

Cryptographic protocols

Or how to use maths to keep secrets

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Short bio

- I did my bachelor's degree here at UniMelb (in maths and CS)
- I did my PhD at Stanford Uni in California
- I am interested in using cryptography for large complicated computations in which you don't trust all the participants
- My favourite research application is electronic elections
 - In which there's a fair argument for not trusting anyone
- I also waste a lot of time writing op ed pieces about how it shouldn't have been done

Chapter 1:

Public Key cryptography

Or how to send secret messages to people you haven't met

What's cryptography?

- Sending messages that are secret from everyone but the intended recipient
- The sender has to “hide” the message for sending, so nobody else can understand it
 - This is called **encrypting**
- The receiver has to “un-hide” and recover the message
 - This is called **decrypting**
- **Public key cryptography is one of the greatest ideas in computer science ever**

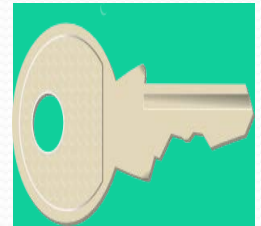
Before public-key cryptography

- There was **secret-key cryptography**
- Both the sender and the receiver had to agree on the secret key in advance
 - They had to “meet” somehow
- Encrypting and decrypting used the same key
 - These are still used, e.g. AES

Sender



Receiver



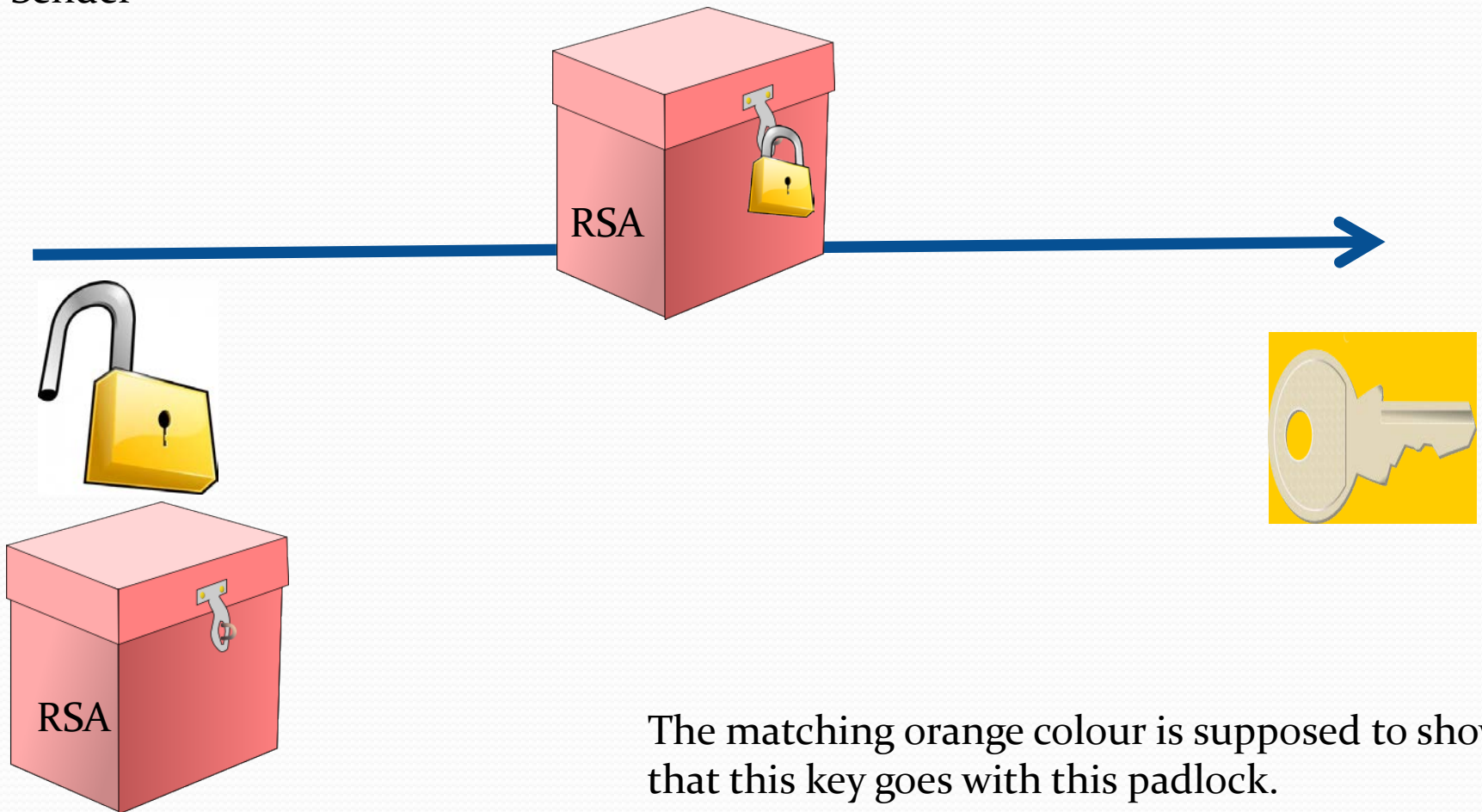
What's public-key cryptography?

- The receiver generates two keys:
 - a public key e (for encrypting), and
 - a private key d (for decrypting)
- She publicises the public key e
 - People use this for encrypting messages
- She keeps the private key d secret
 - She uses this for decrypting messages

Picture of public-key cryptography

Sender

Receiver



The matching orange colour is supposed to show that this key goes with this padlock.

Example: RSA (for the mathematically inclined)

- The receiver thinks of two large prime numbers p, q
 - About 300 digits long
 - She multiplies them together to get $N=pq$
 - She generates the public key e (almost any e will do)
 - She publicises (N, e) . This is her full public key.
- To encrypt message m , compute
 - $m^e \bmod N$
 - (This means take the remainder when m^e is divided by N)
- The receiver can decrypt because she knows p and q
 - Take my word for this for now – it's not supposed to be obvious
 - Nobody else can factorise N – the computation takes too long

Example: RSA (for the even more mathematically inclined)

- The receiver thinks of two large prime numbers p, q
 - About 300 digits long
 - She multiplies them together to get $N=pq$
 - She generates the public key e (almost any e will do as long as it's coprime to $(p-1)(q-1)$)
 - She publicises (N, e) . This is her full public key.
- To encrypt message m ,
 - Pad m with a carefully chosen random string r
 - Compute $(m || r)^e \bmod N$
 - (This means take the remainder when $(m || r)^e$ is divided by N)
- The receiver can decrypt because she knows p and q
 - Take my word for this for now – it's not supposed to be obvious
 - But if you look up the Wikipedia RSA page at See [http://en.wikipedia.org/wiki/RSA_\(algorithm\)](http://en.wikipedia.org/wiki/RSA_(algorithm))
 - and the Euler-Fermat Theorem, you'll be able to figure it out.
 - Nobody else can factorise N . The computation takes too long
 - Strictly speaking, breaking RSA has never been shown to be as difficult as factorising N , but nobody has found a faster way to do it either

The Chinese remainder theorem

- https://en.wikipedia.org/wiki/RSA_%28cryptosystem%29#Using_the_Chinese_remainder_algorithm

- Q: How long does e need to be?

- A: Not very long, because padding m with random junk ensures that $m^e \bmod N$ is always many times larger than N . Choosing $e = 1 + 2^{16} = 65,537$ is popular because it makes m^e easy to compute quickly. There are subtle reasons why very small e is insecure.
- If you're really interested, see <http://crypto.stanford.edu/~dabo/abstracts/RSAattack-survey.html>

What is that good for?

- Exchanging a secret key for secret-key cryptography
 - The sender
 - generates a secret key,
 - encrypts a message with the secret key,
 - encrypts the secret key with the receiver's public key, and
 - sends the encrypted message and the encrypted key.
 - The receiver
 - Uses her private key to decrypt the secret key
 - Uses the secret key to decrypt the message
- This is (almost but not quite) how SSL/TLS works, when you get a comforting little lock at the bottom of your screen before you send your credit card number
- **Exercise:** draw a picture of this protocol, using boxes, padlocks and keys

What else is that good for?

- Lots of people sending to the same receiver
- e.g. in electronic voting, everyone sends their vote to the Electoral Commission
 - Encrypted with the Commission's public key

Python cryptography library

- From <https://cryptography.io/en/latest/hazmat/primitives/asymmetric/rsa/>
- This is a “Hazardous Materials” module. You should **ONLY** use it if you’re 100% absolutely sure that you know what you’re doing because this module is full of land mines, dragons, and dinosaurs with laser guns.
- `from cryptography.hazmat.backends import default_backend`
- `from cryptography.hazmat.primitives.asymmetric import rsa`
- `key=rsa.generate_private_key(public_exponent=65537, key_size=2048, backend=default_backend())`
- `Key.public_key().public_numbers()`
- `Key.private_numbers().p`
- `Key.private_numbers().q`



Python RSA (encryption)

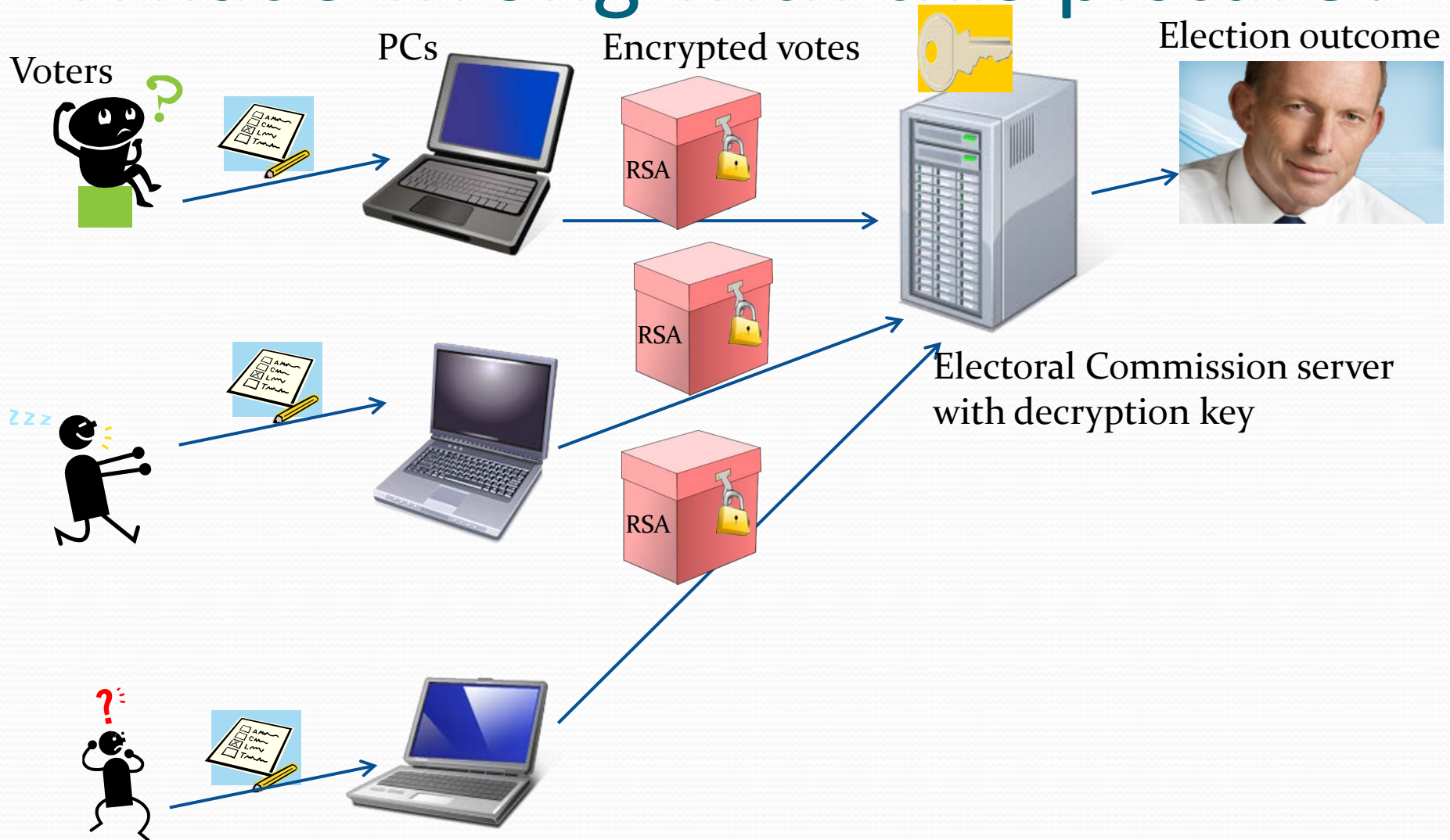
- `private_key=key.private_numbers()`
- `public_key=key.public_key()`
- `from cryptography.hazmat.primitives.asymmetric import padding`
- `from cryptography.hazmat.primitives import hashes`
- `message = b"encrypted data"`
- `ciphertext = public_key.encrypt(message,`
- `padding.OAEP(`
- `mgf=padding.MGF1(algorithm=hashes.SHA1()),`
- `algorithm=hashes.SHA1(),`
- `label=None`
- `)`
- `)`
- `** note: SHA1 is outdated, but more recent things like SHA256/512 aren't supported.`

- Plaintext=key.decrypt(
 - ... ciphertext,
 - ... padding.OAEP(...
 - mgf=padding.MGF1(algorithm=hashes.SHA1()), ...
 - algorithm=hashes.SHA1(), ... label=None
 - ...)
 - ...)

Chapter 2: Internet voting

Or how to use maths to save democracy

What's wrong with this picture?





Answers from the class

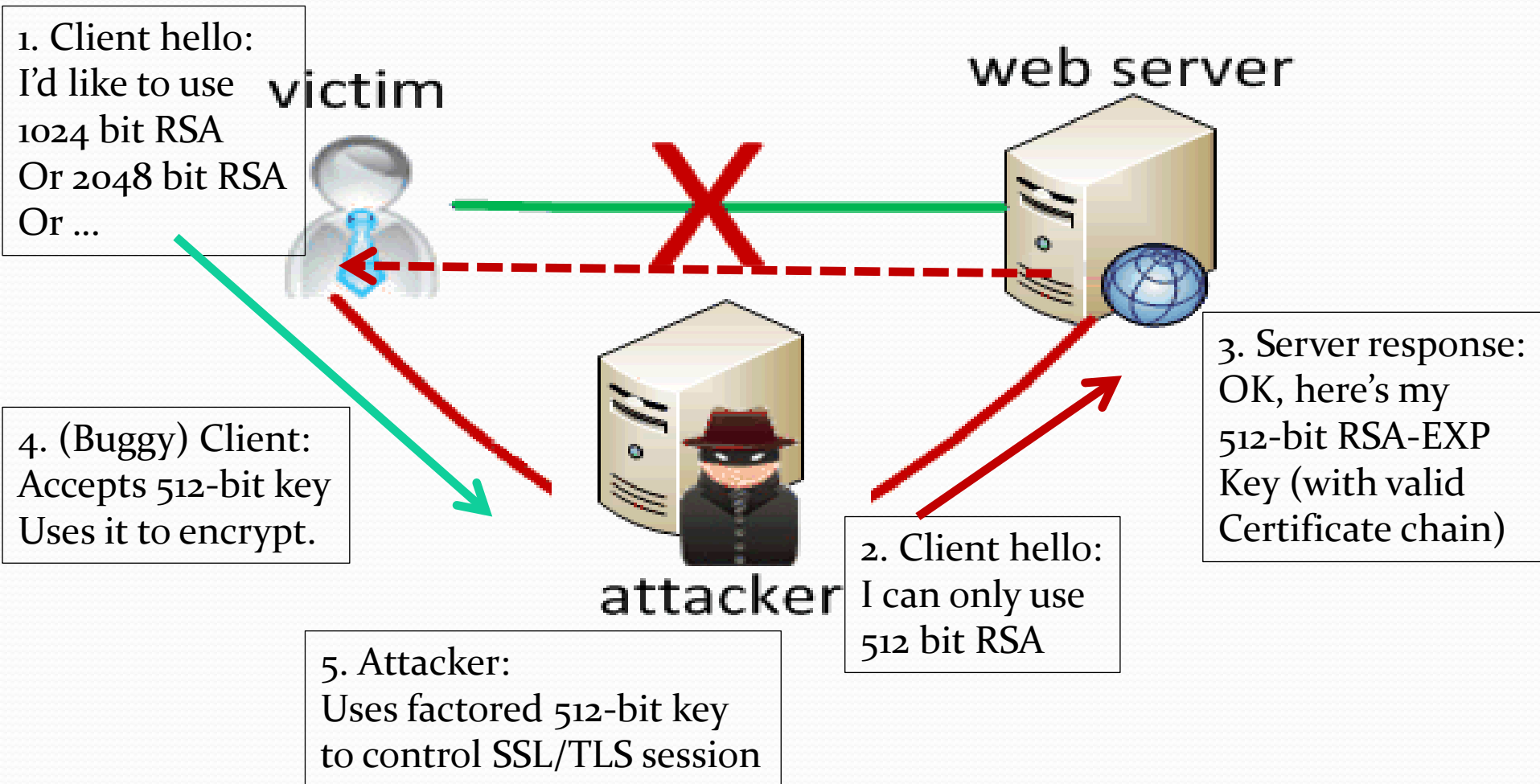
Security Requirements

- Verifiability, so that no-one can manipulate the output
 - Only eligible voters vote
 - At most once
 - Voters should get evidence that their vote was
 - Cast as they intended
 - Counted as cast
 - Everyone gets evidence votes were properly tallied
- Privacy, so coercers can't manipulate the inputs
 - Even if the voter tries to prove how they voted (receipt-freeness)
- Achieving both is hard, especially for remote voting
- I don't know how to solve the problem completely, and neither does anybody else

Factoring RSA Export keys (FREAK)

- First some history:
 - In ancient times (around the 1990s) the US government restricted the export of strong crypto, in particular of RSA using more than 512 bit keys.
 - Web servers and clients within the US could use strong RSA parameters;
 - Software made outside the US was (obviously) not bound by the restriction, but
 - Software produced in the US but exported outside was restricted to this “Export grade” crypto
 - So lots of servers (and clients) maintained the option to use “export grade” crypto, just in case they had to communicate with a restricted computer
 - Unfortunately, many still do (or did until very recently)
 - Many servers used the same 512-bit key over and over again.
 - 512-bit “export grade” RSA now costs about \$100 to break running overnight on Amazon’s EC2 cloud.
(<https://www.cis.upenn.edu/~nadiah/projects/faas/>)

FREAK – intercepting SSL/TLS key establishment



NSW iVote Internet voting security

- The iVote internet voting system was trusted recently in the NSW state election for the return of 280,000 electronic ballots
- During the election period, Alex Halderman and I found a serious security hole that left votes open to manipulation and privacy breach using the FREAK attack
- We notified the Australian CERT, who notified the NSW Electoral Commission, who fixed it, but by then 66,000 votes had been cast
- The final margin of the last seat in the NSW Legislative Council was 3177 votes