

# A second degree polynomial passes through (0,1), (1,3), (2,7), (3,13). Find the polynomial.

we construct the difference table for the given data is as below:

$x$	$y$	$\Delta y$	$\Delta^2 y$	$\Delta^3 y$
0	1 = $y_0$			
1	3	2 = $\Delta y_0$		
2	7	4	2 = $\Delta^2 y_0$	
3	13	6	2	0 = $\Delta^3 y_0$

we know,

Newton's forward interpolation formula,

$$y(x) = y_0 + u \Delta y_0 + \frac{u(u-1)}{2!} \Delta^2 y_0 + \frac{u(u-1)(u-2)}{3!} \Delta^3 y_0 \quad (1)$$

where  $u = \frac{x-x_0}{h} = \frac{x-0}{1} = x$   $h = 1 - 0 = 1$   
 $x_0 = 0$

Now putting those values in equation (1)

$$y(x) = 1 + 2x + \frac{x(x-1)}{2} \times 2 + \frac{x(x-1)(x-2)}{6} \times 0$$

$$= 1 + 2x + x^2 - x$$

$$= 1 + x + x^2$$

$\therefore y(x) = x^2 + x + 1$ , which is the required polynomial.