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**Разработка шестиосевого датчика силы на основе  
оптического датчика давления барьерного типа  
  
Development of a six-axis force sensor based on a barrier-type  
optical pressure cell**

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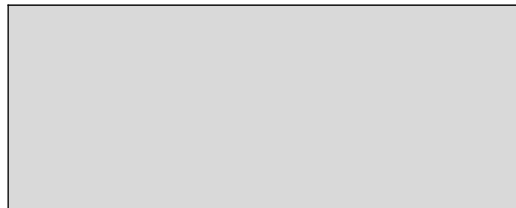
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## **Abstract**

The multi-axis force sensor market is currently dominated by strain gauge sensors, but other options exist, such as hall-effect, fiber Bragg grating (FBG), and optoelectronic cells.

The optoelectronic cell is perceptible due to its low cost, excellent precision, and simple implementation. Nevertheless, a dearth of solutions appropriate for large-scale manufacturing and enable adjustable sensor parameters exists.

This study aims to explore how the shape and material of the barrier affect the measurement range of an optoelectronic barrier-type sensor. Additionally, a modular multi-axis force sensor will be designed using the measurement cells.

The study design involves examining the impact of barrier shape and material on the measurement range of the optoelectronic barrier-type sensor. Additionally, in the research, I designed a modular multi-axis force sensor based on the presented measurement cells.

The optoelectronic six-axial force sensor, which is the focus of this study, is characterized by its simplicity and ease of implementation as a modular sensor. It provides a cost-effective solution and facilitates the straightforward replacement of construction elements. Consequently, this sensor has the potential to broaden the range of applications for multi-axis force sensors.

This research contributes to understanding how the shape and material of the barrier affect the measurement range of optoelectronic barrier-type sensors. The design of a modular multi-axis force sensor provides a cost-effective and adjustable solution for various robotic applications.

# Chapter 1

## Introduction

Multi-axial force sensors, also referred to as multi-axis force sensors, are devices that can measure forces and torques in multiple directions or axes simultaneously (from one to six dimensions). These sensors find applications in various fields such as robotics, biomechanics, and industrial automation [1].

The classical multi-axis force sensor is a system of uniaxial pressure sensors of different dimensions. While the strain-gauge sensor remains the most common solution as uniaxial pressure measurement cell in the field of multi-axial force sensors, optical sensors shows noticeable accuracy with higher linearity [2]. The structures of the optical multi-force sensors has been solid [2], [3], while for strain-gauge based sensors fully mechanically decoupled solutions exists [4], [5].

The objective of this project is to investigate the relationship between the linearity of optical sensors and the construction of the barrier and multi-axial sensor configuration. The project is divided in two parts: development of a single degree of freedom pressure sensor and a multi-axis force sensor based on a designed pressure cell. Both parts aim to develop a mathematical model for the sensor, its prototype and conduct testing to evaluate accuracy, hysteresis and axis crosstalk.

The multiaxis force sensor development is

The most common solutions for multi-axial force sensors constructions and pressure cells types are described in the

## **1.1 Overview of thesis contents**

Literature Review chapter will outline the general information about multi-axial force sensors, force measurement cells technologies and state pros and cons of multi-axial force sensors existing solutions. Also the chapter will review methods of statical calibration and experimental setups used for testing the sensor' kind.

?? chapter will provide the mathematical model of the optical force measuring cell.

Construction modeling will present the target multi-axis sensor structure.

In Implementation chapter I describe the experimental setup and the results evaluation techniques, provide comparison with my mathematical model.

# Chapter 2

## Glossary

|                               |  |
|-------------------------------|--|
| <b>cell of a sensor</b>       | ...  |
| <b>coupling</b>               | ...  |
| <b>crosstalk</b>              | undesired measured output of a<br>transverse channel under defined load<br>on the calibrated axis ISO 21612:2021(E)                        |
| <b>cross-coupling</b>         | ...  |
| <b>isotropy</b>               | exhibiting properties (such as velocity of<br>light transmission) with the same values<br>when measured along axes in all directions [6]   |
| <b>ERSG</b>                   | Electrical Resistance Strain Gauge   |
| <b>FBG</b>                    | Fiber Bragg grating  |
| <b>Data acquisition (DAQ)</b> | the process of measuring an electrical<br>or physical phenomenon, such as voltage, current,<br>temperature, pressure, or sound. standards. |



# Chapter 3

## Literature Review

### 3.1 Navigation

The objective of this chapter is to conduct a literature review on the development of six degrees of freedom (DOF) force sensors. Section 3.3 defines the types of pressure sensors used as measurement cells for multi-axis force and torque sensors, along with their limitations. In Section 3.5, an examination of the construction of multi-axial load sensor beams is presented.

Finally, in Section 3.6, the research gap in this field is identified.

### 3.2 Metrics

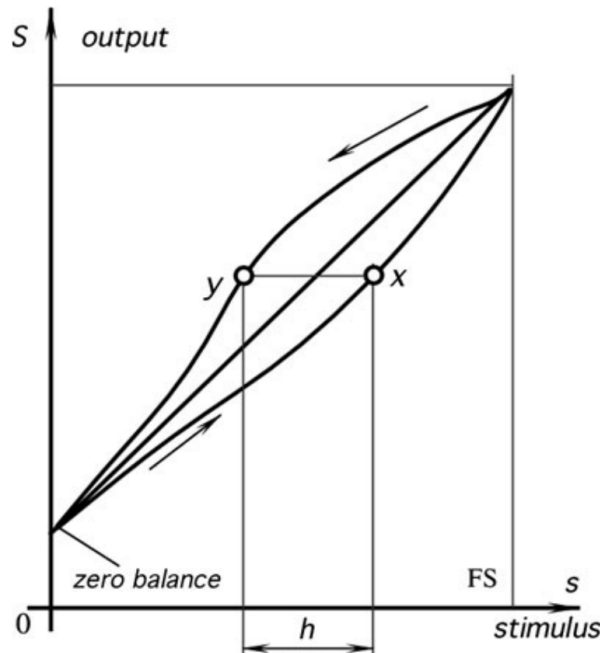
To align with the reader in the terminology used, this section presents the metrics and their definitions used for multi-axis force sensors. stiffness, nominal values, isotropy In a coupled sensor an axis force component produces signal in more than one measurement cell, therefore calibration becomes more complicated.

### 3.2.1 Isotropy

Isotropy of a multiaxial sensor defines the difference in the measuring range of the sensor along different axes. The property is fully depends on the system's construction. Based on the [1, Tab. 2, 3, 4] most multiaxial force sensors the isotropy is low mostly because the structure of the sensors is unsymmetrical.

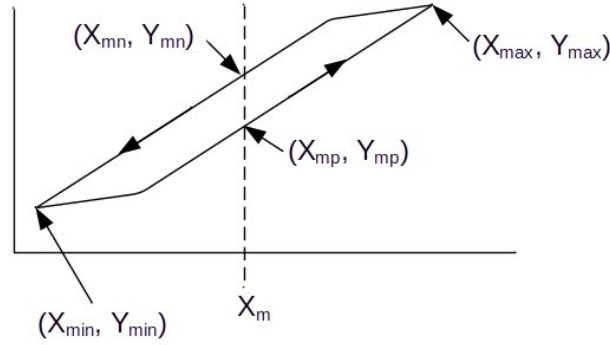
### 3.2.2 Hysteresis

In certain systems, the sensor output varies based on the direction of load application. The difference between the outputs is referred to as hysteresis error [7], which represents the memory of the system.



**Figure 3.1:** Diagram illustrating the relationship between stimulus and signal in a system with hysteresis. Adapted from [7, Fig. 2.11].

The hysteresis calculated in the paper is defined as in manual published by the Missouri University of Science and Technology [8].



**Figure 3.2:** Definition of main hysteresis points. Adapted from [8, Fig. 3].

$$X_m = \frac{X_{max} - X_{min}}{2} + X_{min} \quad (3.1)$$

The equations (3.1) and (3.2) define the hysteresis as a value variance compared to the value full scale.

$$Hysteresis = \left| \frac{Y_{mn} - Y_{mp}}{Y_{max} - Y_{min}} \right| \quad (3.2)$$

### 3.2.3 Coupling

One of the main metrics for multi-axial force sensor is degree of coupling, which determines the complexity of calibration matrix of a sensor [1], [4], [9]. Dimensions coupling problem is one of the most common problems for multi-axial force sensors [10]. The degree of coupling among the axes directly impacts the accuracy of the sensor and the complexity of calibration [1], [4], [9]. In a coupled sensor, an axis force component can produce signals in more than one measurement cell, thereby complicating the calibration process. However, designing and manufacturing highly decoupled structures can be challenging [11].

To reduce axis dependence one may change structure of the sensor or perform high precision calibration. Existing solutions for multi-axial force sensor

structures are presented in the 3.5 section.

The crosstalk term, [12]

### 3.3 Pressure cells types

The pressure sensors are the main measuring components used for multi-axial force sensors. The output of the sensors is mapped via transition function into the force/torque terms. The choice of the measuring components defines the hysteresis, linearity, span and resolution of the whole system. Thereby, several pressure sensors types will be described in the subsection.

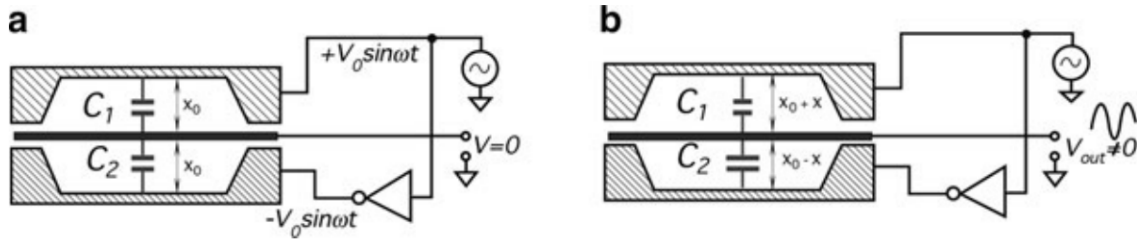
#### 3.3.1 Piezoelectric sensor

Piezoelectric pressure sensor consists of a thin silicon diaphragm as elastic part and a piezoelectric gauge resistor [7]. The single crystal silicon has exceptional elastic characteristics, therefore no hysteresis occurs in the system [7].

The piezoelectric element has an AC effect, allowing the piezoelectric pressure sensor to convert pressure changes into an output signal. When a load is applied to the sensor, piezoelectric crystals generate voltage across the sides of the crystal, related to amount of bending load. On the other hand, it may not measure steady-state pressure [7].

The main issue with crystal resonators in pressure sensors is that the resonator must have the highest possible quality factor and be isolated from the environment. However, the quality factor of the crystal is reduced when a load is applied [7].

Even when a multi crystal structure is used in the sensors, the total wave reflection occurs and affects the quality factor [7].



**Figure 3.3:** Principle of operation for a flat-plate capacitive sensor. Adapted from [7, Fig. 7.6].

### 3.3.2 Capacitive sensor

The capacitance of a flat capacitor can be determined using equation (3.3). This formula describes the connection between capacitance, plate area, and the distance between the plates of the device. Changes in distance and area result in variations in capacitance, which is utilized in capacitance-based pressure sensors to measure changes in distance. The principle is as follows: when pressure is applied to the capacitor's plate and alters the distance  $d$ , the changes in capacitance are measured and converted into a signal.

$$C = \frac{\epsilon_0 \epsilon A}{d} \quad (3.3)$$

Capacitive sensors can be monopolar, differential (utilizing two capacitors), or a capacitive bridge can be utilized (using four capacitors) [7]. A typical capacitive pressure sensor is differential, with a diaphragm surface serving as the central plate, as depicted in Fig. 3.3, creating a dual variable capacitor [13]. The capacitance changes when a load is applied to the diaphragm surface.

Capacitive pressure sensors have broad measurement range, high sensitivity, accuracy and reliability, absence of contamination risk, large range of working temperatures ( $-70\text{ }^{\circ}\text{C}$  to  $400\text{ }^{\circ}\text{C}$ ). The sensors are low-cost, highly sensitive devices

mostly used in exceptional circumstances, such as miniature or even MEMS force sensors [1] and harsh environmental conditions.

Hysteresis 0.35 % [14], 1.7 % [15].

### 3.3.3 Electrical Resistance Strain Gauge

The principle behind Electrical Resistance Strain Gauges (ERSGs) is the change in resistance caused by deformation, as explained in a study by official representative of Keller AG manufacturer [16]. Stretching or compressing of the piezoresistive material results in a change in the electric resistance of the sensor

[1]. In order to accurately measure small changes in geometry, strain-gauge sensors are typically connected to a Wheatstone bridge.

Since the creation of the multi-axis force sensor in the 1970s, the strain-resistive pressure sensor has remained a classic measuring device [17]. However, these solutions tend to be expensive and require additional surface treatment of the substrate, as well as high-quality technology for bonding with a strain-resistant component [18], [19]. Load cells, which utilize strain gauges, face challenges in signal processing. These challenges include sensitivity to temperature and magnetic noise, the need for regular calibration, and difficulties in maintenance after the substrate undergoes plastic deformation. Regarding response times, typical values of this measuring principle range from 1 to 10 ms. [13]

The hysteresis range for 6-axis force sensor : 0.26 – 0.73 % [20], 0.6–1.3 % [21].

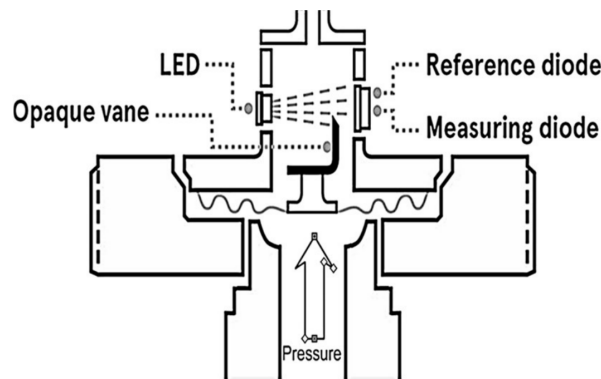
### 3.3.4 Fiber Bragg grating

Fiber Bragg gratings (FBG) are the most popular optical pressure measurement methods. The FBG sensor is a specific type of distributed Bragg reflector that is created within a short section of optical fiber. Its function is to selectively reflect certain wavelengths of light while allowing all other wavelengths to pass through. When subjected to strain or temperature variations, the reflected wavelengths of an FBG shift accordingly. The magnitude of this wavelength shift is directly proportional to the applied load. Several scientific papers, including Xiong L. et al. [17] and Guo Yu [19], have documented the development of six-axis force sensors utilizing a fiber Bragg lattice. This design offers several advantages over strain-resistant sensors, such as immunity to electromagnetic interference, a compact profile, and lightweight construction. However, important to note that FBG-based sensors necessitate significant investments in optical signal demodulation equipment [17], as well as surface treatment processes.

### 3.3.5 Photointerrupter cell with barrier

The optocoupler pressure sensor comprises three main components: a light emitter, two light receivers, and an interrupter positioned between emitter and one of the receivers [18]. When a load is applied to the sensor, the interrupter plate shifts, thereby altering the rate of light intensity on the measuring diode [3]. The signal from the second receiver is a reference and enables the cancellation of the optocoupler characteristics change, that effects whole system equally, caused by temperature, dirt and etc.

In the mathematical model of this type of cell, the barrier can be considered as a spring, making the applied force proportional to the deformation of the barrier.



**Figure 3.4:** Example of an optical pressure sensor. Adapted from [13, Fig. 5].

This type of sensor has negligible hysteresis and repeatability error, since the vane movement amplitude to close the measuring diode is very small [13]. Additionally, it offers a compact geometry and is cost-effective.

Compared to ERSG sensors, the photointerrupter measurement cell is less susceptible to electrical interference [18].

The properties associated with hysteresis and the sensor's nominal range are primarily influenced by the type of barrier utilized [18].

Other advantages of this type of pressure sensor, particularly important in certain industrial applications, include its long transmission distance and low chemical reactivity, making it ideal for operation in explosive-risk environments and intrinsically safe. The sensors using this measuring principle have a response time of about  $100\ \mu\text{s}$  and an average force resolution of  $0.1\ \text{N}$  over a  $200\ \text{N}$  measurement range [13].

The described characteristics of force sensor types force me to use the one in the research and try to apply the measurement principle in cells of my multi-axial force sensor.



## 3.4 Calibration

The multi-axis calibration has static and dynamic methods based on the applied force/pressure [13], [22]. A load usually is said to be static, if it remains constant during the measurement process. Accordingly, a load is said to be dynamic if it varies significantly in a short amount of time, usually, several times during the measurement. The dynamic calibration is applied to sensors designed for highly dynamic environment with pressure pulsations or to determine the sensor response time [13]. In my research the static calibration is sufficient, therefore, lets focus on the methods used in the multi-axis force sensors development.

Two static calibration methods exists: traditional and neural-networks based [10], [23].

Traditional method involves linear transformation (LT) of pressure cells output to the force and torque space using least-square-method (LSM) [23]. The mapping is represented with  $N \times 6$  matrix, where  $N$  - number of uniaxial pressure sensors of the system [23]. The method defines two limitations [23]:

- The LT defines the linear dependency of sensor' output to the elastic body transformation.
- Matrix mapping representation requires load axes independence.

In other words, the sensor output has to be linear to applied load with fully decoupled axes. The conditions are hard to satisfy, therefore many researches about structural sensors decoupling exists [4], [5], [11], [24].

Neural-networks based

...

### 3.4.1 How the ISO standart determines the calibration process

— All force and moment channels are measured during the calibration process of each axis. All channels are to be offset corrected in unloaded condition prior to the calibration test.

For force loading the force is applied within the neutral axes of the load cell.

In order to keep accuracy and to prevent misalignment it should be avoided to exert torque within the mounting plane between load cell and fixture. This load case should be last in the sequence. It can cause rotation of the load cell within the fixture. Thus subsequently exerted loads can be shifted from the intended load axis

#### **misalignment determination**

For a loading in discrete steps or a continuous loading procedure, the output voltages in [mV/V] of all transverse channels need to be recorded. After the calibration of all axes, the current sensitivities of these channels are known and can be used for the calculation of the crosstalk as percentage of the transducer axis' calibration range. For the force and moment channels, the transverse channels' output voltage recorded in [mV/V] (see NOTE 1) shall be converted to the physical dimension force or moment by applying the current sensitivity determined from the calibration test before.

## 3.5 Constructions

Typically, the assessment of forces and moments in various directions is achieved by utilizing multiple strain-sensitive sensors affixed to a flexible substrate [1]. The structure of a sensor plays a crucial role in its design as it governs

characteristics such as stiffness, nominal values, isotropy, and the coupling among the measured axes [1], [24].

To create optimized decoupled structures, engineers employ finite element analysis (FEM) [1], [3], [24].

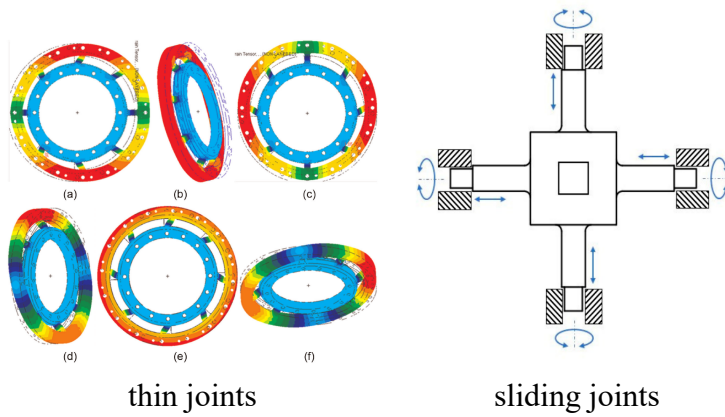
#### 1. Rigid jointed cross-beams

The most prevalent type of sensors used are rigid-joined sensors, primarily due to their solid beam structure, which facilitates simplified manufacturing. According to studies conducted by [1], [24], rigid-joined cross beams exhibit reduced measurement isotropy and an increased level of coupling. The high level of coupling of rigid-joined sensors pushed researchers to find mechanically decoupled solutions. A comprehensive compilation of rigid-joined cross-beam sensors can be found in [1].

#### 2. Flexible jointed cross-beams

The flexible jointed structure was created to avoid the calibration complexity of mechanically coupled sensors [11]. What is a flexible joint of the cross-beam? Some researches define the flexible joint as a thin regions in the beam structure. Those regions are elastic compared to the whole beam, therefore they act as a damper and reduce the cross dimension coupling.

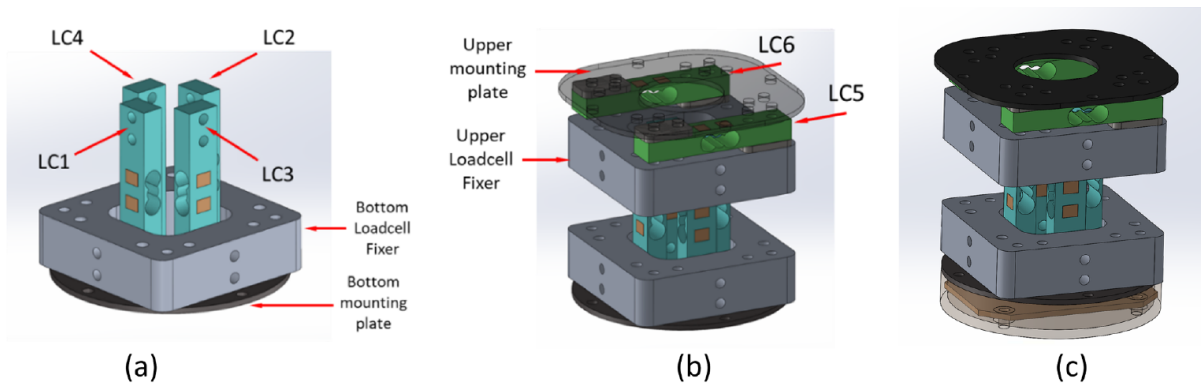
The second type of flexible jointed cross-beams is the *WHICH<sub>W</sub>ORD<sub>T</sub>O<sub>U</sub>SE*. Their constructions has additional mechanical component as joint, for example, bearings or hinges.



**Figure 3.5:** Example of flexible joined beams structures for multi-axial sensors.

### 3. Modal cross-beams

With the advancement in computational power, the creation of mechanically decoupled solutions has become more accessible. In their study, Mayetin and Kucuk [5] developed a modal sensor with an average interference error of less than 3%. This approach allows for the replacement of failed structural elements, enhancing the overall reliability and longevity of the sensor.



**Fig. 3.** Design details of the force-sensing unit, a) beam type load cells for  $X$  and  $Y$  axes, b) beam type load cell for  $Z$  axis, c) full assembly appearance

modal sensor from [5]

## 3.6 Conclusion

In this literature review, we have explored the research conducted by Hosseinabadi and Salcudean [2] and the model proposed by [18] for a mechanically decoupled six DOF force sensor with low cross-coupling error and high resolution to scale ratio of 0.0001%. Additionally, we have examined the 3-DOF force sensor structure proposed in [5], which features four independent beams with an average interference error of less than 3%.

Building upon these previous studies, the current research aims to develop a mechanically decoupled modal structure for a six DOF force sensor, utilizing the measurement cell invented by [18]. The focus of this study will be on calculating the cross-coupling interference, resolution to scale ratio, and hysteresis of the sensor.

# Chapter 4

## Methodology

In the thesis the main focus is to design a high linear, decoupled, modal structured multiaxial force sensors. In the Literature Review we describe theoretical background for the task.

The chapter specifies methodology of the design, therefore the chapter is divided into several sections. The first the Optical modeling section defines transition function for pressure sensor cell. The second section Pressure Sensor Calibration describes the calibration method, used for pressure measurement cells.

The next Modeling of pressure cell section will provide the design used for measurement cells, the electric circuit and the used optical barrier shape.

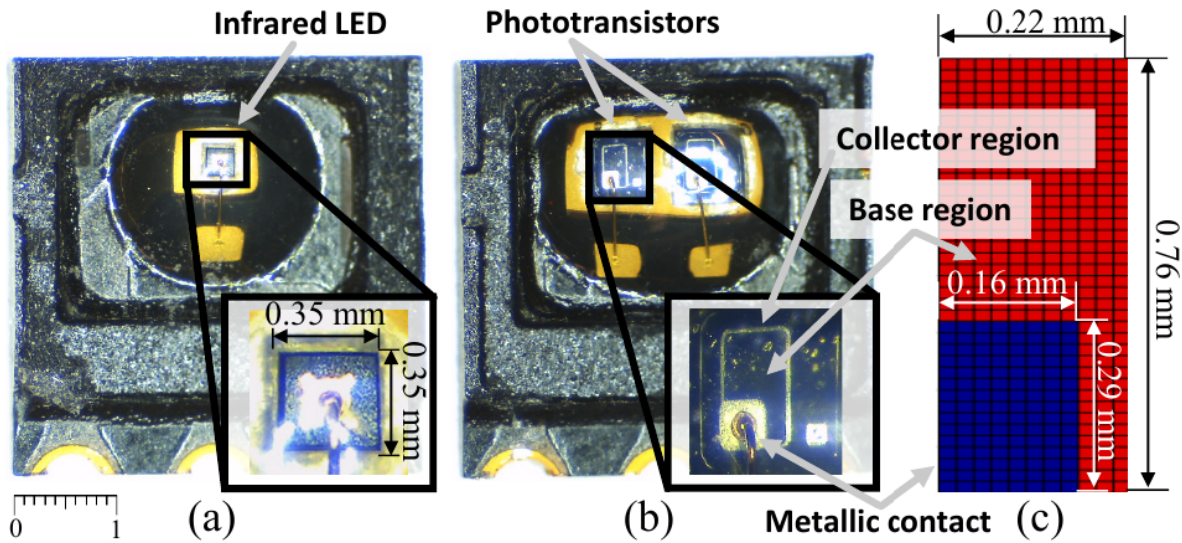
### 4.1 Optical modeling

A well-defined optical model can enhance the linearity of the sensor [18]. Therefore, this chapter will concentrate on the mathematical model of the optocoupler and the physical processes that determine the characteristics of an optical pressure sensor.

The primary components of the optocoupler include two phototransistors (PTs), a light-emitting diode (LED), and a photobarrier (PB). In optical pressure sensing, two PTs are utilized: one as a measuring device and the other as a reference. A barrier is positioned between the measuring PT and the LED. When pressure is applied, the barrier shifts and obstructs a portion of the light from the LED, thereby altering the induced current on the measuring PT.

The purpose of the chapter is to find the function  $F = f(i_{\text{mes pt}})$ , which describes the relation between current on the measuring phototransistor  $i_{\text{mes pt}}$  and load  $F$ , applied to the barrier.

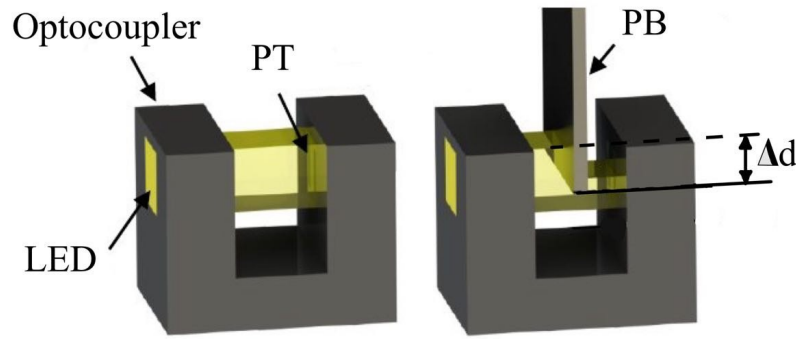
For the project I use a PT module (EE-SX1321, OMRON). The emitter and detector of the sensor consists of a set of cells as shown in Fig. 4.1.



**Figure 4.1:** Microscopic image showing (a) the LED and (b) the PTs embedded within the optocoupler (EE-SX1321, OMRON). (c) Base area of the PT estimated by [18, Fig. 4]. Adapted from [18, Fig. 4].

In the upcoming chapter, the PB will be simplified to a spring element with an aperture. This simplification enables the use of Hooke's law  $F = k\Delta d$ , where  $F$  represents the load applied to the PB,  $\Delta d$  denotes the shift of the barrier's aperture,

and  $k$  represents the characteristic of the spring. By using this law, the function  $F = f(i_{\text{mes pt}})$  can be updated to  $F = k\Delta d = kf_d(i_{\text{mes pt}})$ . The value of  $k$  will be determined through finite element analysis (FEA) in the subsequent chapter.



**Figure 4.2:** Model of PT-based load sensing mechanism. Adapted from [18, Fig. 1].

Limitations of the mathematical model:

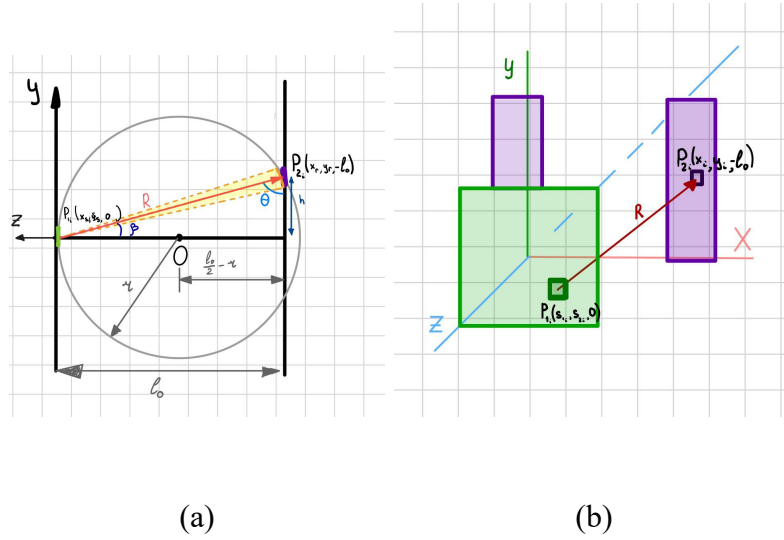
- LED is Lambert's source of light.
- PT acceptable wavelength is the same as of emitted light.
- Light is a stream of particles.
- PB will be simplified to the spring element with aperture. When a force is applied to the PB, the aperture will be shifted relative to the main optical axis of the light source.

### 4.1.1 Optocoupler

Fig. 4.3 illustrates the geometric relationship between the LED and PT. As mentioned, the optocoupler's LED and PT are divided into small cells by hardware. Each cell of the LED will be treated as a Lambertian source of light, and the



intensity of PT cells will be calculated individually. The overall intensity of the entire PT is then determined by summing these individual intensities.



**Figure 4.3:** Geometrical relationships between LED (green) and PT(purple): (a) YZ plane sketch, (b) oblique sketch.

To start with function  $f_d(i_{\text{mes pt}})$ , lets note that  $i_{\text{mes pt}} \sim \Phi(\vec{r})$ , where  $\Phi(\vec{r})$  represents the amount of radiant power (radiation flux) passing through the area of interest, with its norm aligned with  $\vec{r}$ .

To incorporate the distance between the light emitter and receiver into the model, I will utilize luminous intensity, which indicates the level of brightness and determines the flux passing through a solid angle  $\Omega$ , proportional to the squared distance from the observer to the light source.

$$I(\vec{r}) = \frac{d\Phi}{d\Omega}$$

$$\Omega = \frac{A^\perp}{r^2}$$

The radiant intensity of a unit area of the LED exhibits Lambertian reflectance.

Therefore, a unit surface of the application will receive an amount of radiation proportional to the cosine law:

$$I(\vec{r})_{\perp} = I_0 \cos(\beta)$$

The radiation pattern on a unit area perpendicular to the  $r$  vector will be as follows [18]:

$$I(\vec{r})_{\perp} = I_0 \frac{\cos \beta}{4\pi r^2}$$

In our case, the PT surface is a sheet, which is why we need to project the calculated illuminance onto the PT plane:

$$I(\vec{r}) = I_0 \frac{\cos^2 \beta}{4\pi r^2}$$

$$h = (x_s - x_r)^2 + (y_s - y_r)^2$$

$$R^2 = h^2 + l_0^2$$

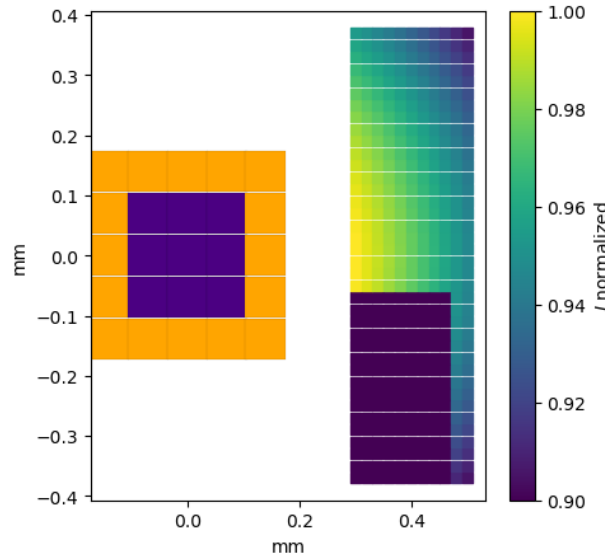
$$r^2 = h^2 + \left(\frac{l_0}{2}\right)^2$$

$$\beta = \arcsin\left(\frac{h}{R}\right)$$

where  $R$  - radius vector from  $i$ -th light source to the  $j$ -th receiver cell,  $\beta$  - angle between norm vector of emitter area and the vector  $R$ ,  $s_1$  and  $s_2$  - coordinates of the LED,  $x$  and  $y$  - coordinates of the PT.

From the geometrical relationship, the total PT radiation flux is the integral of the LED ( $A_{LED}$ ) and PT ( $A_{PT}$ ) areas:

$$\Phi = \int_{A_{LED}} \int_{A_{PT}} I(\vec{r}) dA_{LED} dA_{PT} \quad (4.1)$$



**Figure 4.4:** Results of optical model simulation without PB (LED on the left, PT on the right). The purple color defines zones of optocoupler used for electrical connection (EE-SX1321, OMRON).

On the Fig. 4.4 results of the model simulation with one PT and a LED are presented.

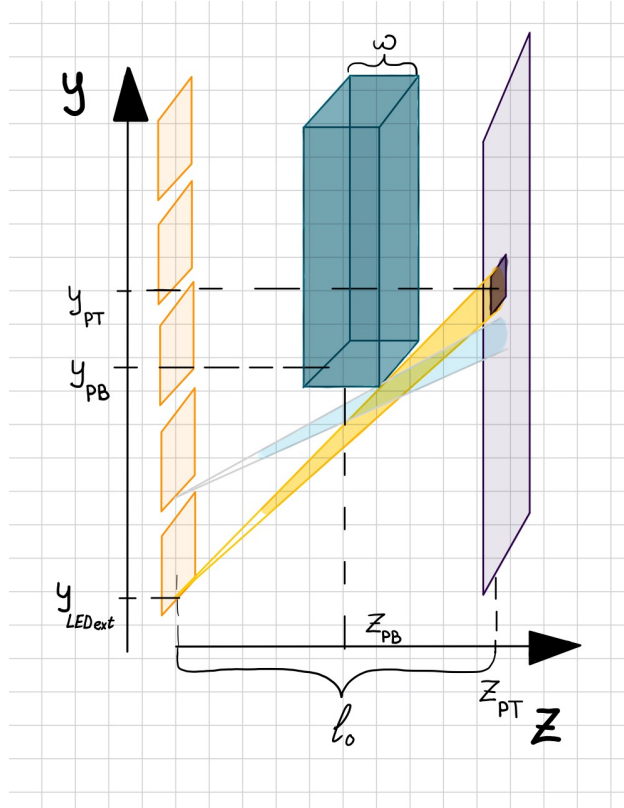
### 4.1.2 Photobarrier

The Photo Barrier (PB) will be simplified to a cuboid shape, the PB partially covers the measurement phototransistor from the LED light. The relationship between the optocoupler and the PB is shown in Figure 4.2. The stimulus for the pressure sensor depends on the shift of the photobarrier as its tip moves alongside the measuring PT. The PT module used (EE-SX1321, OMRON) has small dimensions, so the barrier shift is limited by the height of the PT, which is 0.76 mm as shown in Fig. 4.1. When the bottom edge of the PB reaches the borders of the PT,

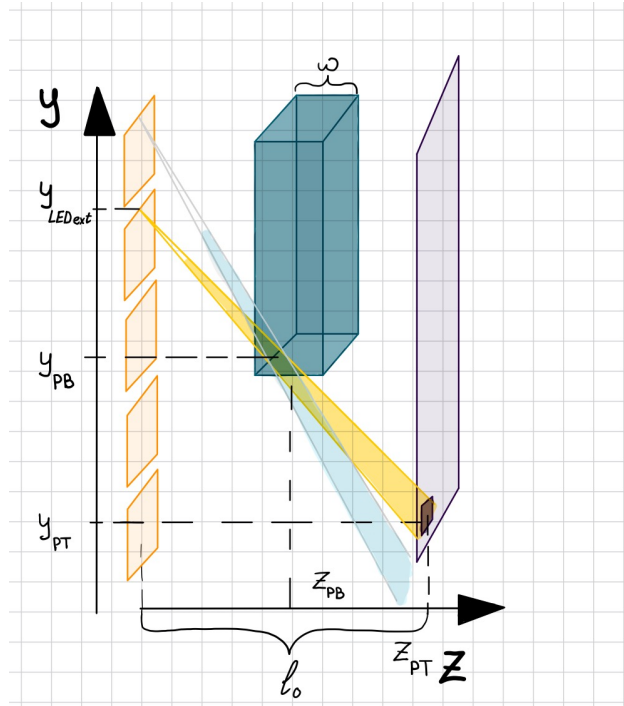
the intensity measurements will remain constant.

In order to determine the intensity of light on the PT cells with respect to the PB, we establish the geometric relationship between the amount of light that is transmitted to the receiver from an LED cell when a barrier is shifted. The extremum  $y_{PT_{ext}}$  coordinate within the model is defined as the  $y$  coordinate of the bottom edge of the barrier shadow on the PT. Consequently, the PB cells located above the  $y_{PT_{ext}}$  do not receive light from the LED cell.

The model does not utilize the  $y_{PT_{ext}}$ , but instead the  $y_{LED_{ext}}$ . This represents the coordinate of the LED that emits light reaching the PT cell, as depicted in Figure 4.5.



(a)



(b)

**Figure 4.5:** Geometrical relationship between  $y_{LEDext}$ , photobarrier and phototransistor cells: (a)  $y_{PT} > y_{PB}$ , (b)  $y_{PT} < y_{PB}$

The extremum  $y_{LEDext}$  is calculated for each PT cell is defined as the following:

$$\Delta y = y_{PB} - y_{PT}$$

$$\begin{cases} \Delta z = z_{PB} + (\omega/2), & \text{if } y_{PT} > y_{PB} \\ \Delta z = z_{PB} - (\omega/2) & \text{otherwise} \end{cases}$$

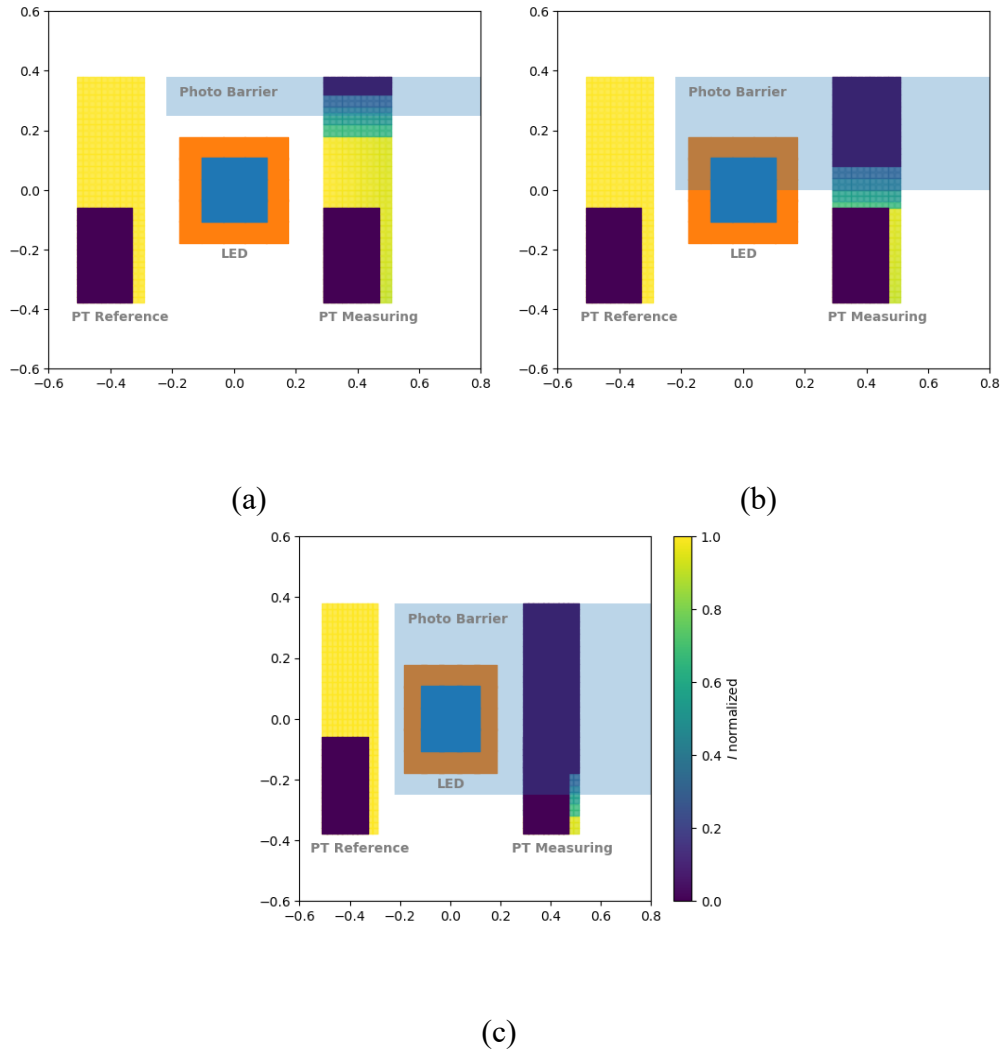
$$y_{LEDext} = \frac{\Delta y l_0}{\Delta z}$$

where  $y_{PB}, z_{PB}$  - y, z coordinated of PB cell,  $y_{PT}$  - y coordinate of the PT cell,  $l_0$  - distance between PT and LED,  $\omega$  - barrier thickness.

From Fig. 4.5 one can see that the light from a LED cell with coordinated  $(x_{LED}, y_{LED})$  reaches the PT cell if  $y_{LED} < y_{LEDext}$ . Therefore the total PT radiation flux Eq. 4.1 updates up to:

$$\Phi = \int_{A_{LED}} \int_{A_{PT}} I(\vec{r}) dA_{LED} dA_{PT} = \sum_{A_{LED}} \sum_{A_{PT}} \begin{cases} I(\vec{r}), & \text{if } y_{LED} < y_{LEDext} \\ 0, & \text{otherwise} \end{cases} \quad (4.2)$$

On the Fig. 4.6 the change of flux on the phototransistor is presented. The results are correlated to the results, received by the researches in [18].



**Figure 4.6:** Simulation with PB results for different barrier aperture shift: (a) 0.15 mm, (b) 0.4 mm, (c) 0.65 mm.

## 4.2 Pressure Sensor Calibration

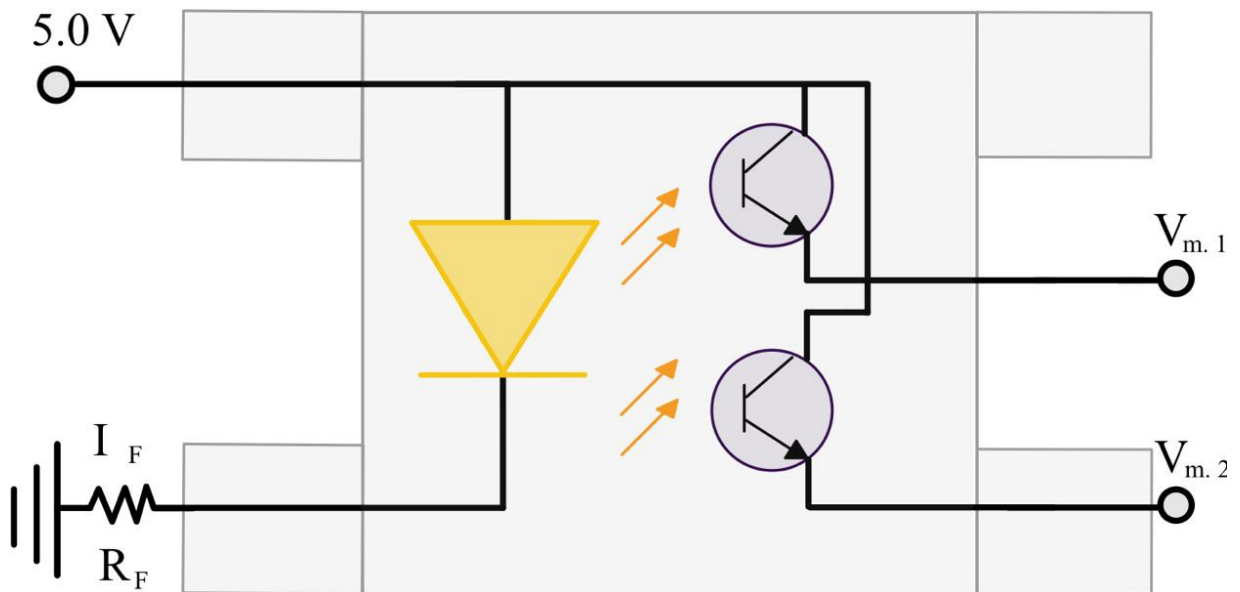
## 4.3 Modeling of pressure cell

The main focus of the section is to describe the design pressure cell, which is the main measurement component for multi-axial force sensor. As mentioned in the section on Optical modeling, I used the pressure cell design described in the

study [18] as a guide. I selected the photomicrosensor (OMRON EE-SX1321) as the optopair, similar to the authors, because it includes one LED and two phototransistors, eliminating the need for separate design and calibration of a reference phototransistor subcircuit. This step is important for optocoupler pressure sensor types to ensure that the reference and measurement phototransistors behave identically and any changes in optocoupler characteristics are minimized.

The section describes the electrical circuit and optical barrier designs.

### 4.3.1 Electric circuit design



**Figure 4.7:** Schematic of a dual-photointerrupter sensor circuit.



After testing the voltage measurement with oscilloscope, I decided to simplify the circuit presented in the research [18] up to the scheme ?? based on my experiments with the optopair component. The current of the LED is limited to  $I_F$  by the resistor  $R_F$ .

### 4.3.2 Barrier design

The dimensions of the PT are provided in 4.1

# **Chapter 5**

## **Implementation**

This chapter describes the theoretical aspects of six-axial optical force sensor development, the data filtration, communication protocols and the calibration process?

### **5.1 Optical pressure sensor**

# **Chapter 6**

## **Results and Discussion**

### **6.1 Results**

# Bibliography cited

- [1] B. B. S. J. O. Templeman and T. Sun, "Multi-axis force sensors: A state-of-the-art review," *Sensors and Actuators A: Physical*, vol. 304, p. 111 772, 2020, ISSN: 0924-4247. DOI: <https://doi.org/10.1016/j.sna.2019.111772>. [Online]. Available: <https://www.sciencedirect.com/science/article/pii/S0924424719308842>.
- [2] A. H. H. Hosseinabadi and S. E. Salcudean, "Ultralow noise, high bandwidth, low latency, no overload 6-axis optical force sensor," *IEEE/ASME Transactions on Mechatronics*, vol. 26, no. 5, pp. 2581–2592, 2021. DOI: 10.1109/TMECH.2020.3043346.
- [3] S. Hirose and K. Yoneda, "Development of optical 6-axial force sensor and its signal calibration considering non-linear interference," *IEEE International Conference on Robotics and Automation*, vol. 1, 1990.
- [4] W. Bo and P. Cai, "Decoupling analysis of a sliding structure six-axis force/torque sensor," *Measurement Science Review*, vol. 13, no. 4, pp. 187–193, 2013. DOI: <https://doi.org/10.2478/msr-2013-0028>.
- [5] U. Mayetin and S. Kucuk, "A low cost 3-dof force sensing unit design for wrist rehabilitation robots," *Mechatronics*, vol. 78, p. 102 623, 2021, ISSN: 0957-4158. DOI: <https://doi.org/10.1016/j.mechatronics>.

- 2021.102623. [Online]. Available: <https://www.sciencedirect.com/science/article/pii/S0957415821001045>.
- [6] Merriam-Webster, *Isotropic*, <https://www.merriam-webster.com/dictionary/isotropic>, (Accessed 20 Feb. 2024.)
- [7] J. Fraden, *Handbook of Modern Sensors: Physics, Designs, and Applications (Handbook of Modern Sensors)*. SpringerVerlag, 2003, ISBN: 0387007504.
- [8] “Explanation of hysteresis calculation,” *Missouri University of Science and Technology*, 2011, (Accessed 20 Feb. 2024.)
- [9] L. P. Chao and K. T. Chen, “Shape optimal design and force sensitivity evaluation of six-axis force sensors,” *Sensors and Actuators A: Physical*, vol. 63, no. 2, pp. 105–112, 1997, ISSN: 0924-4247. DOI: [https://doi.org/10.1016/S0924-4247\(97\)01534-3](https://doi.org/10.1016/S0924-4247(97)01534-3). [Online]. Available: <https://www.sciencedirect.com/science/article/pii/S0924424797015343>.
- [10] H. Cao, Y. Yu, and Y. Ge, “A research of multi-axis force sensor static decoupling method based on neural network,” Aug. 2009. DOI: 10.1109/ICAL.2009.5262800.
- [11] S. L. M. K. Kang and J. H. Kim, “Shape optimization of a mechanically decoupled six-axis force/torque sensor,” *Sensors and Actuators A: Physical*, vol. 209, pp. 41–51, 2014. DOI: <https://doi.org/10.1016/j.sna.2014.01.001>.
- [12] “Road vehicles – Crosstalk determination for multi-axis load cell,” International Organization for Standardization, Geneva, CH, Standard, Feb. 2021.

- [13] J. D. Pereira, "Pressure sensors: Working principles of static and dynamic calibration," *Sensors*, vol. 24, no. 2, 2024, ISSN: 1424-8220. DOI: 10.3390/s24020629. [Online]. Available: <https://www.mdpi.com/1424-8220/24/2/629>.
- [14] X. Wang, Y. Deng, P. Jiang, X. Chen, and H. Yu, "Low-hysteresis, pressure-insensitive, and transparent capacitive strain sensor for human activity monitoring," *Microsystems & nanoengineering*, vol. 8, p. 113, Oct. 2022. DOI: 10.1038/s41378-022-00450-7.
- [15] J. Roh, K.-S. Shin, T.-H. Song, J. Kim, and D.-S. Lee, "Development of an implantable capacitive pressure sensor for biomedical applications," *Micro-machines*, vol. 14, p. 975, Apr. 2023. DOI: 10.3390/mi14050975.
- [16] S. Boyn, *Piezoresistive pressure measurement technology, [online]*, [https://www.catsensors.com/media/Archivos\\_pdf/Fachbeitrag\\_Piezo\\_e.pdf](https://www.catsensors.com/media/Archivos_pdf/Fachbeitrag_Piezo_e.pdf), (Accessed Nov. 2, 2023).
- [17] G. J. L. Xiong and et. al., "Three-dimensional fiber sensor of the bragg grating friction force for the robot.," *Journal of Information Systems & Operations Management*, vol. 4, no. 2, pp. 99–107, 2010.
- [18] Y. C. S. Chong and J. Desai, "Miniature force sensor based on double photo damage with high linearity and interference compensation," pp. 736–747, 2016.
- [19] J. K. Y. Guo and et. al., "Three-axis force sensor at the fingertip based on fiber bragg grating," *Sensors and Actuators A: Physical*, vol. 249, pp. 141–148, 2016, ISSN: 0924-4247. DOI: <https://doi.org/10.1016/j.sna.2016.08.020>. [Online]. Available: <https://www.sciencedirect.com/science/article/pii/S0924424716303958>.

- [20] C. Yuan, L.-P. Luo, Q. Yuan, *et al.*, “Development and evaluation of a compact 6-axis force/moment sensor with a serial structure for the humanoid robot foot,” *Measurement*, vol. 70, pp. 110–122, 2015, ISSN: 0263-2241. DOI: <https://doi.org/10.1016/j.measurement.2015.03.027>. [Online]. Available: <https://www.sciencedirect.com/science/article/pii/S0263224115001736>.
- [21] L. Feng, A. Ba, W. Zhang, H. Pang, and T. Wang, “Design and optimization of a self-decoupled six-axis wheel force transducer for a heavy truck,” *Proceedings of the Institution of Mechanical Engineers, Part D: Journal of Automobile Engineering*, vol. 229, Feb. 2015. DOI: 10.1177/0954407014566439.
- [22] S. M. Nacy, M. A. Tawfik, and I. A. Baqer, “Static and dynamic calibration for flexiforce sensor using a special purpose apparatus,” *Innovative Systems Design and Engineering*, vol. 4, pp. 30–40, 2013. [Online]. Available: <https://api.semanticscholar.org/CorpusID:118367418>.
- [23] H. Oh, U. Kim, G. Kang, J. Seo, and H. Choi, “Multi-axial force/torque sensor calibration method based on deep-learning,” *IEEE Sensors Journal*, vol. PP, pp. 1–1, May 2018. DOI: 10.1109/JSEN.2018.2834727.
- [24] J. Ma and A. Song, “Fast estimation of strains for cross-beams six-axis force/torque sensors by mechanical modeling,” *Sensors*, vol. 13, May 2013.