COMP20007 Design of Algorithms

Week 2



Administrivia

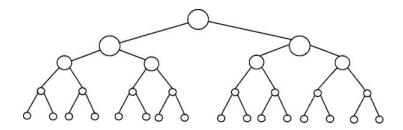
- 1. Tute and lab attendance
- 2. Lecture capture
 - sort of works but doesn't get the document camera
- 3. Assessment:
 - handbook says project will be due in week 4
 - we want to give you til end of week 5
 - two implementation methods
 - mid-semester test is worth 10%
 - use it to lock in marks
 - if you do better in the final exam, we'll scale that
 - max(MST + Exam, 70/60 * Exam)

4. Office hours:

- Tuesday 11, Wednesday 2:15
- Friday 10 (this week only)
- other times by appointment

Theoretical limits: e.g. sorting

- "Guess the number I'm thinking of"
 - o integers 1..2^p
 - o how many questions do you need?



- Apply this idea to sorting n items: A, B, C, ...
 - "guess how I've scrambled the sorted list"
 - decision tree for n=2:AB BA
 - decision tree for n=3:
 ABC ACB BAC
 BCA CAB CBA
 - $\circ \qquad \text{Stil} \\ n! \sim \sqrt{2\pi n} \left(\frac{n}{e}\right)^{n}$
 - We'll return to this in week 12



More examples of divide-and-conquer: Matrix multiplication

• Method 1 $XY = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} E & F \\ G & H \end{bmatrix} = \begin{bmatrix} AE + BG & AF + BH \\ CE + DG & CF + DH \end{bmatrix}$

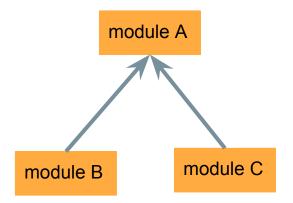
Method 2 (Strassen 1969)

$$XY = \begin{bmatrix} P_5 + P_4 - P_2 + P_6 & P_1 + P_2 \\ P_3 + P_4 & P_1 + P_5 - P_3 - P_7 \end{bmatrix}$$

$$P_1 = A(F - H)$$
 $P_5 = (A + D)(E + H)$
 $P_2 = (A + B)H$ $P_6 = (B - D)(G + H)$
 $P_3 = (C + D)E$ $P_7 = (A - C)(E + F)$
 $P_4 = D(G - E)$

Divide and Conquer revisited: multi-module programs

- "let's break it down"
 - o benefits of modularity?
- architecture diagram
- how this is done in C
 - o command line (bash, MinGW)
 - extern
 - Makefiles



A basic multi-module C program

```
load.h:
                                         extern int data;
prog.c:
                                         load.c:
#include <stdio.h>
#include "load.h"
                                         #include "load.h"
int main() {
  printf("%d\n", data);
                                         int data = 2;
                                         gcc -c load.c
gcc -c prog.c
(compiling)
```

gcc -o prog prog.o load.o (linking)

Makefiles, dependencies, and toposort