

Problem 5

Dry Run & Analyze: Time and space complexity.

1. Dry run the code for $n=4$. How many times is printed? what is the time complexity?

```

void printTriangle(int n){
    for (int i=0; i<n; i++)
        for (int j=0; j<=i; j++)
            System.out.print(" *");
}

```

Ans:-

Dry Run for $n=4$:

$n=4$

- $i=0$: j runs 0 \rightarrow prints 1*
 - $i=1$: $j=0,1 \rightarrow$ prints 2*
 - $i=2$: $j=0,1,2 \rightarrow$ prints 3*
 - $i=3$: $j=0,1,2,3 \rightarrow$ prints 4*
- Total * printed $1+2+3+4=10$

Time complexity

- Outer loop runs n times
- Inner loop runs $i+1$ times
- Total iterations: $1+2+\dots+n = \frac{n(n+1)}{2} = O(n^2)$

Total * : 10

Time complexity: $O(n^2)$

Space complexity: $O(1)$

Q2

Dry run for $n=8$. what's the number of iterations? Time Complexity.

```
void printPattern(int n) {  
    for (int i = 1; i <= n; i *= 2)  
        for (int j = 0; j < n; j++)  
            System.out.println(i + ", " + j);  
}
```

Ans:- Dry run for $n=8$:

- $i : 1, 2, 4, 8 \rightarrow 4$ iterations
- inner loop runs $n=8$ times for each i

Total iterations = $4 \times 8 = 32$

Time Complexity

- outer loop: $O(\log n)$
- inner loop: $O(n)$
- Total: $O(n \log n)$.

Answer:-

Total iterations: 32

Time Complexity: $O(n \log n)$

Space Complexity: $O(1)$

Q3. Dry run for $n=20$. How many recursive calls? what values are printed?

```
void recHalf(int n) {
    if (n <= 0) return;
    System.out.print(n + " ");
    recHalf(n/2);
}
```

Ans- Dry run for $n=20$:

- call `recHalf(20)` → prints 20
- `recHalf(10)` → prints 10
- `recHalf(5)` → prints 5
- `recHalf(2)` → prints 2
- `recHalf(1)` → prints 1
- `recHalf(0)` → stops

Printed values : 20 10 5 2 1

Recursive calls : 6 (including base case)

Time Complexity : $O(\log n)$

- Each call divides n by 2

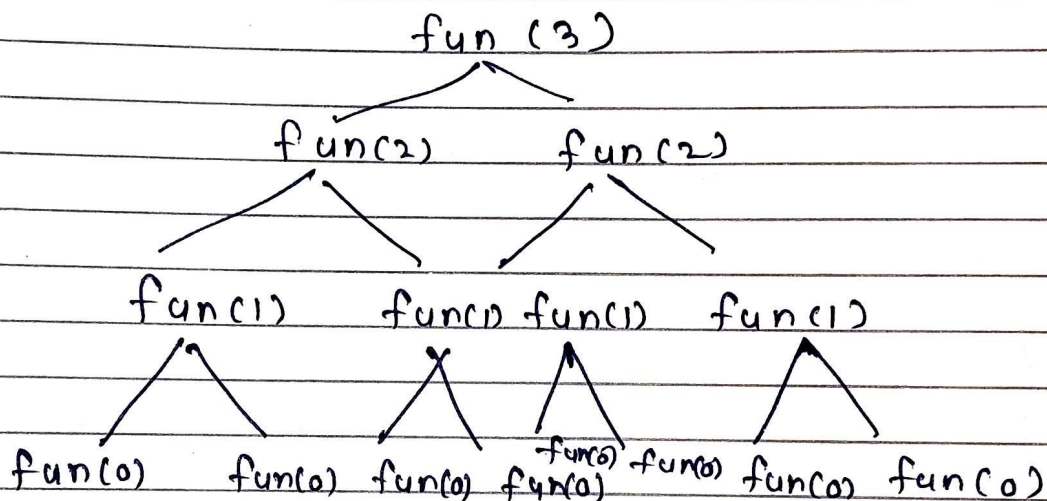
Answer :-

- printed : 20 10 5 2 1
- Recursive calls : 6
- Time Complexity : $O(\log n)$
- Space Complexity : $O(\log n)$

4. Dry run for $n=3$. How many total calls are made? what's the time complexity?

```
void fun(int n) {
    if (n == 0) return;
    fun(n-1);
    fun(n-1);
}
```

Ans 3



Total calls.

This form a full binary tree with $2^n - 1$ calls for $n=3$, total $2^3 - 1 = 7$

Time complexity : $O(2^n)$

Space complexity : $O(n)$

Answer.

Total calls : 7

Time complexity : $O(2^n)$

Space complexity : $O(n)$

5. Dry run for $n=3$. How many total iterations? Time Complexity?

```
void tripleNested (int n) {  
    for (int i=0; i<n; i++)  
        for (int j=0; j<n; j++)  
            for (int k=0; k<n; k++)  
                System.out.println(i+j+k);  
}
```

Ans:- Dry run for $n=3$

• All three loops run from 0 to 2

• Total iterations: $n \times n \times n = 3^3 = 27$.

Time complexity: $O(n^3)$

• Each loop runs n times

Answer

• Total iterations: 27

• Time Complexity: $O(n^3)$

• Space Complexity: $O(1)$