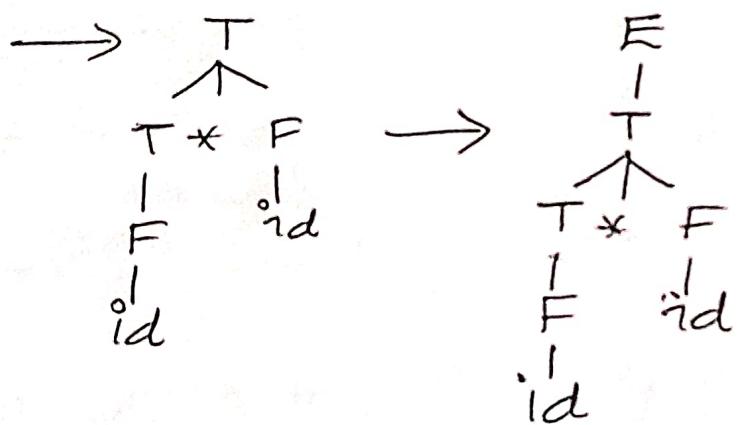
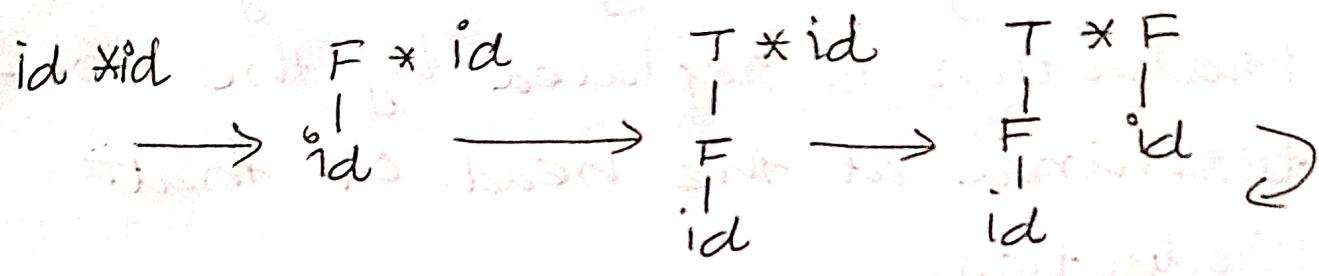


Bottom-up Parsing

Module 3

It is the construction of a parse tree for an input string beginning at the leaves (the bottom) and working up towards the root (the top).



For the grammar,

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid \text{id}$$

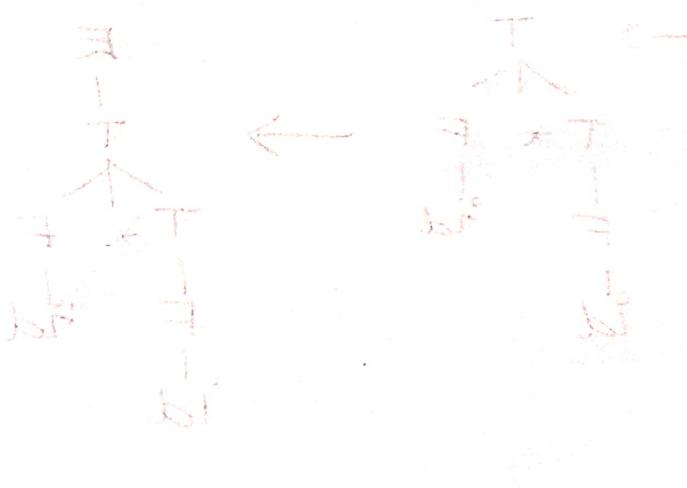
A bottom-up parse for $\text{id} * \text{id}$.

- The above grammar cannot be used for top-down parsing, b'coz its left recursive.
- Also known as Shift-Reduce parsing.
- It allows Right Most Derivation in reverse Order.

Reductions

Bottom-up parsing as the process of reducing a string w to the start symbol of the grammar.

At each reduction step, a specific substring matching the body of a production is replaced by the non-terminal at the head of that production.



Bottom-up parsing is called bottom-up because it starts with the start symbol and reduces it to the terminal symbols.

Bottom-up parsing is also called leftmost derivation because it always derives the leftmost symbol first. This is in contrast to rightmost derivation which always derives the rightmost symbol first.

Bottom-up parsing is often used in compilers to parse programs. It is also used in some natural language processing systems. Bottom-up parsing is generally more efficient than top-down parsing because it does not need to keep track of all possible derivations. However, it can be more difficult to implement than top-down parsing.

Handle Pruning

Bottom-up parsing during a left to right scan of the input constructs a right most derivation in reverse.

A handle is a substring that matches the body of a production whose reduction represents one step along the reverse of a rightmost derivation.

Example

$$\begin{array}{l} S \rightarrow aABe \\ A \rightarrow Abc/b \\ B \rightarrow d \end{array}$$

input string 'abbcde'

handles during parsing of abbcde

Right sentential form	Handle	Reducing production
abbcde	b	$A \rightarrow b$
a <u>A</u> bcde	Abc	$A \rightarrow Abc$
a A <u>d</u> e	d	$B \rightarrow d$
<u>aABe</u>	aABe	$S \rightarrow aABe$

\xrightarrow{S}
start symbol

Example 2

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid id$$

input 'id * id'

Right
Sentential form

Handle

Reducing
Production

id * id

id

$F \rightarrow id$

$F * id$

F

$T \rightarrow F$

$T * id$

id

$F \rightarrow id$

$T * F$

$T * F$

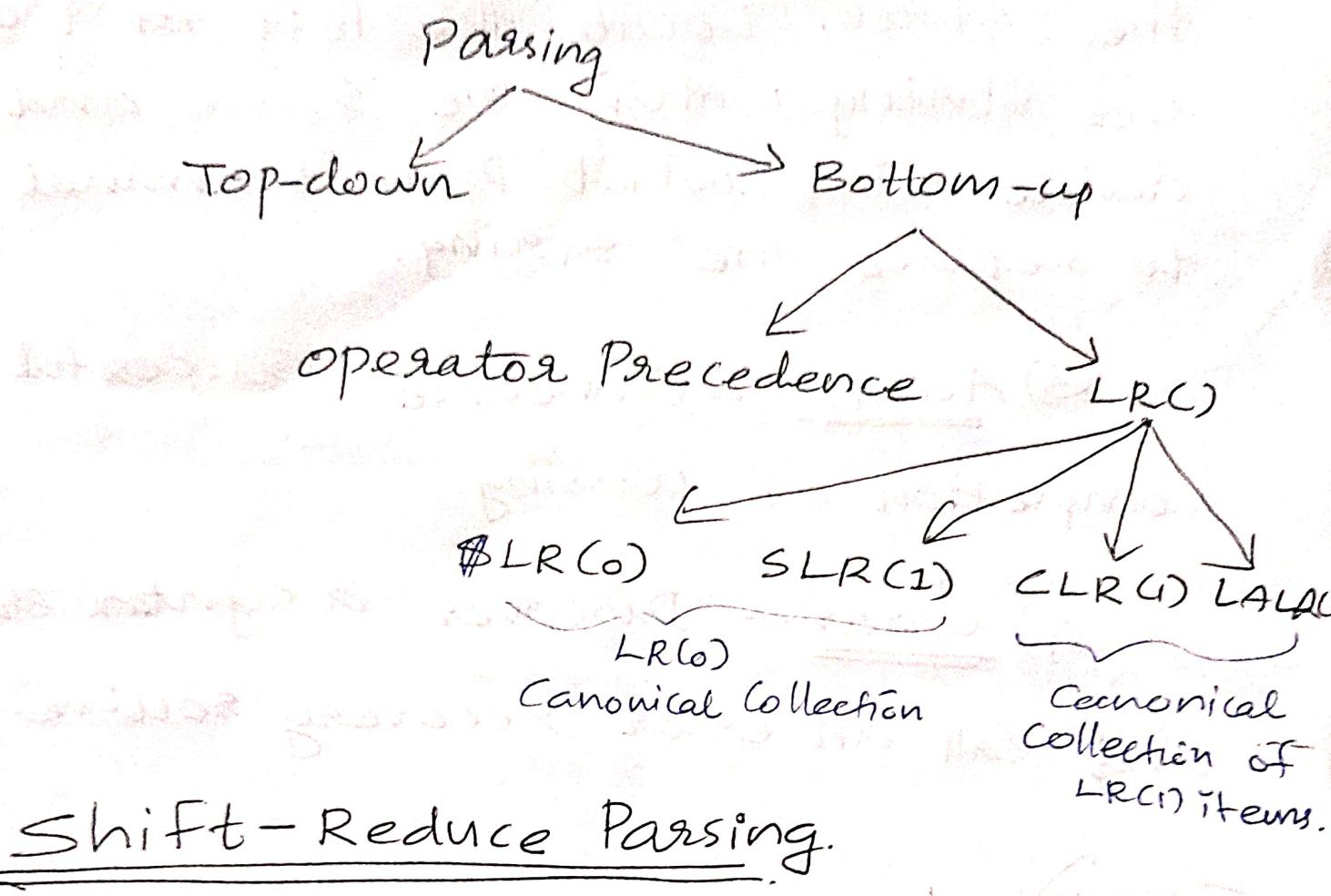
~~\overline{T}~~
 ~~$\overline{*}$~~
 $T \rightarrow T * F$

T

$E \rightarrow T$

E

→ start
symbol.



Shift-Reduce Parsing.

S-R parsing is a form of bottom-up parsing in which stack holds grammar symbols and an input buffer holds the rest of the string to be parsed.

Mainly two data structures

Actions of S-R parser

- 1) Shift - shift the next input symbol onto the top of the stack.
- 2) Reduce - The right end of the string to be reduced must be at

the stack. Locate the left end of the string within the stack and decide with what non-terminal to replace the string.

3) Accept — Announce successful completion of parsing.

4) Error — Discover a syntax error and call an error recovery routine.

Example 1

$$\begin{array}{l} E \rightarrow E + T / T \\ T \rightarrow T * F / F \\ F \rightarrow (E) / id \end{array}$$

input string

"id * id"

stack	Input buffer	Action
\$	id * id \$	Shift
\$ id	* id \$	Reduce $F \rightarrow id$
\$ F	* id \$	Reduce $T \rightarrow F$
<u>① \$ T</u>	* id \$	Shift
\$ T *	id \$	Shift
\$ T * id	\$	Reduce $F \rightarrow id$
<u>② \$ T * F</u>	\$	Reduce $T \rightarrow T * F$
\$ T	\$	Reduce $E \rightarrow T$
\$ E	\$	Accepted.

① Shift-reduce conflict.

② Reduce-reduce conflict.

Example 2

$$S \rightarrow (L) / a$$

$$L \rightarrow L, S / S$$

parse the input string $(a, (a, a))$
using shift-reduce parser.

Stack	Input buffer	Action
\$	$(a, (a, a))\$$	Shift
\$C	$a, (a, a))\$$	Shift
\$(\$a	$, (a, a))\$$	Shift
\$(\$a,	$, (a, a))\$$	Reduce $S \rightarrow a$
\$(\$S	$; (a, a))\$$	Reduce $S \rightarrow a$
\$(\$L	$; (a, a))\$$	Shift
\$(\$L,	$(a, a))\$$	Shift
\$(\$L, ($a, a))\$$	Shift
\$(\$L, (a	$, a))\$$	Reduce $S \rightarrow a$
\$(\$L, (\$	$, a))\$$	Reduce $L \rightarrow S$
\$(\$L, \$L	$, a))\$$	Shift

$\$ (L, (L,$	a)) \$	shift
$\$ (L, (L, a$)) \$	Reduce $S \rightarrow a$
$\$ (L, (L, S$)) \$	Reduce $L \rightarrow S$
$\\$ (L, (L, L$)) \$	shift
$\\$ (L, (L,)$		
$\$ (L, (L$)) \$	shift
$\$ (L, (L)$) \$	Reduce $S \rightarrow (L)$
$\$ (L, S$) \$	Reduce $L \rightarrow S$
$\$ (L$) \$	shift
$\$ (L)$	\$	Reduce $S \rightarrow (L)$
$\$ S$	\$	<u>Accepted.</u>
$\underline{\underline{=}}$		

Operator Precedence Parsing.

- It is applied to a small class of operator grammars.
- A grammar is said to be Operator precedence grammar if it has 2 properties :
- i) No RHS of any production has an ϵ .
 - ii) No two non-terminals are adjacent.
- Operator precedence can only be established b/w the terminals of the grammar. It ignores the non-terminals.

Example:

$$E \rightarrow EAE / (E) / -E / id$$

$$A \rightarrow + / - / * / / \uparrow$$

is not an operator grammar, b'coz the right side EAE has two consecutive non-terminals.

If we substitute for A, each of its alternates, we obtain

$$E \rightarrow E + E / E \rightarrow E / E * E / E / E / E \uparrow E /$$

$$(E) / -E / id$$

→ There're certain disadvantages for this parsing technique, such as it is hard to handle tokens like the minus sign which has two different precedences.

→ only a small class of grammars can be parsed using this technique.

→ we use three disjoint precedence relations: $<$, $=$ and $>$, between certain pairs of terminals.

→ These precedence relations guide the Selection of handles.

Rule 1:

- If $a < b$: 'a yields precedence to b'
- If $a = b$: 'a has same precedence as b'
- If $a > b$: 'a takes precedence over b'.

Rule 2:

- An identifier (id) is always given the higher precedence than any other symbol.
- \$ - always lower precedence.

Rule 3:

If two operators have the same precedence, check their associativity.

Left associative — Operators are evaluated from left to right.

Right associative — Operators are evaluated from right to left.

$$E \rightarrow E + E \mid E * E \mid id$$

operator precedence relation table:

	+	*	id	\$	Top buffer
+	>	<	<	>	Push buffer
*	>	>	<	>	Pop buffer
id	>	>	—	>	Pop buffer
\$	<	<	<	Accepted	

Stack:

id, a, b... - higher prec.

\$ - lower precedence.

+ > +

associativity - from left to right

+ < *

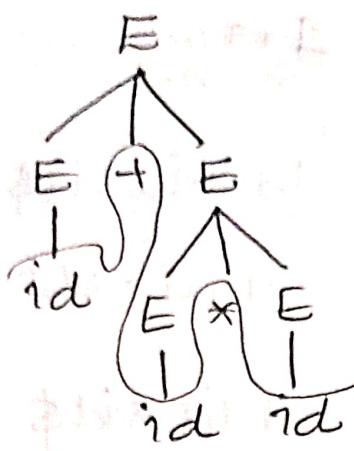
* > *

left associative

Parsing the input string

Stack	Relation \leq	Input string	Operation
\$	<	<u>id + id * id \$</u>	Shift id
\$ id	>	+ id * id \$	Reduce $E \rightarrow id$
\$ E	<	+ id * id \$	Shift +
\$ E +	<	<u>id * id \$</u>	Shift id
\$ E + id	>	* id \$	Reduce $E \rightarrow id$
\$ E + id	<	* id \$	Shift λ
\$ E + E	<	<u>id \$</u>	Shift id
\$ E + E *	>	\$	Reduce $E \rightarrow id$
\$ E + E * id	>	\$	Reduce $E \rightarrow E * E$
\$ E + E * E	>	\$	Reduce $E \rightarrow E + E$
\$ E + E * E	>	\$	Reduce $E \rightarrow E + E$
\$ E		\$	<u>A Ccepted</u>

Parse tree.



id + id * id

Precedence and Associativity

Parsers that evaluate expressions usually have to establish the order in which various operations are carried out.

Precedence —

It dictates which of two different operations is to be carried out first.

Eg:- A+B*C

Associativity -

It indicates which of two similar operations is to be carried out first.

Eg: $A - B - C$

can be operated as

$(A - B) - C$. // in C language.

$A - (B - C)$ // in APL or FORTRAN.

Associativity in CFG

$\langle \text{Expr} \rangle \rightarrow \langle \text{term} \rangle / \langle \text{expr} \rangle + \langle \text{term} \rangle /$

$\langle \text{expr} \rangle - \langle \text{term} \rangle$

$\langle \text{terms} \rangle \rightarrow \langle \text{factor} \rangle / \langle \text{terms} \rangle * \langle \text{factor} \rangle /$

$\langle \text{term} \rangle / \langle \text{factor} \rangle$

$\langle \text{factor} \rangle \rightarrow \langle \text{number} \rangle / (\langle \text{expr} \rangle)$

$\langle \text{number} \rangle \rightarrow \langle \text{digit} \rangle / \langle \text{number} \rangle \langle \text{digit} \rangle$

$\langle \text{digit} \rangle \rightarrow 0/1/2/3/4/5/6/7/8/9$

All operators have same precedence here
And no associativity definitions also.

So all undefined categories are included
in ambiguous grammar.

$(=)$	$\$ < id$	$\theta < C$ —
$(< ($	$) > \$$	$C < \theta$ —
$(< id$	$) >)$	$\theta >)$ —
$\$ < ($		
$id >)$		

~~P-Q → Jan 2024~~
Illustrate actions according to operator
precedence parser for the input
 $id_1 + id_2 * id_3$ based on the given
grammar $E \rightarrow E+E | E*E | (E) | id$