lec02

A Problem

1ethod 0

Homework

Homework

COMP10002

Semester One, 2017

Why Algorithms?!

A simple computational problem

Simply a matter of programming

Making it go faster

Adding algorithmic design

Homework

A Problem

Method 0

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Given: A sequence S of n symbols

Problem: Find all locations in S at which repeated subsequences of length m or more appear.

```
Try
```

fat.rat.eat.bat.cat.eat.fat.rat.

```
with m = 7?
```

findrepeats0 7 < test1.txt n = 32m = 70 24: fat.rat 1 25: at.rat.

5 17: at.eat.

count = 3



Method 0:

```
read the sequence S for i=0 to n-m do for j=i+1 to n-m do compare m characters starting at S[i] and S[j] if all m characters are the same then write an output line
```

Works just fine.

Until you give it non-trivial data.

Look at those loops.

To execute the program, takes $n \times n \times m = n^2 m$ individual character comparisons.

When n = 1,000 and m = 10, gives $n^2m = 10^7$ operations, so just fractions of a second.

But when n=1,000,000 and m=100, means $n^2m=10^{14}$ operations. No longer fractions of a second. No longer even seconds or minutes.

Method 0

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Why test the full m characters every time, can surely do less work on average than that? Leads to Method 1:

```
read the sequence S
for i = 0 to n - m do
  for i = i + 1 to n - m do
    compare at most m characters starting at S[i] and S[j],
         stopping as soon as any discrepancy is noted
    if no differences are in m characters then
       write an output line
```

This makes it significantly faster.

Worst case is still n^2m operations (what kind of sequence?)

But on average, each check fails very early; now spend kn^2 operations for a sequence of n characters, where $k \ll m$ is a small constant.

Faster, but still not fast enough to be "scalable".

For n = 1,000,000 gives rise to 10^{12} + operations. And that will still be a thousand or more seconds.

Method 0

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Algorithms are the aspect of computing that require science.

There will be a variety of ways of achieving any given goal, with subtle and not-so-subtle differences between them.

It is often possible to trade memory space for execution time; and exploit selective pre-computation.

Sophisticated data structures are chosen to match the exact mix of operations that need to be supported.



```
read the sequence S for i=0 to n-m do P[i] \leftarrow i sort P[i] based on S[P[i]], S[P[i]+1], \ldots for i=0 to n-m do compare at most m characters starting at S[P[i]] and S[P[i+1]] if no differences are found then write an output line
```

Finds one instance of each repetition; easy modification finds all of them.

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Sorting n items takes fewer than $2n \log n$ comparisons.

In a simple implementation, each step is a string comparison over (still never more than) m characters.

So for n = 1,000,000 and m = 100 now have fewer than $\approx 2mn \log n = 4 \times 10^9$ operations.

That should take just a second or so!

One prepared earlier...

n = 1,000,000,000

Method	0	1	2
n = 10,000	1.0 s	0.1 s	0.005 s
n = 100,000	94 s	11.2 s	0.04 s
n = 1,000,000		1102 s	0.47 s
n = 10,000,000			7.50 s
n = 100,000,000			113 s
n = 100,000,000			113 5

(Using m=25 and W&P up to 1M, then m=250 and WSJ).

35 y 24 m

can make estimates

3 m

Are we there yet?

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Method 2 can be improved if a tailored sorting mechanism is used.

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Using a ternary Quicksort (a couple of hours of implementation effort), Method 3 runs around 50% faster, and takes 50 seconds for 100 MB.

Using an explicit method for building a suffix array (perhaps a couple of days of implementation effort) might give rise to another halving.

Method 0

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Careful tuning and hand optimization might halve it again, to maybe 10-15 seconds for 100 MB.

And would mean that a terabyte of data can be processed in 4 days.

No, not really.

The problem now is that sorting requires random access into the underlying string, and so each processing node would have to store the whole string, plus part of the suffix array.

Ooops!

Setting up a successful parallel computation requires a deep understanding of what the computation is doing and how it can be parallelized. A Problem

Method 0

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Method 4 uses more (disk) space, but all processing is sequential, making it amenable to a parallel implementation over a cluster.

Method 1
Method 2
Homework

A Problem

Only a little more complex, and executes fast enough: with n=100,000,000 and m=250, requires 40 seconds; with estimated time for $n=10^9$ of 7 minutes, and for $n=10^{12}$ of 7 days.

Or, 10 minutes when spread over 1,024 processors.

As an invention, Method 4 is patentable and/or publishable!

Method 0

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Homework

Given: A sequence S of n symbols.

Problem: Determine if there is any value in S that occurs more than n/2 times, and if so, what the value is.

Target: Worst case linear time, constant additional space.

- Real data, and a precise description of the transformation or processing that must be performed against it; plus
- An understanding of what the end application/benefit will be from the desired techniques; plus
- Smart students to work with us.

Algorithms are Fun!

A Problem

Method 0

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