

## Coursework 1

This coursework relates to the Hopfield network. In the `auto` folder you will find programmes `seven_segment.jl` and `seven_segment.py`. These contain a function for converting an 11-component vector of ones and -1's into an old-fashioned seven-segment digit<sup>1</sup> and a number: the first seven digits correspond to the seven-segment display and the remaining four code for the number in a sort of binary where the zeros have been replaced with -1. It also contains three patterns: one, three and eight.

The goal of this coursework is to extend one or other of these programmes to include a Hopfield network to store these three patterns using the formula for  $w_{ij}$  when  $i \neq j$

$$w_{ij} = \frac{1}{N} \sum_a x_i^a x_j^a \quad (1)$$

where  $a$  labels patterns,  $x_i^a$  is the activation of the  $i$ th node in the  $a$ th pattern and  $N$  is the number of patterns.  $w_{ii} = 0$ .

In the code there are also two test patterns, your programme should update these synchronously until convergence and print out the patterns at each iteration.

This coursework is intended to check you understand Hopfield networks, you are not being asked to do anything over elaborate beyond that. In summary you should:

- Create a weight matrix of  $w_{ij}$ s.
- Fix the weight values to store the three patterns.
- Write a function to evolve the network according to the McCulloch-Pitts formula; this should be done synchronously so all the nodes are updated at each timestep.
- For each of the two test patterns, evolve the patterns until they stop moving, printing the pattern at each step.

---

<sup>1</sup>[https://en.wikipedia.org/wiki/Seven-segment\\_display](https://en.wikipedia.org/wiki/Seven-segment_display)

## COMSM20127

Add to the above a function to calculate the energy of a configuration

$$E = -\frac{1}{2} \sum_{ij} x_i w_{ij} x_j \quad (2)$$

and print out the energy of the three learned patterns, of the test patterns and any patterns formed as the patterns are updated.

## Submission instructions

Upload your programme on safe; if your programme does what it is supposed to do you will get full marks. The reason there are two programmes, `seven_segments.py` and `seven_segments.jl` is to give you a choice of languages, it is only expected you will submit one piece of code in one of the two languages.