

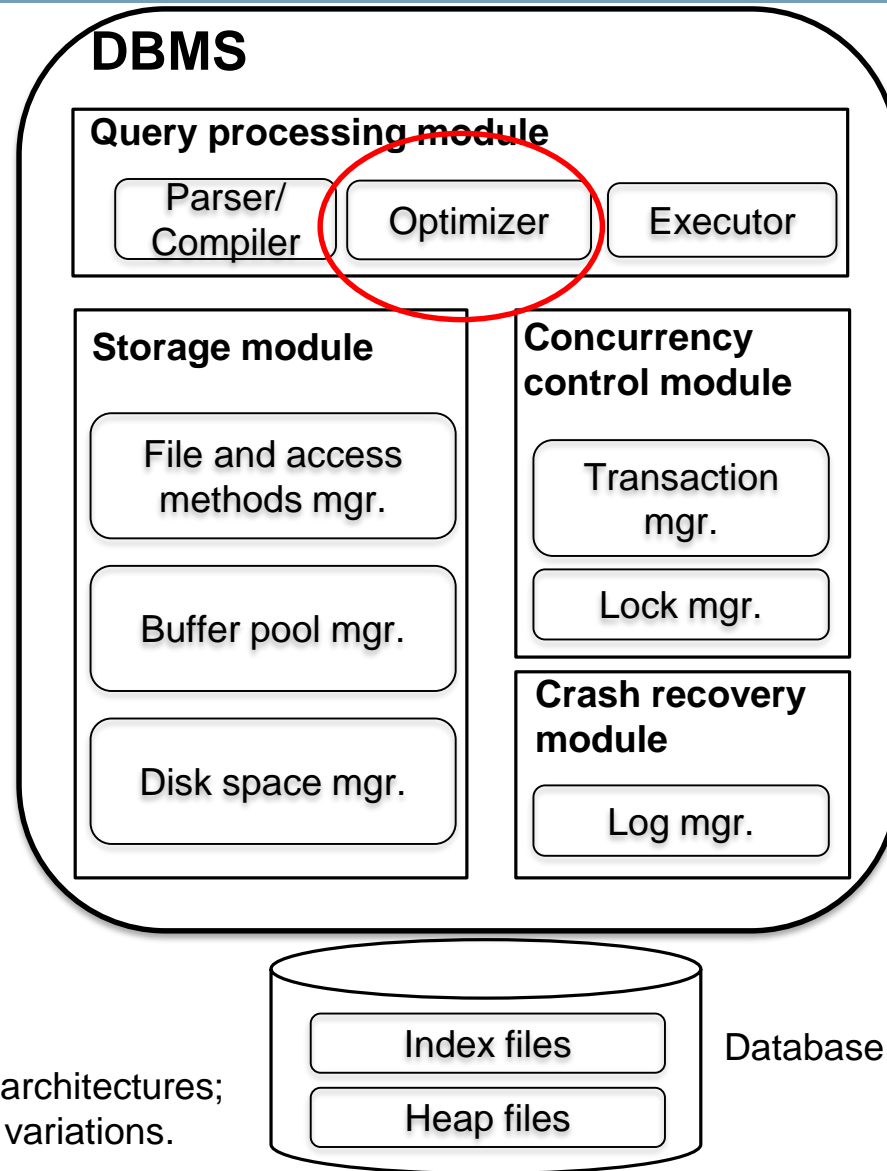


INFO20003 Database Systems

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Lecture 13
Query Optimization Part I

Remember this? Components of a DBMS



**TODAY &
Next time**

This is one of several possible architectures; each system has its own slight variations.



REEDUCATION

- Overview
- Query optimization
- Cost estimation

Readings: Chapter 12 and 15, Ramakrishnan & Gehrke, Database Systems



- Implementation of single Relational Operations
- Choices depend on indexes, memory, stats,...
- Joins
 - Blocked nested loops:
 - simple, exploits extra memory
 - Indexed nested loops:
 - best if one relation small and one indexed
 - Sort/Merge Join
 - good with small amount of memory, bad with duplicates
 - Hash Join
 - fast (enough memory), bad with skewed data



- Typically many methods of executing a given query, all giving same answer
- Cost of alternative methods often **varies enormously**
- Desirable to find a low-cost execution strategy
- **We will cover:**
 - Relational algebra equivalences
 - Cost estimation
 - Result size estimation and reduction factors
 - Statistics and Catalogs
 - Enumerating alternative plans
- Will focus on “System R”-style optimizers

Query

```
Select *  
From Blah B  
Where B.blah = "foo"
```

Query Parser

Query Optimizer

Plan
Generator

Plan Cost
Estimator

Query Plan Evaluator

Usually there is a
heuristics-based
rewriting step before
the cost-based steps.

Catalog Manager

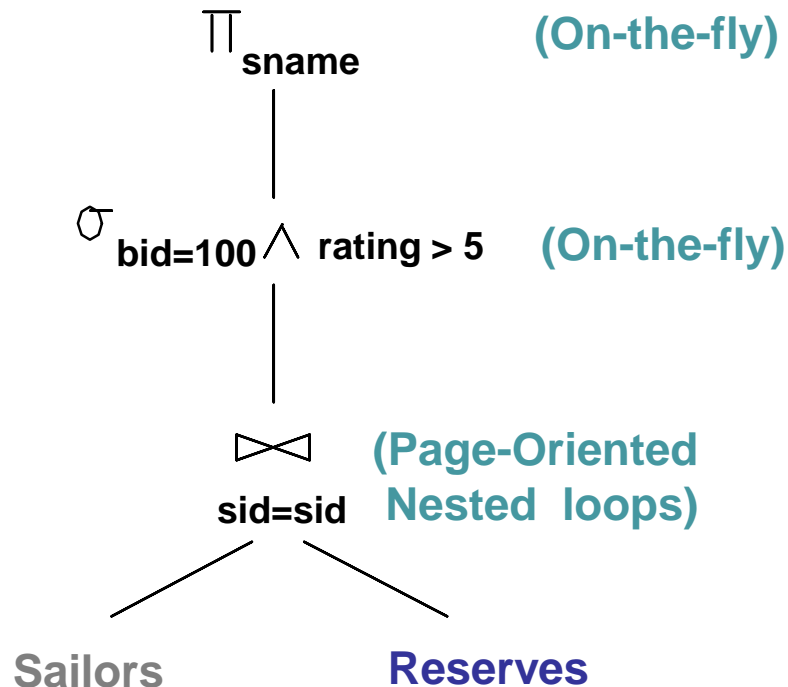
Schema

Statistics



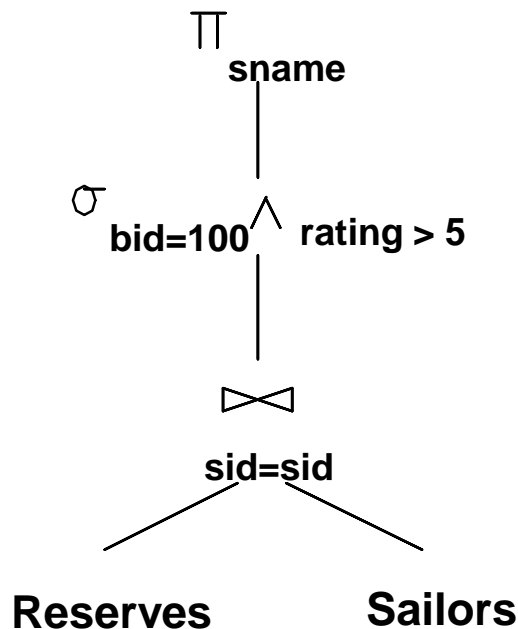
- A tree, with relational algebra operators as nodes
- Each operator labeled with choice of algorithm

Plan:



* By convention, *outer* is on *left*.

- A note on implementation:



- Relational operators at nodes support uniform *iterator* interface:
Open(), get_next(), close()
- **Unary Operators** – On *Open()* call *Open()* on child
- **Binary Operators** – call *Open()* on left child then on right

Query:

```
SELECT S.sname  
FROM Reserves R, Sailors S  
WHERE R.sid=S.sid AND  
R.bid=100 AND S.rating>5
```

To optimize:

1. Query first broken into “blocks”
2. Each block converted to relational algebra
3. Then, for each block, several alternative **query plans** are considered
4. Plan with lowest **estimated cost** is selected



Sailors (*sid*: integer, *sname*: string, *rating*: integer, *age*: real)
Reserves (*sid*: integer, *bid*: integer, *day*: dates, *rname*: string)
Boats (*bid*: integer, *bname*: string, *color*: string)



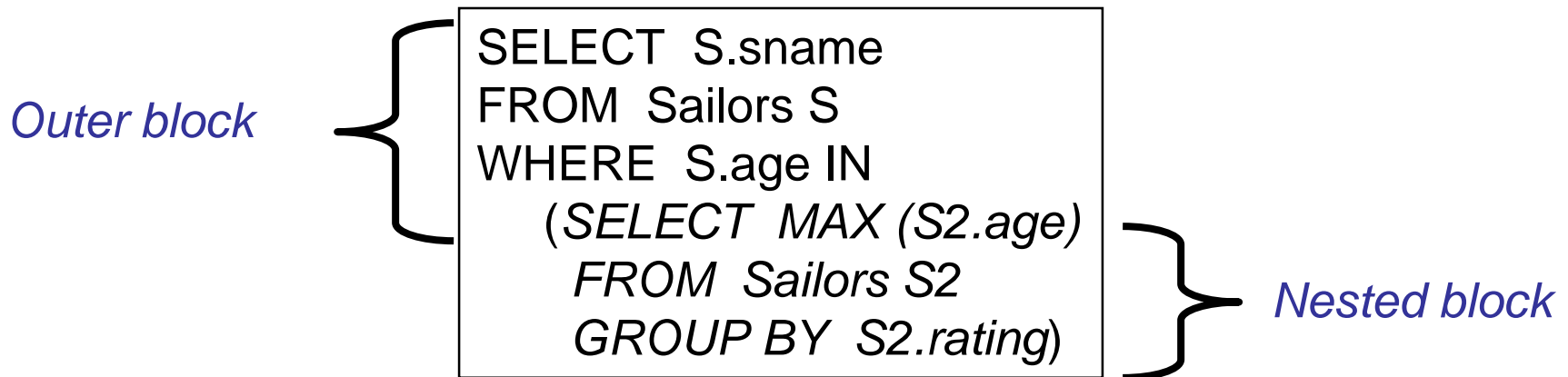
- Overview
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Readings: Chapter 15, Ramakrishnan & Gehrke, Database Systems



Step 1: Break query into Query Blocks

- Query block = unit of optimization
- Nested blocks are usually treated as calls to a subroutine, made once per outer tuple
(This is an over-simplification, but serves for now)





Step 2: Converting query block into relational algebra expression

Query:

```
SELECT S.sid  
FROM Sailors S, Reserves R, Boats B  
WHERE S.sid = R.sid AND R.bid = B.bid AND B.color = "red"
```

Relational algebra:

$$\pi_{S.sid}(\sigma_{B.color = \text{"red"}}(Sailors \bowtie Reserves \bowtie Boats))$$



- For each sailor with the highest rating (over all sailors), and at least two reservations for red boats, find the sailor id and the earliest date on which the sailor has a reservation for a red boat

```
SELECT S.sid, MIN (R.day)
FROM Sailors S, Reserves R, Boats B
WHERE S.sid = R.sid AND R.bid = B.bid AND B.color = "red"
AND S.rating = ( SELECT MAX (S2.rating) FROM Sailors S2)
GROUP BY S.sid
HAVING COUNT (*) >= 2
```



```
SELECT S.sid, MIN (R.day)
FROM Sailors S, Reserves R, Boats B
WHERE S.sid = R.sid AND R.bid = B.bid AND B.color = "red"
AND S.rating = ( SELECT MAX (S2.rating) FROM Sailors S2)
GROUP BY S.sid
HAVING COUNT (*) >= 2
```

π S.sid, MIN(R.day)
(HAVING COUNT(*)>2 (
GROUP BY S.Sid (
 σ B.color = "red" ^ S.rating = val(
Sailors \bowtie Reserves \bowtie Boats))))

Inner Block



- Core of every query is a **select-project-join (SPJ)** expression
- Other aspects, if any, carried out on result of SPJ core:
 - Group By (either sort or hash)
 - Having (apply filter on-the-fly)
 - Aggregation (easy once grouping done)
 - Order By (sorting is the name of the game)
- Not much room to exploit equivalences on non-SPJ parts
- Focus on optimizing SPJ core

- *Selections*: $\sigma_{c_1 \wedge \dots \wedge c_n}(R) \equiv \sigma_{c_1} \left(\dots \left(\sigma_{c_n}(R) \right) \right)$ (*Cascade*)
 $\sigma_{c_1} \left(\sigma_{c_2}(R) \right) \equiv \sigma_{c_2} \left(\sigma_{c_1}(R) \right)$ (*Commute*)
- *Projections*: $\pi_{a_1}(R) \equiv \pi_{a_1} \left(\dots \left(\pi_{a_n}(R) \right) \right)$ (*Cascade*)
 a_i is a set of attributes of R and $a_i \subseteq a_{i+1}$ for $i = 1 \dots n - 1$
- These equivalences allow us to ‘push’ selections and projections ahead of joins.



$$\sigma_{\text{age} < 18 \wedge \text{rating} > 5} (\text{Sailors})$$

$$\longleftrightarrow \sigma_{\text{age} < 18} (\sigma_{\text{rating} > 5} (\text{Sailors}))$$

$$\longleftrightarrow \sigma_{\text{rating} > 5} (\sigma_{\text{age} < 18} (\text{Sailors}))$$

~~$$\pi_{\text{age}, \text{rating}} (\text{Sailors}) \longleftrightarrow \pi_{\text{age}} (\pi_{\text{rating}} (\text{Sailors})) \quad (?)$$~~

$$\pi_{\text{age}, \text{rating}} (\text{Sailors}) \longleftrightarrow \pi_{\text{age}, \text{rating}} (\pi_{\text{age}, \text{rating}, \text{sid}} (\text{Sailors}))$$



- A projection commutes with a selection that only uses attributes retained by the projection

$$\pi_{\text{age, rating, sid}} (\sigma_{\text{age} < 18 \wedge \text{rating} > 5} (\text{Sailors})) \\ \longleftrightarrow \sigma_{\text{age} < 18 \wedge \text{rating} > 5} (\pi_{\text{age, rating, sid}} (\text{Sailors}))$$

$$R \bowtie (S \bowtie T) \equiv (R \bowtie S) \bowtie T \quad (\textit{Associative})$$

$$(R \bowtie S) \equiv (S \bowtie R) \quad (\textit{Commutative})$$

* These equivalences allow us to choose different join orders



- Converting selection + cross-product to join

$$\sigma_{S.sid = R.sid} (\text{Sailors} \times \text{Reserves})$$

$$\leftrightarrow \text{Sailors} \bowtie_{S.sid = R.sid} \text{Reserves}$$

- Selection on just attributes of S commutes with $R \bowtie S$

$$\sigma_{S.age < 18} (\text{Sailors} \bowtie_{S.sid = R.sid} \text{Reserves})$$

$$\leftrightarrow (\sigma_{S.age < 18} (\text{Sailors})) \bowtie_{S.sid = R.sid} \text{Reserves}$$

- We can also “push down” projection (*but be careful...*)

$$\pi_{S.sname} (\text{Sailors} \bowtie_{S.sid = R.sid} \text{Reserves})$$

$$\leftrightarrow \pi_{S.sname} (\pi_{sname, sid} (\text{Sailors}) \bowtie_{S.sid = R.sid} \pi_{sid} (\text{Reserves}))$$



QUESTIONS

1. $R \times S = S \times R$

2. $(R \times S) \times T = R \times (S \times T)$

3. $\sigma_p(R \cup S) = \sigma_p(R) \cup S$

4. $R \cup S = S \cup R$

5. $\sigma_p(R - S) = R - \sigma_p(S)$

6. $R \cup (S \cup T) = (R \cup S) \cup T$

7. $\sigma_{R.p \vee S.q} (R \bowtie S) =$

$$[(\sigma_p R) \bowtie S] \cup [R \bowtie (\sigma_q S)]$$



REWRITING

- Modern DBMS's may **rewrite** queries before the optimizer sees them
- Main purpose: **de-correlate** and/or **flatten** nested subqueries
- De-correlation:
 - Convert correlated subquery into uncorrelated subquery
- Flattening:
 - Convert query with nesting into query w/o nesting

Example: Decorrelating a Query

```
SELECT S.sid  
FROM Sailors S  
WHERE EXISTS  
  (SELECT *  
    FROM Reserves R  
    WHERE R.bid=103  
    AND R.sid=S.sid)
```

Equivalent uncorrelated query:

```
SELECT S.sid  
FROM Sailors S  
WHERE S.sid IN  
  (SELECT R.sid  
    FROM Reserves R  
    WHERE R.bid=103)
```

* **Advantage**: nested block only needs to be executed **once** (rather than once per S tuple)



Example: “Flattening” a Query

```
SELECT S.sid  
FROM Sailors S  
WHERE S.sid IN  
    (SELECT R.sid  
    FROM Reserves R  
    WHERE R.bid=103)
```

Equivalent non-nested query:

```
SELECT S.sid  
FROM Sailors S, Reserves R  
WHERE S.sid=R.sid  
    AND R.bid=103
```

* **Advantage:** can use a join algorithm + optimizer can select among join algorithms & reorder freely



RELEVANCE

- Before optimizations, queries are flattened and de-correlated
- Queries are first broken into blocks
- Blocks are converted to relational algebra expressions
- Equivalence transformations are used to push down selections and projections



Agenda

- Overview
- Query optimization
- Cost estimation

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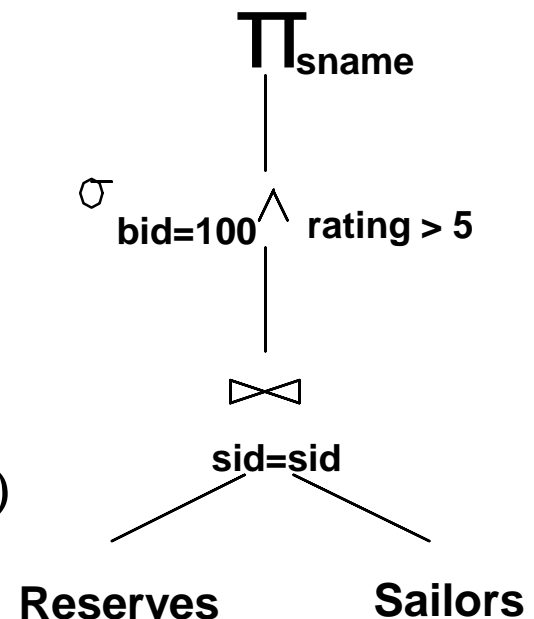
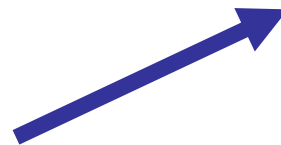


1. Query first broken into “blocks”
2. Each block converted to relational algebra
3. Then, for each block, several alternative **query plans** are considered
4. Plan with lowest **estimated cost** is selected

```
SELECT S.sname
FROM Reserves R, Sailors S
WHERE R.sid=S.sid AND
      R.bid=100 AND S.rating>5
```



$\pi_{(sname)} \sigma_{(bid=100 \wedge rating > 5)} (Reserves \bowtie Sailors)$





Queries

```
Select *  
From Blah B  
Where B.blah = "foo"
```

Query Parser

Query Optimizer

Plan
Generator

Plan Cost
Estimator

Usually there is a
heuristics-based
rewriting step before
the cost-based steps.

Catalog Manager

Schema

Statistics

Query Plan Evaluator

Steps 3 & 4





1. For a given query, **what plans are considered?**
 - Algorithm to search plan space for cheapest (estimated) plan.
2. How is the **cost of a plan estimated?**
 - **Ideally:** Want to find best plan.
 - **Reality:** Avoid worst plans!



- Impact:
 - Most widely used currently; works well for < 10 joins
- Cost estimation:
 - Very inexact, but works okay in practice
 - Statistics, maintained in system catalogs, used to estimate cost of operations and result sizes
 - Considers combination of CPU and I/O costs
 - More sophisticated techniques known now
- Plan Space: Too large, must be pruned
 - Only the space of *left-deep plans* is considered
 - Cross products are avoided



Sailors (*sid*: integer, *sname*: string, *rating*: integer, *age*: real)
Reserves (*sid*: integer, *bid*: integer, *day*: dates, *rname*: string)

- Reserves:
 - Each tuple is 40 bytes long, 100 tuples per page, 1000 pages, 100 distinct bids
- Sailors:
 - Each tuple is 50 bytes long, 80 tuples per page, 500 pages, 10 Ratings, 40.000 sids



- For each plan considered, must estimate cost:
 - Must *estimate cost* of each operation in plan tree.
 - Depends on input cardinalities
 - We've already discussed how to estimate the cost of operations (sequential scan, index scan, joins, etc.)
 - Must *estimate size of result* for each operation in tree!
 - Use information about the input relations
 - For selections and joins, assume independence of predicates
 - In System R, cost is boiled down to a single number consisting of $\#I/O + \textit{factor} * \#CPU \text{ instructions}$



- Need information about the relations and indexes involved.
Catalogs typically contain at least:
 - # tuples (**NTuples**) and # pages (**NPages**) per relation
 - # distinct key values (**NKeys**) for each index
 - low/high key values (**Low/High**) for each index
 - Index height (**IHeight**) for each tree index
 - # index pages (**INPages**) for each index
- Statistics in catalogs are updated periodically
 - Updating whenever data changes is too expensive; lots of approximation anyway, so slight inconsistency is OK
- More detailed information (e.g., histograms of the values in some field) are sometimes stored

SELECT clause

```
SELECT attribute list  
FROM relation list  
WHERE term1 AND ... AND termk
```

- Consider a query block:
- Maximum # tuples in result is the product of the cardinalities of relations in the FROM clause
- *Reduction factor (RF)* associated with each *term* reflects the impact of the *term* in reducing result size
- RF is usually called “selectivity”

- *Result cardinality* = Max # tuples * product of all RF's
(Implicit assumption that **values are uniformly distributed**
and **terms are independent!**)
- Term *col=value* (given index *I* on *col*)
$$RF = 1/NKeys(I)$$
- Term *col>value*
$$RF = (High(I)-value)/(High(I)-Low(I))$$
- *Note: if missing indexes, assume $RF = 1/10$*



- Q: Given a join of R and S, what is the range of possible result sizes (in #of tuples)?
 - Hint: what if $R_cols \cap S_cols = \emptyset$?
 - $R_cols \cap S_cols$ is a key for R (and a Foreign Key in S)?

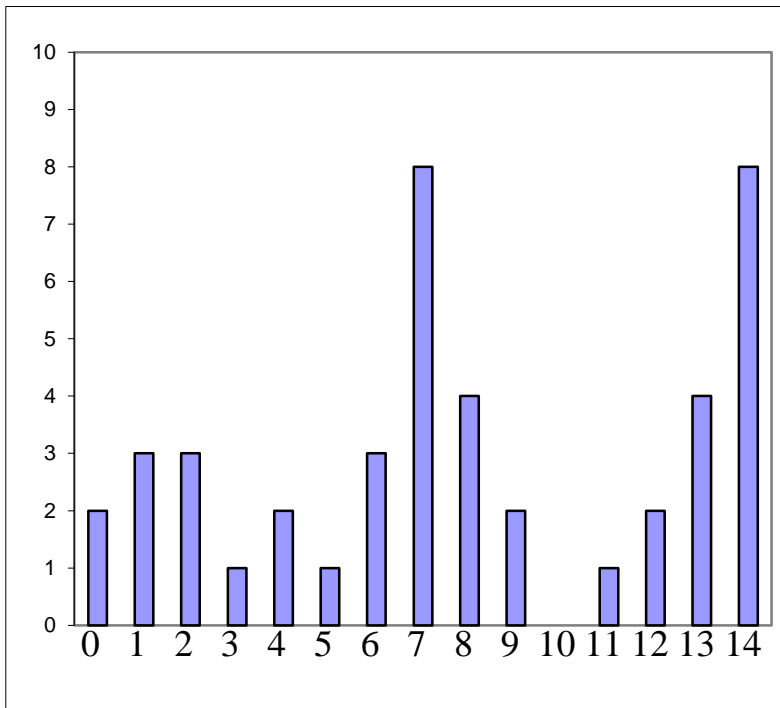


- General case: $R_cols \cap S_cols = \{A\}$ (and A is key for neither)
 - If $NKeys(A, \mathbf{S}) > NKeys(A, \mathbf{R})$
 - Assume S values are a superset of R values, so each R value finds a matching value in S
 - Estimate each tuple r of R generates $NTuples(S)/NKeys(A, S)$ result tuples, so...
$$est_size = NTuples(R) * NTuples(S)/NKeys(A, \mathbf{S})$$
 - Else, if $NKeys(A, \mathbf{R}) > NKeys(A, \mathbf{S})$... symmetric argument, yielding:
$$est_size = NTuples(R) * NTuples(S)/NKeys(A, \mathbf{R})$$
 - Overall:
$$est_size = NTuples(R) * NTuples(S) / \text{MAX}\{NKeys(A, \mathbf{S}), NKeys(A, \mathbf{R})\}$$

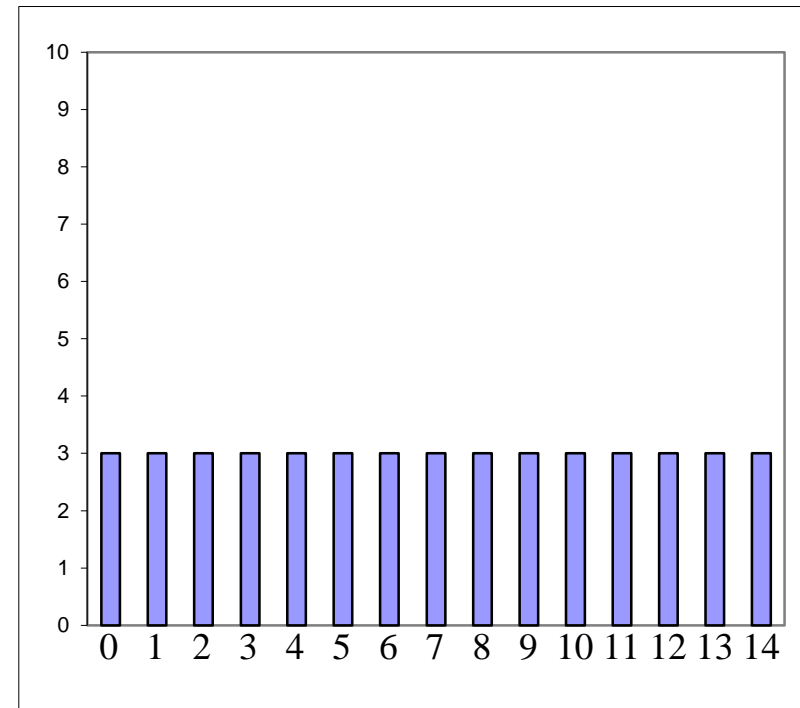


- Assuming uniform distribution is rather crude

Distribution D



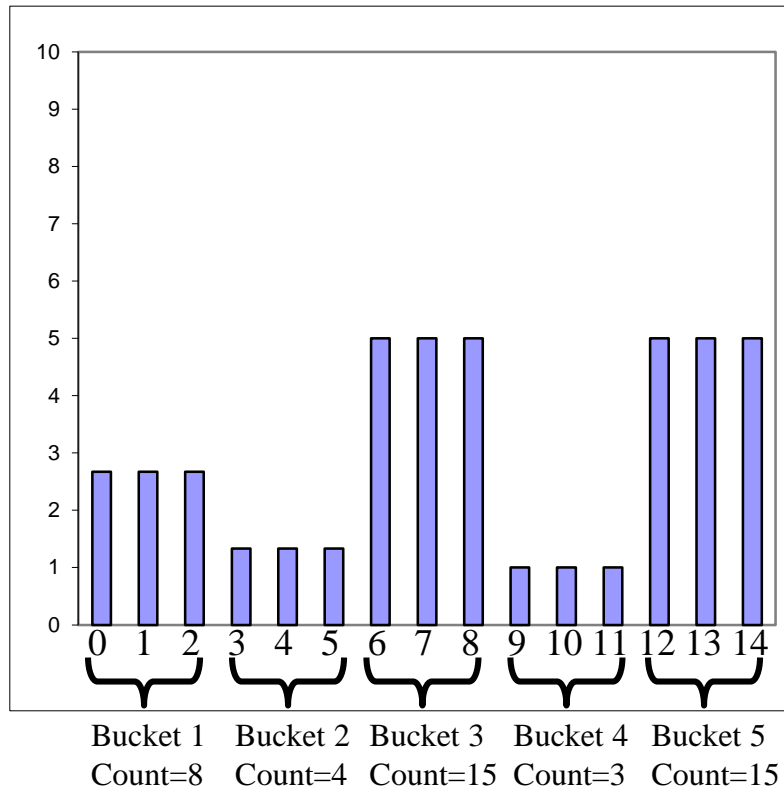
Uniform distribution approximating D



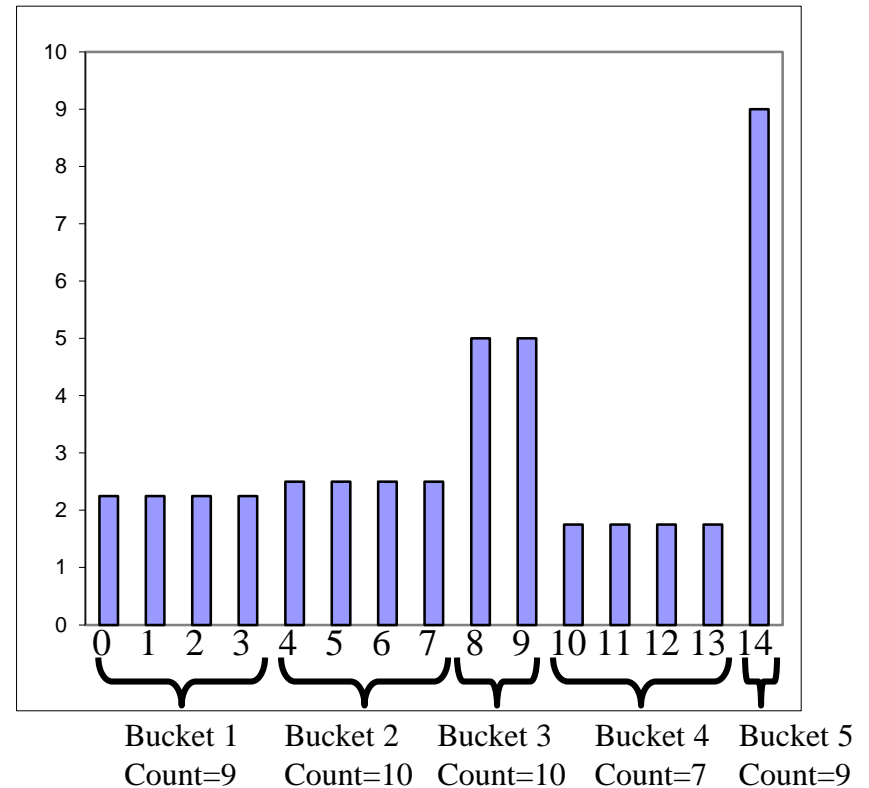


- For better estimation, use a *histogram*

Equiwidth histogram



Equidepth histogram





- The costs of possible strategies vary widely
- Estimate result sizes using statistics
- Estimate costs of each operator
- Focus on optimizing select-project-join (SPJ) blocks



REVISION

- What is query optimization/steps?
- Equivalence classes
- Result size/cost estimation
- Important for Assignment 3 as well



- Query optimization Part II
 - Plan enumeration