

WS Q2

$$x^2 y'' + 7xy' + 9y = 0 \quad \text{let } y = x^n$$

$$x^2 n(n-1)x^{n-2} + 7xn x^{n-1} + 9x^n = 0$$

$$n(n-1) + 7n + 9 = 0$$

$$n^2 + 6n + 9 = 0$$

$$(n+3)^2 = 0$$

$$n = -3 \quad \text{repeated root}$$

Thus $y = C_1 x^n + C_2 (\ln x) x^n$
 $= C_1 x^{-3} + C_2 (\ln x) x^{-3}$ is the general sol.