

FATE P01, P02

# Data Anonymization

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Fairness, Accountability, Transparency  
and Ethics of Data Processing (FATE)

# Programming Sessions



1. **6 Labs** = 3 Modules x 2 Sessions

2. **Grading Policy**

|                        |       |                                  |
|------------------------|-------|----------------------------------|
| M1: Data Anonymization | (35%) | Submit by 11:59 PM, Feb 03, 2025 |
|------------------------|-------|----------------------------------|

|                            |       |                                  |
|----------------------------|-------|----------------------------------|
| M2: Algorithmic Fairness I | (30%) | Submit by 11:59 PM, Feb 20, 2025 |
|----------------------------|-------|----------------------------------|

|                             |       |                                  |
|-----------------------------|-------|----------------------------------|
| M3: Algorithmic Fairness II | (35%) | Submit by 11:59 PM, Mar 11, 2025 |
|-----------------------------|-------|----------------------------------|

**You must attend at least one session of each module to be eligible for grading.**

3. **Queries / Discussion**

Please post on the Aula Global Forum for everyone's benefit.

4. **Solved Practices:** To be available after each deadline.

# Overview



1. Attributes in Microdata
2.  $k$ -Anonymity
3. Methods for  $k$ -Anonymity
  - a. Global Recoding (Generalization)
  - b. Micro-Aggregation
4.  $\ell$ -Diversity [ New! ]
5. Local Suppression for  $\ell$ -Diversity

# Attributes In Microdata



## 1. Identifiers

Can unambiguously identify a person ( passport, DNI/NIE, email address, etc. )

## 2. Quasi-Identifiers

Can sometimes identify the person when combined with other quasi-identifiers.

( **gender** <-> zip-code <-> age )

## 3. Confidential Attributes

Sensitive information about a person ( salary, ethnicity, **gender**, etc. )

## 4. Non-Confidential Attributes

Whatever remains...

# k-Anonymity

**D1:**  $x_1, x_2 \in X$  belong to the same **equivalence class** if  $\forall$  quasi-identifiers  $q \in Q, x_1(q) = x_2(q)$ .

**D2:**  $X$  satisfies **k-anonymity** when there exist at least  $k$  elements in each **equivalence class**.

| Gender | Zip-Code | Salary | Equivalence Class |
|--------|----------|--------|-------------------|
| man    | 08010    | <5000€ | C1                |
| man    | 08010    | <5000€ | C1                |
| woman  | 08022    | >5000€ | C2                |
| woman  | 08022    | >5000€ | C2                |

# Global Recoding (Generalization)

| Gender | Zip-Code | Generalized Zip-Code | Salary | Equivalence Class |
|--------|----------|----------------------|--------|-------------------|
| man    | 08011    | 0801*                | <5000€ | C1                |
| man    | 08012    | 0801*                | <5000€ | C1                |
| woman  | 08020    | 0802*                | >5000€ | C2                |
| woman  | 08022    | 0802*                | >5000€ | C2                |

## Remember

All instances in the database are modified during generalization.

( which is why it is **global** )

It is non-perturbative. Why ?

|                   |                        |
|-------------------|------------------------|
| Quasi-Identifiers | Confidential Attribute |
|-------------------|------------------------|

# Micro-Aggregation

| Company | Workers | Aggregated Workers | Profit | Equivalence Class |
|---------|---------|--------------------|--------|-------------------|
| A       | 44      | 41                 | +1000€ | C1                |
| B       | 25      | 27                 | +500€  | C2                |
| C       | 39      | 41                 | +750€  | C1                |
| D       | 30      | 27                 | +300€  | C2                |

## Discuss

Why do we take the **mean**?

Is it **perturbative** OR  
**non-perturbative**?

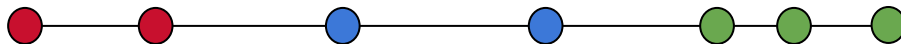
| Identifier | Quasi-Identifiers | Confidential Attribute |
|------------|-------------------|------------------------|
|------------|-------------------|------------------------|

# Micro-Aggregation ► Intuition

## Univariate Case

Sort data by the continuous quasi-identifier

Assign first  $k$  items class 1, next  $k$  items class 2, and so on... ( \*not always optimal )

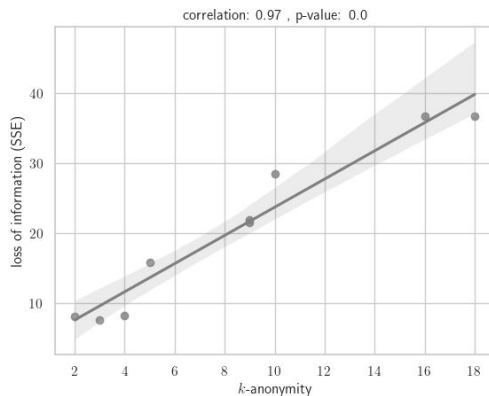
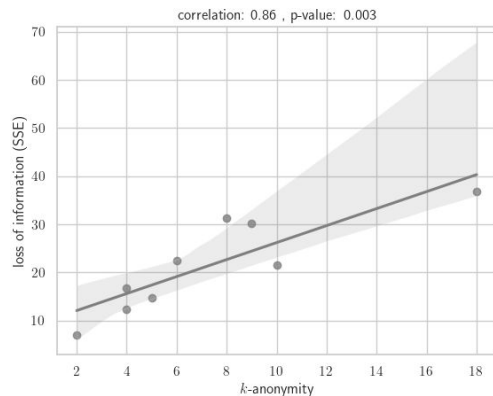
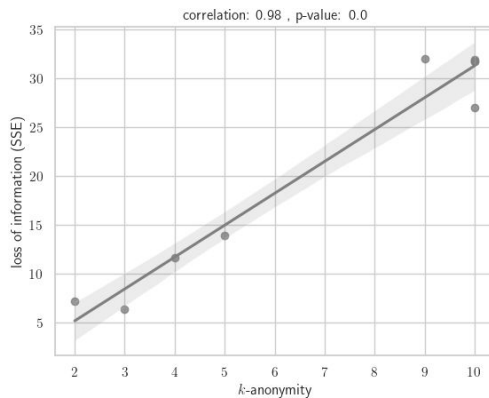
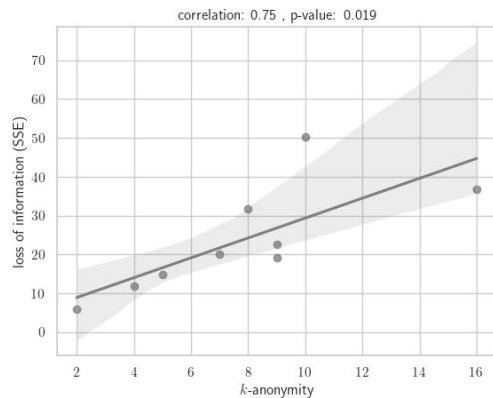


## Multivariate Case

$k$ -Partition Problem with Minimal Information Loss [ NP-Hard ]



# Micro-Aggregation ► Loss of Information



Plots generated across different runs of **Gaussian Mixture Model** to cluster and micro-aggregate data to achieve  $k$ -anonymity.

## Loss of Information

$$SSE = \sum_{c \in C} \sum_{q \in Q_c} (q - \bar{q}_c)'(q - \bar{q}_c)$$

$C$  is the set of equivalence classes

$Q_c$  is the set of quasi-identifier vectors in equivalence class  $c$

# ℓ-Diversity

A dataset  $X$  satisfies **ℓ-diversity** when there exist at least  $\ell$  distinct values of the **confidential attribute** in each **equivalence class**.

| Zip-Code | Profession        | Equivalence Class |
|----------|-------------------|-------------------|
| 0801*    | Software Engineer | C1                |
| 0801*    | Software Engineer | C1                |
| 0802*    | Architect         | C2                |
| 0802*    | Doctor            | C2                |

What is the problem here?

# $\ell$ -Diversity ► Local Suppression

A dataset  $X$  satisfies  **$\ell$ -diversity** when there exist at least  $\ell$  distinct values of the **confidential attribute** in each **equivalence class**.

| Zip-Code | Profession        | Equivalence Class |
|----------|-------------------|-------------------|
| 0801*    | Software Engineer | C1                |
| 0801*    | Engineer          | C1                |
| 0802*    | Architect         | C2                |
| 0802*    | Doctor            | C2                |

What is the problem now?