,:],x AB[1,:],label='$AB$')
plt.plot(x BC[0,:],x BC[1,:],label='\$BC\$')
plt.plot(x CA[0,:],x CA[1,:],label='$CA$')
plt.plot(x CD[0,:],x CD[1,:],label='$CD$')
plt.plot(A[0], A[1], 'o')
plt.text(A[0] * (1 + 0.1), A[1] * (1 - 0.1),
plt.plot(B[0], B[1], 'o')
plt.text(B[0] * (1 - 0.2), B[1] * (1), 'B')
plt.plot(C[0], C[1], 'o')
plt.text(C[0] * (1 + 0.03), C[1] * (1 - 0.1),
    'C')
plt.plot(D[0], D[1], 'o')
plt.text(D[0] * (1 - 0.2), D[1] * (1), 'D')
#Plotting the circle
theta = np.linspace(0,2*np.pi,50)
x = c*np.cos(theta)
y = c*np.sin(theta)
plt.plot(x,y)
plt.xlabel('$x$')
plt.ylabel('$y$')
plt.legend(loc='best')
plt.grid() # minor
plt.axis('equal')
#if using termux
plt.savefig('../figs/circle.pdf')
plt.savefig('../figs/circle.eps')
subprocess.run(shlex.split("termux-open ../
```

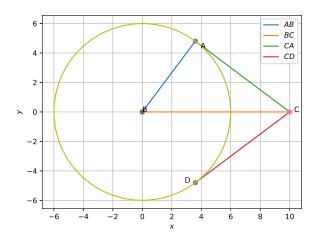


Fig. 2.1

```
figs/circle.pdf"))
#else
#plt.show()
```

- 2.2 Construct a tangent to a circle of radius 4 units from a point on the concentric circle of radius 6 units.
- 2.3 Draw a circle of radius 3 units. Take two points P and Q on one of its extended diameter each at a distance of 7 units from its centre. Draw tangents to the circle from these two points P and Q.
- 2.4 Draw a pair of tangents to a circle of radius 5 units which are inclined to each other at an angle of 60°.
- 2.5 Draw a line segment AB of length 8 units. Taking A as centre, draw a circle of radius 4 units and taking B as centre, draw another circle of radius 3 units. Construct tangents to each circle from the centre of the other circle.
- 2.6 Let ABC be a right triangle in which a = 8, c = 6 and  $\angle B = 90^{\circ}$ . BD is the perpendicular from **B** on AC. The circle through **B**, **C**, **D** is drawn. Construct the tangents from **A** to this circle.