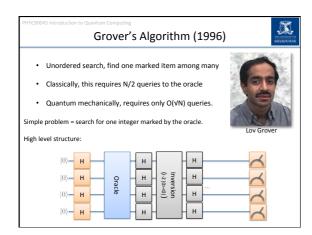
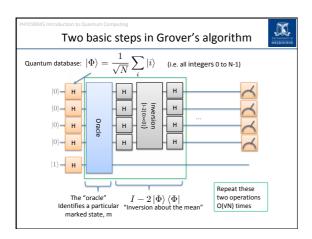
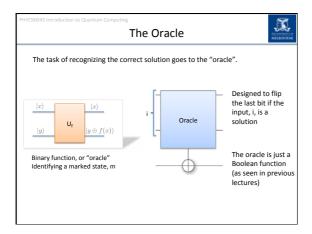
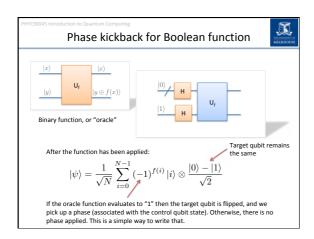


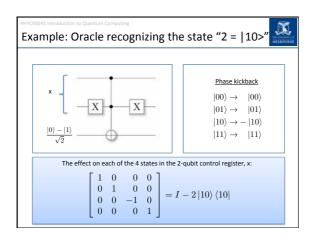
PHYC90045 Introduction to Quantum Computing  Quantum search — Grover's problem	MELBOARDE
Given an black box (oracle), $U_p$ which computes the function: $f:\{0,1\}^n \to \{0,1\}$	
Find an $x$ s.t. $f(x) = 1$	



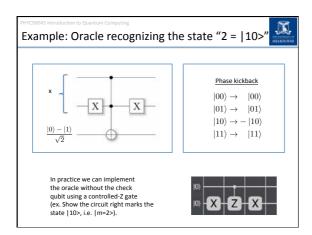


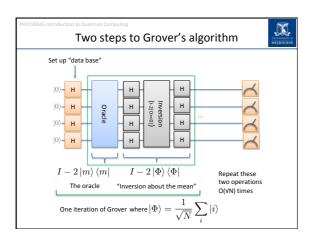


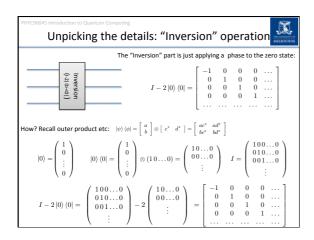


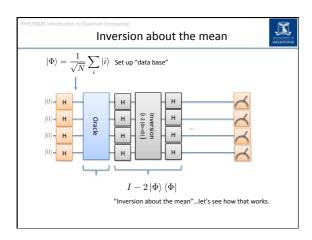


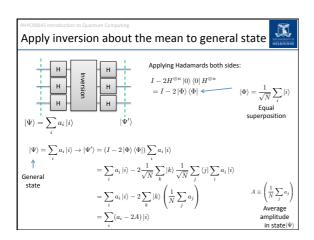
PHYC90045 Introduction to Quantum Computing  The marked state	PER CONTRACT OF MELEONIENE		
Initially in Grover's algorithm, we will be searching for a <i>single (integer)</i> solution, <b>m</b> . In that case the effect of the oracle on the control register is:			
$I-2\leftert m ight angle \left\langle m ightert$ (in decimal	ket notation)		
As a matrix: $ \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}  $ -1 in the minor of the	<sup>th</sup> position		
Here, as in future slides, we are only writing out the control qubits (in qubits only).	this case 2		



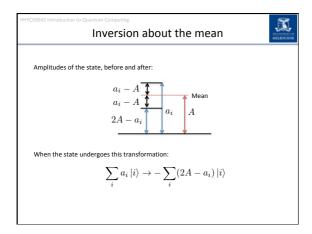


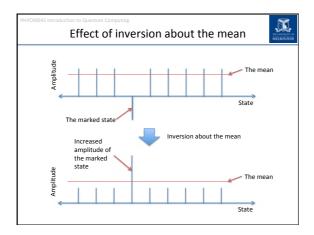




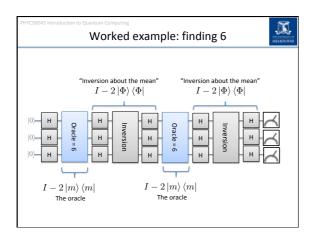


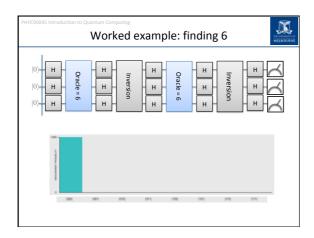
PHYC90045 Introduction to Quantum Computing  Inversion about the mean		
Consider a general state. The resulting amplitude from the "Inversion about the mean" step is:		
$\sum_i a_i \ket{i}  o \sum_i (a_i - 2A) \ket{i}$ Original amplitude Average amplitude		
In practice on the QUI		

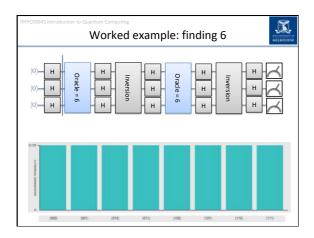


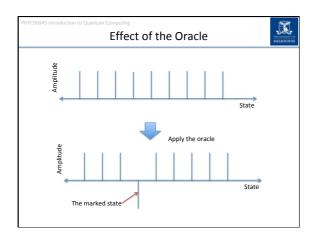


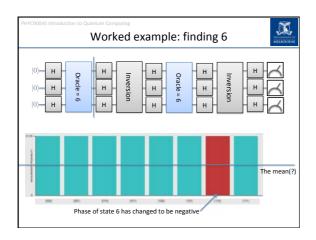
PHYC90045 Introduction to Quantum Computing  Interactive Example	MELECURAL
https://codepen.io/samtonetto/full/BVOGmW	

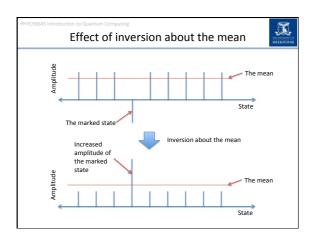


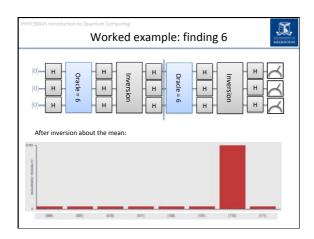


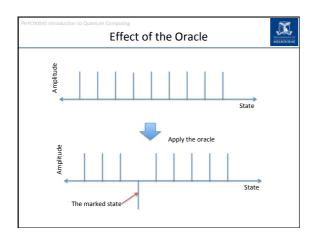


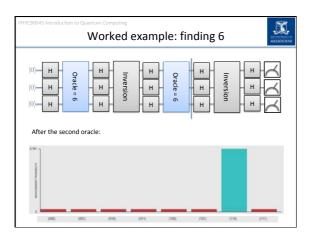


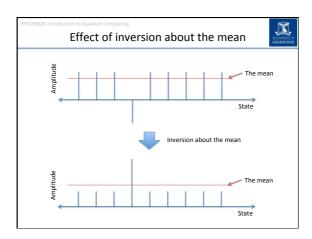


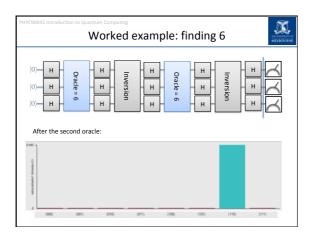


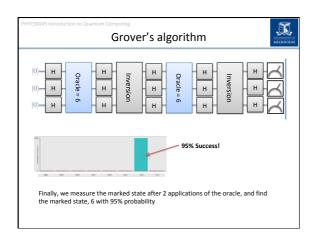


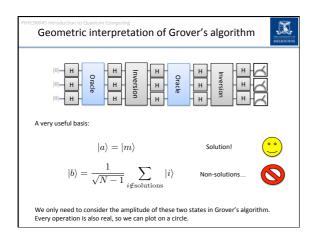


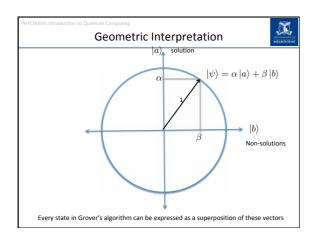




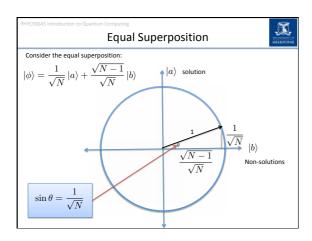


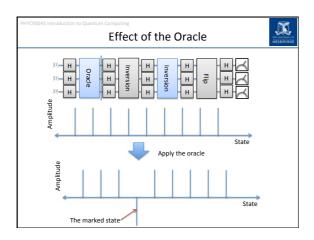


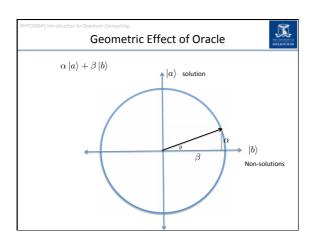


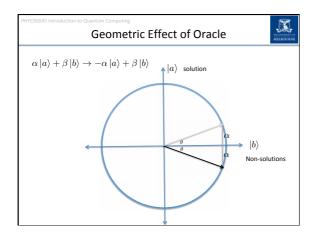


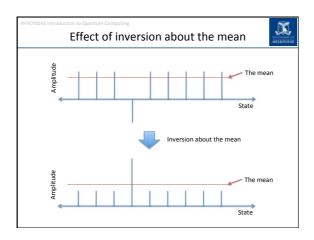
PHYC90045 Introduction to Quantum C	Equal superposition	MILEOUENE
0)	nversion  H H H H H H H H H H H H H H H H H H H	
Equal superposition state:	$\begin{split}  \Phi\rangle &= \frac{1}{\sqrt{N}} \sum_i  i\rangle \\ &= \frac{1}{\sqrt{N}}  a\rangle + \frac{\sqrt{N-1}}{\sqrt{N}}  b\rangle \end{split}$	
a angle =	$ b\rangle = \frac{1}{\sqrt{N-1}} \sum_{i \notin \text{solutions}}  i\rangle$	

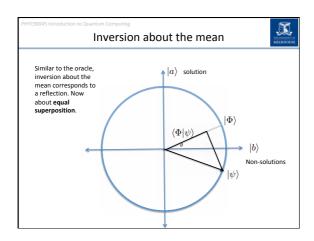


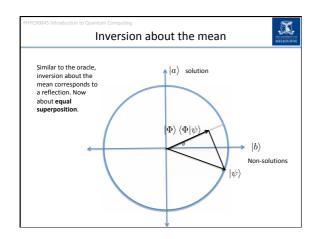


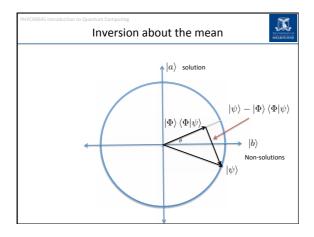


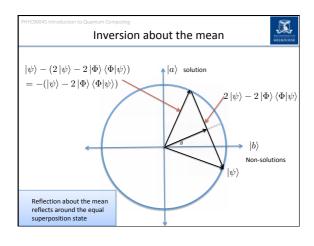


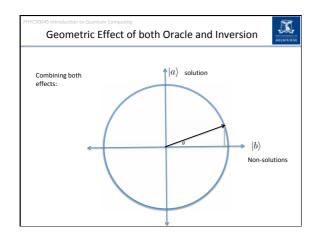


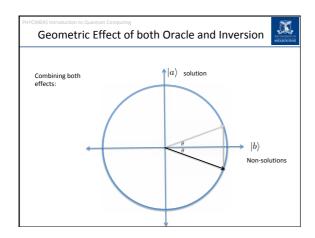


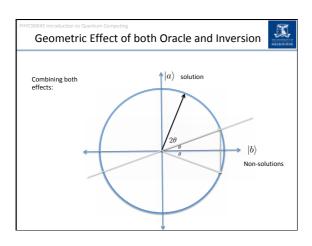


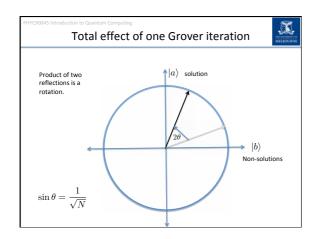


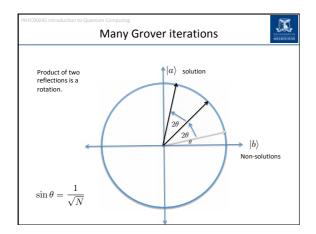




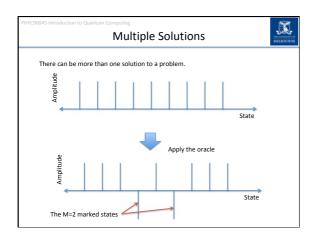


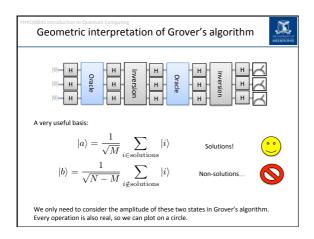


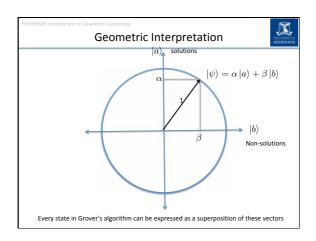


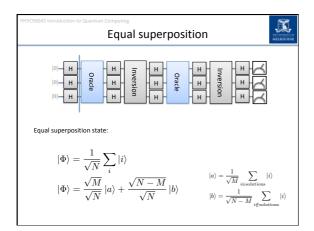


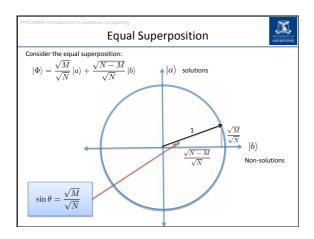
PHYC90045 Introduction to Quantum Computing	T
How many iterations required?	MELIOUENE
$\sin\theta = \frac{1}{\sqrt{N}}$ For small angles, $\theta \approx \frac{1}{\sqrt{N}}$	
After n iterations, we rotate to have only marked solutions: $(2n+1)\theta=\frac{\pi}{2}$ $n\approx\frac{\pi}{4}\sqrt{N}$	
The number of steps, n, required scales as O(VN), and not with N as it would classically.	
This is a "polynomial" rather than an "exponential" speedup.	

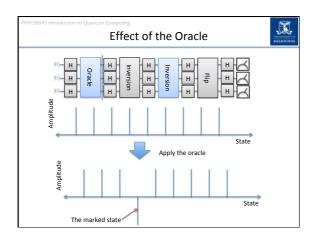


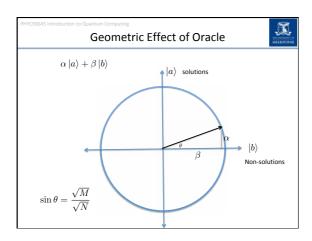


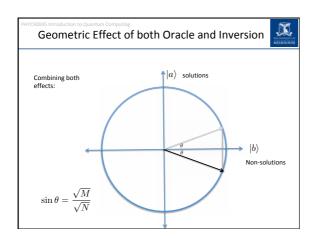


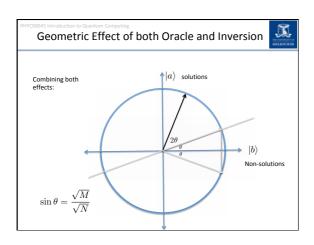


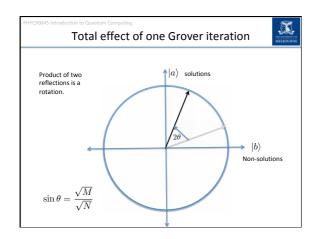


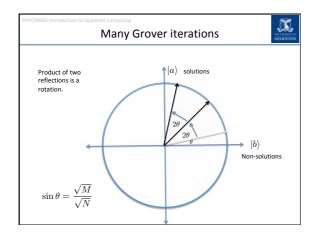












PHYC90045 Introduction to Quantum Computing  How many iterations required?	MELECURA
$\sin  heta = rac{\sqrt{M}}{\sqrt{N}}$ For small angles, $ heta pprox rac{\sqrt{M}}{\sqrt{N}}$	
After n iterations, we rotate to have only marked solutions: $(2n+1)\theta=\frac{\pi}{2}$ $n\approx\frac{\pi\sqrt{N}}{4\sqrt{M}}$	
Having multiple solutions is faster than searching for a single marked solution.	

