

FEBRUARY 2022

02

Wednesday

Week 6 ■ 033-332

JANUARY

2022

Su	Mo	Tu	We	Th	Fr	Sa
30	31					1
2	3	4	5	6	7	8
9	10	11	12	13	14	15
16	17	18	19	20	21	22
23	24	25	26	27	28	29

Formal Languages & Automata TheoryModule 5 - Context Sensitive Languages,  
Turing machinesContext Sensitive grammar & language

Grammar,  $G = (V, T, P, S)$  is CSG, if it satisfies all of the following:

- LHS may contain terminals
- RHS should not contain  $\epsilon$ .
- $|\alpha| \leq |\beta|$

V - variables

T - terminals

 $P: \alpha \rightarrow \beta, \alpha, \beta \in (V \cup T)^+$  (production)

S - Start symbol.

Language produced by CSG  $\rightarrow$  CSL.

Automata - Linear Bounded Automata.

Type 1 grammar.

Properties of CSL

1) Union

2) Intersection

3) Concatenation

4) Complement.

MARCH

2022

Su	Mo	Tu	We	Th	Fr	Sa
		1	2	3	4	5
6	7	8	9	10	11	12
13	14	15	16	17	18	19
20	21	22	23	24	25	26
27	28	29	30	31		

2022 FEBRUARY

Thursday

Week 6 ■ 034-331

03

Linear Bounded Automata $M = (Q, \Sigma, T, \delta, q_0, M_L, M_R, F)$ 

Q - set of states

 $\Sigma$  - input symbols

T - Tape alphabets

 $\delta$  - transition function  $\rightarrow$  tape symbol $\delta(q, \text{tape symbol}) \rightarrow (q, t_1, c)$  $\downarrow$   
0, +1, -1. $\delta: (Q - F) \times T \rightarrow Q \times T \times \{L, R\}$  $\downarrow$   
excluding  
final state $\downarrow$   
direction $q_0$  - Start state $M_L$  - left marker $M_R$  - Right marker

F - final state

Tape length = length of input symbols.

$$\textcircled{A} \xrightarrow{a/x, \textcircled{D}} \textcircled{B} \quad \delta(q, a) = (q, x, D)$$

a - Input symbol

x - Replacement (tape symbol)

D - direction.



FEBRUARY 2022

04

Friday

Week 6 ■ 035-330

## Turing Machine

$M = (Q, \Sigma, \Gamma, \delta, q_0, B, F)$

$Q$  - set of state

$\Sigma$  - input symbols

$\Gamma$  - tape symbols

$\delta$  - Transition function

$\delta(q, x) = (p, y, D)$

$\nwarrow \nearrow$   
L R

$q_0$  - start symbol

$B$  - Blank symbol

$F$  - set of final states

Recursive language: Accepts all strings in 'L' & reject all strings not in 'L'.  
Will halt every time & give an answer.

Recursively enumerable: Accepts for all input strings in 'L'.  
May or may not halt for all input strings not in 'L'.

Decidable language  $\Leftrightarrow$  recursive language  
Partially decidable  $\rightarrow$  recursively enumerable  
Undecidable  $\rightarrow$  could be partially decidable but not decidable.  
 $\downarrow$   
not mandatory

JANUARY

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MARCH

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2022 FEBRUARY

Saturday

Week 6 ■ 036-329

05

## Universal Turing Machine

Input:  $M$  = Turing machine

$w$  = string given as input.

Action: Simulate  $M$

May accept, reject or loop.

UTM is a recognizer (not a decider) for

$A_{TM} = \{ \langle M, w \rangle \mid M \text{ is a TM \& } M \text{ accepts } w \}$

## The Halting problem

$\rightarrow$  Undecidable.

Let

$H(P, I)$

$\downarrow$  Halt

$\downarrow$  Not Halt

$C(x)$

if  $(H(x, x) == \text{Halt})$

loop forever;

else

return;

$C(C)$

$H(C, C) == \text{Halt}$

$\downarrow$   
Halt

$H(C, C) == \text{Not Halt}$

$\downarrow$   
Halt

Sunday 06

Week 7 ■ 037-328



FEBRUARY 2022  
07



Monday

Week 7 ■ 038-327

JANUARY

Su	Mo	Tu	We	Th	Fr	Sa
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## Chomsky Hierarchy

Regular  
(FA)

Context  
free  
(PDA)

Context  
Sensitive  
(LBA)

Recursively  
enumerable  
(TM)