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Assignment # 1

Course Title: Computational methods of Electronic structure theory (CMEST)

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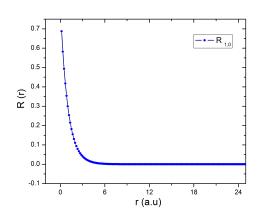
Solution to Hydrogen atom by LAPACK subroutines

1 Hydrogen atom radial plot

Six lowest hydrogen energy levels are:

n	l	Energy (a.u)
1	0	-0.4988
2	0	-0.1248
2	1	-0.1251
3	0	-0.0555
3	1	-0.0556
3	2	-0.0312

The corresponding figures are plotted below.



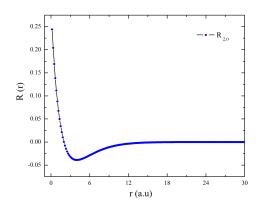
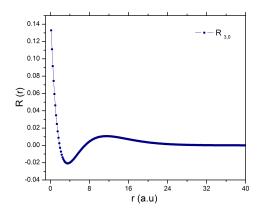


Figure 1.1:



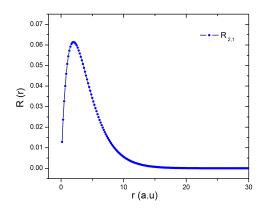
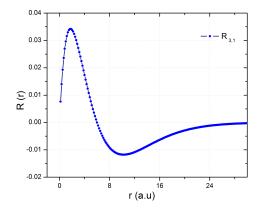


Figure 1.2:



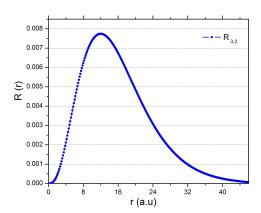


Figure 1.3:

1 Appendix 4

Appendix

The difference among these solvers dsyev, dsbev and dstebz resides in the execution time. In case for dstebz, the execution time is faster as seen by local CPU_time. Since, in this routine eigenvalues can be called in the given range, which implies no need for extra calculation. If compared to dsbev subroutine the diagonal and sub or super-diagonal term are stored in another matrix of these dimensions which is a little faster. Lastly, dsyev just take the given matrix and solves for eigenvalues and optionally eigenvectors. Over here it doesn't do any extra effort of assigning matrix to other dimension and solve. So, if by execution time (by calling *CPU time subroutine*) it could be stated in this way

dstebz < dsbev < dsyev

Exercise # 1: DSYEV.f90 subroutine

Functions/Subroutines:

```
call dsyev (JOBZ, UPLO, N, A, LDA, W, WORK, LWORK, INFO)
```

DSYEV computes the eigenvalues and, optionally, the left and/or right eigenvectors for symmetric matrices.

```
program SE
2
    implicit none
    double precision
3
                                          :: t, start_time, stop_time
   double precision, parameter
                                          :: rmax = \overline{50}
4
                                          :: i , j , k , N , M , INFO , LWORK, l :: r , W , WORK
5
   integer
6
   {\bf double\ precision}\ ,\ {\bf dimension}\ (:)\ ,\ {\bf allocatable}
   double precision, dimension(:,:), allocatable :: H
7
    intrinsic INT, MIN, MAX
9
    \mathbf{print}*, "Enter the size of a grid N > 2 " ; \mathbf{read}*, N
10
   \mathbf{print}*, "Enter the value for angular momentum l= " ; \mathbf{read}*, l
11
12
13
   allocate(WORK(LWORK), r(N-1), H(N-1, N-1), W(N))
14
    15
16
17
   t = rmax/dble(N)
   r = 0d0
18
19
   H = 0d0
20
   21
    22
23
   do i = 1, N-2
    r(i) = i*t 
 H(i,i) = 2*(1 - (1/r(i))*t*t + (dble(1)*(dble(1)+1)) &
24
25
                   *(1/(r(i)**2))*((t*t)/2)
26
27
    H(i+1,i) = -1d0
28
    H(i, i+1) = -1d0
29
   enddo
   H(N-1,N-1) = 2*(1-(1/(r(N-2)+t)*t*t) + (dble(1)*(dble(1)+1))* &
30
31
                  (1/(r(N-2)+t)**2)*((t*t)/2)
32
   H = H/(2*t**2)
33
   34
35
36
    call cpu_time(start_time)
    call dsyev ('V', 'L', M, H, M, W, WORK, LWORK, INFO)
37
    call cpu time(stop_time)
38
    if(INFO.gt.0) then
39
40
    write(*,*)'The algorithm failed to compute eigenvalues.'
41
    stop
    endif
42
43
44
    print*, ":: The Eigenvalues for l = ", l
45
    write(*, '(9X,100F8.4)') (W(i), i = 1, 4)
46
47
    write (*,*) "The corresponding Eigenvectors are"
48
49
   open(unit = 20, file = 'radialplot.dat', action = 'write', status = 'replace')
```

Exercise # 1: DSBEV.f90 subroutine

DSBEV computes all the eigenvalues and, optionally, eigenvectors of a **real symmetric band matrix**. **call** dsbev(JOBZ, UPLO, N, KD, AB, LDAB, W, Z, LDZ, WORK, INFO)

```
program SE
     implicit none
3
     double precision
                                                       :: t
     double precision, parameter
                                                       :: rmax = 40
                                                       :: \ i \ , \ \ \underbrace{j} \ , \ \ k, \ \ N, \ \ M, \ \ INFO \ , \ \ kd \ , \ \ LDAB, \ \ l
5
    integer
     {\bf double\ precision}\ ,\ {\bf dimension}\ (:)\ ,\ {\bf allocatable}
                                                      :: r, W, WORK
:: H, Z, ab
 6
     double precision, dimension(:,:), allocatable
                                                       :: uplo = 'U'
     \textbf{character}\left(1\right), \ \textbf{parameter}
8
     intrinsic INT, MIN, MAX
9
10
     double precision
                                                       :: st time, sp time
11
     \mathbf{print}*, "Enter the size of a grid N > 5: " ; \mathbf{read}*, N
12
13
     print*, "Enter the value for angular momentum l = "; read*, l
14
     kd = 1 !***** For H we have only one super/sub diagonal vector*******
15
    LDAB = kd + 1
16
17
     allocate(r(N-1),H(N-1,N-1),W(N),Z(N,N),ab(LDAB,N),WORK(3*N-2))
19
     20
     t = rmax/dble(N)
21
22
    23
     {\bf do}\  \  \, {\rm i}\  \, =\  \, 1\,,\  \  \, {\rm N}\!\!-\!2
24
     \begin{array}{lll} r\,(\,i\,) & = \,i\,*t \\ H(\,i\,\,,\,i\,) & = \,2\,*(\,1\,\,-\,\,(1/\,r\,(\,i\,\,))\,*\,t\,*t\,\,+\,\,(\,l\,*(\,l\,+1))\,*(1/\,r\,(\,i\,\,)\,*\,*\,2\,)\,*((\,t\,*\,t\,\,)/\,2) \end{array} \,) \end{array}
25
26
     H(i+1,i) = -1d0
27
28
     H(i, i+1) = -1d0
29
     enddo
30
    H(N-1,N-1) = 2*(1 - (1/(r(N-2)+t)*t*t) + (1*(1+1))*(1/(r(N-2)+t)**2)&
                     *((t*t)/2)
31
32
    H = H/(2*t**2)
33
     34
     if (uplo == 'U') then
35
     do i = 1, N-1
36
     \mathbf{do} \ \mathbf{j} = \mathbf{i} \ , \ \mathbf{MIN}(\mathbf{N}-1, \ \mathbf{i}+\mathbf{kd})
37
       ab\,(\,kd{+}1{+}i\,{-}j\,\,,\,j\,\,)\,\,=\,\,H(\,i\,\,,\,j\,\,)
38
39
         enddo
40
    enddo
41
     else if (uplo = 'L') then
     \begin{array}{lll} \mathbf{do} & \mathrm{i} & = & \mathrm{i} & \mathrm{N-1} \\ \mathbf{do} & \mathrm{j} & = & \mathrm{i} & \mathrm{MAX}(1\,,\,\,\mathrm{i}\,\mathrm{-kd}\,) \end{array}
42
43
44
        ab(1+i-j, j) = H(i, j)
45
      enddo
      enddo
46
47
     endif
48
     49
     50
51
52
     call cpu time(st_time)
     call dsbev ('V', uplo, N, kd, ab, LDAB, W, Z, N, WORK, INFO)
54
     call cpu_time(sp_time)
     55
     print*, ":: The Eigen values for l = ", l write(*,'(1x,1000 f12.5)'), (W(i), i = 1, 5)
56
```

```
print*, ":: The correspoding Eigenvector are"
58
59
       !****** Saving the radial part in file to plot*****************
60
      open(unit = 20, file = 'radialWF.dat', action = 'write', status = 'replace')
61
62
       write(20,*) N-1
63
       do i = 1, N-1
        \mathbf{write} (20, '(1X, 1000\,\mathrm{F}12.5)') \ \mathrm{r}(\mathrm{i}), \ \mathrm{H}(\mathrm{i}, 1) * (1/\mathrm{r}(\mathrm{i})), \ \mathrm{H}(\mathrm{i}, 2) * (1/\mathrm{r}(\mathrm{i})), \ \mathrm{H}(\mathrm{i}, 3) * (1/\mathrm{r}(\mathrm{i})), \ \mathrm{H}(\mathrm{i}, 4) * (1/\mathrm{r}(\mathrm{i}))
64
65
66
       write (*,*) "Wall Time", sp time - st time, "seconds"
67
     end program SE
```

Exercise # 1: DSTEBZ.f90 subroutine

```
call dstebz (RANCE, ORDER, N, VL, VU, IL, IU, ABSTOL, D, E, M, NSPLIT, & W, IBLOCK, ISPLIT, WORK, IWORK, INFO)
```

DSTEBZ computes the eigenvalues of a symmetric tridiagonal matrix T. The user may ask for all eigenvalues, all eigenvalues in the half-open interval (VL, VU], or the IL-th through IU-th eigenvalues.

```
program eigendstebz
1
     USE SE mod! module is given below this program for constructing Hamiltonian
3
     implicit none
                                               :: \mathbf{RANGE} = 'A', ORDER = 'E'
    character(1), parameter
4
                                              :: N, M, NSPLIT, INFO, i, j, l
    integer
                                              :: IL = 0, IU = 0
:: IBLOCK, ISPLIT, IWORK
6
    {\bf integer}\;,\;\;{\bf parameter}\;
    integer, dimension(:), allocatable
                                              :: VL = 0, VU = 0
    {\bf double\ precision}\ ,\ {\bf parameter}
                                               :: ABSTOL = -1
9
    {\bf double\ precision}\ ,\ {\bf parameter}
                                                  :: W, WORK, D, E
10
    \  \  \, double\  \  precision\;,\;\; dimension\;\;(:)\;,\;\; allocatable
    11
12
    double precision
                                              :: start_time, stop_time
13
14
    !********Requesting\ matrix\ dimension*****
    15
16
    call hamil(A.N.1)
17
18
    allocate (IBLOCK(N), ISPLIT(N), IWORK(3*N), W(N), WORK(4*N), D(N), E(N-1))
19
    N = N - 1
20
21
    open (unit = 10, file = 'hamilmatrix', action = 'write', status = 'replace')
22
    do i = 1. N
     write(10, '(1x, 1000000F12.6)') (A(i, j), j = 1, N)
23
    enddo
25
    close (10)
26
     27
    do i = 1, N
     D(i) = A(i,i)
28
29
    enddo
30
    do j = 1, N-1
31
     \mathrm{E}(\,\mathrm{j}\,) \,=\, \mathrm{A}(\,\mathrm{j}\,\,,\,\mathrm{j}\,{+}1)
32
     33
34
35
    call cpu time(start time)
    call DSTEBZ(RANGE ORDER, N, VL, VU, IL, IU, ABSTOL, D, E, M, &
36
37
    NSPLIT, W, IBLOCK, ISPLIT, WORK, IWORK, INFO)
38
    call cpu time(stop_time)
39
    if (INFO.NE.0) then
40
     write(*,*) 'DSTEBZ', INFO
41
42
    _{
m else}
43
     write(*,*)
     write(*,*) "Number of Eigen values found", M, NSPLIT
44
     Write (*, *) 'Eigenvalues are::'
45
     Write (*, *) (W(j), j=1, 5)
46
47
    print*, "Original loop time", start time - stop time, "seconds"
48
    deallocate (IBLOCK, ISPLIT, IWORK, W, WORK, D, E, A)
49
   end program eigendstebz
51
   !!!!!!!!!!!!!!!!!!!!!MODULE FOR constructing Hamiltonian!!!!!!!!!!
   MODULE SE mod
```

```
53
     implicit none
54
     contains
55
    subroutine hamil(H,N,1)
56
    double precision
                                                     :: t
    double precision, parameter
57
                                                     :: rmax = 100
58
    integer
                                                     :: \quad i \ , \quad j \ , \quad k \ , \quad M, \quad g
    double precision, dimension(:), allocatable :: r
double precision, dimension(:,:), allocatable, intent(inout) :: H
59
60
61
    integer , intent(in)
                                     :: N, 1
    \textbf{allocate} \left( \begin{smallmatrix} r \end{smallmatrix} (N-1), H(N-1, N-1) \right)
62
63
    t = rmax/dble(N)
64
    r\ =\ 0\,d0
65
66
    H\,=\,0\,\mathrm{d}0
67
    68
    Hamiltonian **********
    69
70
71
    do i = 1, N-2
     \begin{array}{lll} r(\,i\,) & = \,i\, *\, t \\ H(\,i\,,\,i\,) & = \,2*(1\,-\,(1/r\,(\,i\,))*t*t\,+\,(1*(1+1))*(1/r\,(\,i\,)**2)*((\,t*t\,)/2) \end{array})
72
73
74
     H(i+1,i) = -1d0
75
     H(i, i+1) = -1d0
76
    enddo
    H(N-1,N-1) = 2*(1 - (1/(r(N-2)+t)*t*t) + (1*(1+1))*((1/r(N-2)+t)**2)*((t*t)/2))
77
    H = H/(2*t**2)
78
79
    end subroutine hamil
81 END MODULE SE mod
```