

COMP20003
Algorithms and Data Structures
Distribution Counting

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Sorting by Counting



- Distribution counting:
 - unusual approach to sorting
- Later we will look at more common approaches
- Distribution counting **requires**:
 - Key values to be **within** a certain **range**, *lower to upper*.

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2-2

**Sorting by Counting:
 Approach**

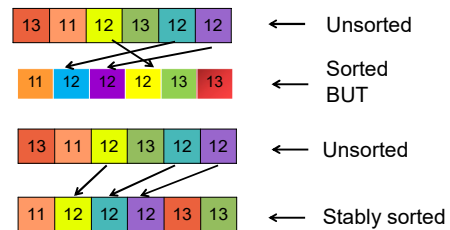


- Steps in distribution counting:
 - Start with array of:
 - Records, or
 - Keys + pointers to records
 - Count number of **records** associated with **each key value** (*lower to upper*)
 - Redistribute array elements
- Net result:
 - Sorted array
 - Stable sort

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Segue: What is a stable sort?



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Stable sorting: definition

Stable sorting algorithms maintain relative order of records with equal key values.

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1-5

Stable sorting: Applications

- Want file sorted on one key, and within each group, sorted on another key:

| sorted by time | sorted by location (not stable) | sorted by location (stable) |
|------------------|---------------------------------|-----------------------------|
| Chicago 09:00:00 | Chicago 09:25:52 | Chicago 09:00:00 |
| Phoenix 09:00:03 | Chicago 09:03:13 | Chicago 09:00:03 |
| Houston 09:00:13 | Chicago 09:11:05 | Chicago 09:00:13 |
| Chicago 09:00:59 | Chicago 09:19:46 | Chicago 09:00:59 |
| Houston 09:01:10 | Chicago 09:19:32 | Chicago 09:01:10 |
| Chicago 09:01:13 | Chicago 09:00:00 | Chicago 09:01:13 |
| Seattle 09:10:11 | Chicago 09:35:21 | Chicago 09:10:11 |
| Seattle 09:10:25 | Chicago 09:00:59 | Chicago 09:10:25 |
| Phoenix 09:14:25 | Houston 09:01:10 | Chicago 09:35:21 |
| Chicago 09:19:32 | Houston 09:00:13 | Houston 09:00:13 |
| Chicago 09:19:46 | Phoenix 09:37:44 | Houston 09:01:10 |
| Chicago 09:21:05 | Phoenix 09:00:03 | Phoenix 09:00:03 |
| Seattle 09:22:43 | Phoenix 09:14:25 | Phoenix 09:14:25 |
| Seattle 09:22:54 | Seattle 09:10:25 | Phoenix 09:37:44 |
| Chicago 09:25:52 | Seattle 09:36:14 | Seattle 09:10:11 |
| Chicago 09:35:21 | Seattle 09:22:43 | Seattle 09:10:25 |
| Seattle 09:36:14 | Seattle 09:10:11 | Seattle 09:22:43 |
| Phoenix 09:37:44 | Seattle 09:22:54 | Seattle 09:36:14 |

Stability when sorting on a second key

Example from Sedgwick and Wayne, Algorithms, 4th Edition, 2011

1-6

Back to Distribution Counting: Approach

- Steps in distribution counting:
 - Input: array of:
 - records, or
 - keys + pointers to records
 - Count number of records associated with each key value (lower to upper).
 - Redistribute array elements.
 - Output: stably sorted array.

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Back to Distribution Counting: Example:

- Sort [4,4,2,2,0,2,1,3,2,4,3,1,4,3,1,4]
- Count records for each key [1,3,4,3,5]
 - CumulativeCount = [0,1,4,8,11]
- Redistribute
 - Create auxiliary array
 - traverse original array copying each item to position:
 - aux_array[cumulativeCount[item.key]] = item
 - Increase cumulativeCount[itemkey] + 1

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Distribution Counting: Analysis

- Time:
 - Worst-case:
 - Average-case:
- Space:

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Does the key range influence the complexity?

- $O(n)$ if range r of keys is in $O(n)$
 - `count[]` array size is r
 - Initialization and shuffling are $O(r)$
 - So if $r > n \dots$

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But what about theory?

- we said weeks ago:
 - Comparison-based sorting is $\Omega(n \log n)$
- Does distribution counting contradict that statement?

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Sorting without comparing

- Other non-comparison-based sorting algorithms include:
 - LSD Radix sort
 - MSD Radix sort
 - Several others
- Drawbacks:
 - Take extra space
 - Generally less flexible than comparison-based
 - Can be fiddly if keys are not the same length, e.g. variable length strings in MSD radix

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1-12