

Homework N 20

N 2a.

$M = \text{"DO NOT PASS GO"}$

$K = 3$. Formula $f(p) = (p+k) \bmod 26$

$$D \rightarrow 3 + K = 6 \rightarrow G$$

$$O \rightarrow 14 + K = 17 \rightarrow R$$

$$N \rightarrow 13 + K = 16 \rightarrow Q$$

$$T \rightarrow 19 + K = 22 \rightarrow W$$

$$P \rightarrow 15 + K = 18 \rightarrow S$$

$$A \rightarrow 0 + K = 3 \rightarrow D$$

$$S \rightarrow 18 + K = 21 \rightarrow V$$

$$G \rightarrow 6 + K = 9 \rightarrow J$$

Encrypted $M = GRQWSDVJ$

Encrypted $M = GRQRWSDVJR$

N 4a.

Decrypt $M = \text{"EOXHNHDQV"}$

$K = 3$. Formula $f^{-1}(p) = (p-k) \bmod 26$

$$E \rightarrow 4 - 3 = 1 \rightarrow B$$

$$O \rightarrow 14 - 3 = 11 \rightarrow L$$

$$X \rightarrow 23 - 3 = 20 \rightarrow U$$

$$H \rightarrow 7 - 3 = 4 \rightarrow E$$

$$M \rightarrow 12 - 3 = 9 \rightarrow J$$

$$D \rightarrow 3 - 3 = 0 \rightarrow A$$

$$Q \rightarrow 16 - 3 = 13 \rightarrow N$$

$$V \rightarrow 21 - 3 =$$

Decrypted $M =$

N?

Cryptanalysis

NBOKW"

$O \times 5$, we ca

$K = 10$. Formu

$D \rightarrow 3 - 10 =$

$Y \rightarrow 24 - 10 =$

$C \rightarrow 2 - 10 =$

$V \rightarrow 21 - 10 =$

$O \rightarrow 14 - 10 =$

$Z \rightarrow 25 - 10 =$

$B \rightarrow 1 - 10 =$

$N \rightarrow 12 - 10 =$

$R \rightarrow 17 - 10 =$

$K \rightarrow 10 - 10 =$

$X \rightarrow 2 - 10 =$

$N \rightarrow 1 - 10 =$

$W \rightarrow 2 - 10 =$

Decrypt

TO

$$V \rightarrow 21 - 3 = 18 \rightarrow S$$

Decripted M = "BLUE JEANS"

N?

Cryptanalyse M = "DY WOOZ ZOBMRKXMO DY
NBOKW"

D \times 5, we can assume it's E then it ~~means~~ means $14 - 4 = 10$

$k=10$. Formula $f^{-1}(p) = (p-k) \bmod 26$

$$D \rightarrow 3 - 10 = -7 \bmod 26 \rightarrow = 19 \rightarrow T$$

$$Y \rightarrow 24 - 10 = 14 \bmod 26 \rightarrow 0$$

$$C \rightarrow 2 - 10 = -8 \bmod 26 = 18 \rightarrow S$$

$$V \rightarrow 21 - 10 = 11 \rightarrow L$$

$$O \rightarrow 14 - 10 = 4 \rightarrow E$$

$$Z \rightarrow 25 - 10 = 15 \rightarrow P$$

$$B \rightarrow 1 - 10 = -9 \bmod 26 = 17 \rightarrow R$$

$$M \rightarrow 12 - 10 = 2 \rightarrow C$$

$$R \rightarrow 17 - 10 = 7 \rightarrow H$$

$$K \rightarrow 10 - 10 = 0 \rightarrow A$$

$$X \rightarrow 23 - 10 = 13 \rightarrow N$$

$$N \rightarrow 13 - 10 = 3 \rightarrow D$$

$$W \rightarrow 22 - 10 = 12 \rightarrow M$$

Decripted M = "TO SLEEP ~~FOR~~ PERCHANCE
TO DREAM,"

N11.

Decryption fun. for Affine Cipher

$$c = (15p + 13) \text{ mod } 26,$$

1. To find modular inverse of $a \text{ mod } 26$, mod inverse .

$$2. p = \bar{a}(c - b) \text{ mod } 26$$

$$\text{Formula, } f(p) = (ap + b) \text{ mod } 26 \rightarrow a = 15 \text{ and } b = 13$$

$$1) \text{Modular Inverse } ax \equiv 1 \text{ mod } 26$$

$$15 \cdot 2 \equiv 4 \text{ mod } 26$$

$$15 \cdot 4 \equiv 8 \text{ mod } 26$$

$$15 \cdot 8 \equiv 16 \text{ mod } 26$$

$$15 \cdot 11 \equiv 9 \text{ mod } 26$$

$$15 \cdot 14 \equiv 2 \text{ mod } 26$$

Picking

Extended Euclidean Algo.

$$\gcd(a, m) \rightarrow a = 15, m = 26$$

$$sa + tm = \gcd(a, m) = 1$$

$$sa + tm = 1 \text{ mod } m$$

$$\exists 15s + 26t = 1 \text{ mod } 26$$

$$\cancel{2 \cdot 15 + 9 = 26} \quad \cancel{1 \cdot 15 + 11 = 26}$$

$$11 = 26 - (1 \cdot 15) = 11$$

$$11 = 26 - 1 \cdot 15 \Rightarrow 26 - (1 \cdot 15) = 11$$

$$11 = 26 - 1 \cdot 15 \Rightarrow 26 - (1 \cdot 15) = 11$$

$$11 = 26 - 1 \cdot 15 \Rightarrow 26 - (1 \cdot 15) = 11$$

$$11 = 26 - 1 \cdot 15 \Rightarrow 26 - (1 \cdot 15) = 11$$

$$11 = 26 - 1 \cdot 15 \Rightarrow 26 - (1 \cdot 15) = 11$$

$$2) P = 4$$

$$P = (7c -$$

$$P = (7c -$$

$$P = (7c -$$

N24.

Encrypt

$$A \rightarrow 00$$

$$T \rightarrow 18$$

$$C \rightarrow 02$$

$$K \rightarrow 10$$

$$M_1 = 19$$

$$M_2 = 1$$

$$M_3 = 21$$

$$C_1 = 1$$

$$C_2 = 1$$

$$C_3 = 1$$

Cipher

N29

Diff

Publi

plie

Bol

$$2) p = 7(c - 13) \pmod{26}$$

$$p = (7c - 7 \cdot 13) \pmod{26}$$

$$p = (7c - 91) \pmod{26}$$

$$p = (7c + 13) \pmod{26} \text{ or } p = 7(c - 13) \pmod{26}$$

N₂₄.

Encrypt $M \in \text{"ATTACK"}$ using RSA $\rightarrow n = 43 \cdot 53, e = 13$

$$A \rightarrow 00$$

$$T \rightarrow 18$$

$$C \rightarrow 02$$

$$K \rightarrow 10$$

$$M_1 = 19 \text{ (AT)} \rightarrow 180019 \rightarrow 18$$

$$M_2 = 1900 \text{ (TA)} \rightarrow 1900$$

$$M_3 = 210 \text{ (CK)} \rightarrow 0210 \rightarrow 210$$

$$C_1 = 18^{13} \pmod{2537} = 1819$$

$$C_2 = 1900^{13} \pmod{2537} = 1415$$

$$C_3 = 210^{13} \pmod{2537} = 0981$$

Ciphertext : 1819 1415 0981

N₂₅

Diffie-Hellman. $p = 23, a = 5, K_1 = 8, K_2 = 5$.

Public Keys, $p = 23$ and $a = 5$

Alice - $K_1 = 8$

Bob - $K_2 = 5$

Alice:

$$A = a^{k_1} \bmod p = 5^8 \bmod 23$$

$$5^8 = 380625$$

$$380625 \bmod 23 = 16$$

Bob:

$$B = a^{k_2} \bmod p \rightarrow 5^5 \bmod 23$$

$$5^5 = 3125$$

$$3125 \bmod 23 = 20$$

$$A = 16 \quad B = 20$$

$$s_{\text{Alice}} = B^{k_1} \bmod p \rightarrow 20^8 \bmod 23 \Rightarrow 18$$

~~20⁸ ≈~~

$$s_{\text{Bob}} = A^{k_2} \bmod p \rightarrow 16^5 \bmod 23 \Rightarrow 18$$

$$s = 18.$$