

## Experiment - 5

Aim: To study PDF & CDF functions of different Discrete Random Variables and the effects of Parametric changes.

Theory: A random variable  $X$  is a function defined on sample space  $S$  of an experiment. Its value are real numbers. For every number 'a' the probability  $P(X=a)$ , with which  $X$  assumes 'a' is defined. Similarly  $P(X \in I)$ , with which  $X$  assumes any value  $\in I$  is defined.

### Discrete Random Variable:

By definition, a random variable and its distribution are discrete if  $X$  assumes only finitely many or at most countably many values  $x_1, x_2, x_3, \dots$  called the possible values of  $X$ . Discrete Distribution of  $X$  is also determined by the probability function  $f(x)$  of  $x$ , defined by

$$f(x) = \begin{cases} p_j & \text{if } x = x_j \\ 0 & \text{otherwise} \end{cases} \quad (j = 1, 2, \dots)$$

From this we get the values of the distribution function.

$$F(x) = \sum_{x_j \leq x} f(x_j) = \sum_{x_j \leq x} p_j$$

## Bernoulli Random Variable

It is Discrete Probability distribution of a random variable which takes the value 1 with prob.  $P$  & value 0,  $q=1-P$

$$\text{PDF} \rightarrow f_x(x) = \begin{cases} (1-P)\delta(x) + P\delta(x-1) & x=1 \\ 0 & x=0 \end{cases}$$

$$\text{CDF} \rightarrow F_x(x) = (1-P)u(x) + P u(x-1)$$

$$\text{Mean} = P \quad \text{Variance} = P(1-P)$$

## Binomial Distributions

$$\text{PDF} \quad f_x(x) = \sum_{k=0}^n \binom{n}{k} P^k (1-P)^{n-k} \delta(x-k)$$

$$\text{CDF} \quad F_x(x) = \sum_{k=0}^n \binom{n}{k} P^k (1-P)^{n-k} u(x-k)$$

$$\text{Mean} \quad \bar{x} = np \quad \text{Variance} \quad \sigma_x^2 = np(1-P)$$

The Binomial distribution occurs in game of chance, opinion polls, medicine, & so on.

## Poisson Distribution

The discrete distribution with infinitely many possible

$$f(x) = \frac{\mu^x}{x!} e^{-\mu}$$

is called Poisson distribution. Special case of Binomial distribution for  $n \rightarrow \infty \parallel \rightarrow np = \lambda$ .

$$\text{PDF} \quad f_x(x) = \sum_{k=0}^{\infty} \frac{e^{-\lambda}}{k!} \lambda^k \delta(x-k)$$

$$\text{Mean} \quad \bar{x} = \lambda$$

$$\text{Variance} \quad \sigma_x^2 = \lambda$$