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# Abstract

This project deals with the designing of the finite impulse response (FIR) bandpass filter. The FIR filter is designed using windowing method in conjunction with the kaiser window. The corresponding theories are going to be explained according to the prescription that is provided. Matlab R2018a is used for demonstrations and, the figures shown below are the corresponding outputs given by the Matlab R2018a. The codes are included in the appendix.

# Introduction

A filter is a component which eliminates the undesired parts of the input signal with respect to the users requirements. The digital filters can be separated by considering the impulse response as[1],

- finite impulse response (FIR) filters and
- infinite impulse response (IIR) filters.

In this report it is going to deal with a FIR bandpass filter in conjunction with the kaiser window. Kiser window method is one of the most fascinating techniques.

# Basic Theories

This chapter is cited: A. Antoniou's book [1]. The design process of the finite impulse response filters can be categorised into two classical methods.

1. Fourier series method or Window method.
2. Weighted-Chebyshev method.

The Fourier series is used in the first method and it will be discussed further with the basic theories later. The weighted-Chebyshev method is a multivariable optimization method. In order to that window functions are conjuncted with the Fourier series method.

## 3.1 Design Using the Fourier Series

The digital filters have a periodic frequency response. The period is equal to the sampling frequency hence, the frequency response can be denoted as a Fourier series as below.

By substituting  $z=e^{j\omega T}$  to the impulse response of the filter, transfer function can be obtained.

There are two major consequences with this Fourier series method that can be shown because, the Fourier series coefficients have been defined over the range  $-\infty$  to  $+\infty$ .

- The nonrecursive filter obtained is of infinite length.



- The filter is noncausal because the impulse response is nonzero for negative time.

To overcome these problems, the impulse response has truncated. And a causal filter can be obtained by delaying the impulse response or by sampling periods appropriately.

## 3.2 Use of Window Functions

The oscillations can be found in the passband and the stopband. It is because of the slow convergence of the fourier series. These are called Gibb's oscillations and the effect of Gibb's oscillations[2] can be reduced by the complex-convolution with a discrete-time window function.

The above euation can be interpreted in such a way that illustrates the effect of the window spectrum on the frequency response of the filter.

A variety of such windows has been observed and used over the years. Some significant and common windows are listed below.

1. Rectangular.
2. von Hann<sup>2</sup>.
3. Hamming.
4. Blackman.
5. Dolph-Chebyshev.
6. Kaiser.

### 3.2.1 Kaiser Window

Kaiser window is an one of the most widely used window in fir filter designing. It can be easily achieved the prescribed specifications by using the kaiser window method. This is cited:[3]. The window function is given by,

where alpha is an independent parameter. The zero-th order, first kind of Bessel function is denoted by the  $J_0$ . The value of beta and the Bessel function are given in the following manner.

### **3.3 Design of Prescribed Bandpass Filter**

The designing procedure of the prescribed filter by using Kaiser window will be explained. The required parameters would give as below.

The above parameters are demonstrated by using a graph for further clarifications in the figure.

Figure 3.1: Bandpass filter parameters

Now, the design of prescribed bandpass filter design can be started.

#### **3.3.1 Determine the Impulse Response.**

The minimum transition width  $B_t$  is given by the first equation. The frequency response of a band pass filter is given below. The impulse response can be determined by applying the Fourier series. The lower and upper cutoff frequencies approximate as follow.

The impulse response for a bandpass filter can be determined as below.

#### **3.3.2 Choose the Delta**

Delta can be calculated using the following equations. Then the actual stopband loss of the filter can be determined.

#### **3.3.3 Chose the Alpha**

The independent variable alpha should determine at this stage. The following conditions must consider when calculating the alpha.

### **3.3.4 Determine the parameter D**

It is the last parameter to determine before move in to the kaiser window calculations. The parameter D can be obtained after checking these conditions.

The N must satisfy the following inequality as well.

### **3.3.5 Apply the Kaiser Window**

Finally, compute the kaiser window by using the above determined parameters. It is the last step and the filter has been designed.

# Results

The given parameters and their calculated values are showing in the table. The index is taken as a user input and calculated the rest by using Matlab R2018a installed version.

Parameter	Value
Passband Ripple	0.0900 dB
Minimum Stop Band Attenuation	45 dB
Lower passband edge	1200 rad/s
Lower stopband edge	1600 rad/s
Upper stopband edge	1050 rad/s
Upper passband edge	1700 rad/s
Sampling frequency	4200 rad/s

The required impulse response and its frequency domain representation is showing in the figure.

Figure 4.1: Impulse response.

The time domain representation of the bandpass kaiser window is showing in the figure.

Figure 4.2: Bandpass kaiser window.

The impulse response of the kaiser window and its frequency domain representation are showing in the figure.

Figure 4.3: Impulse response of the kaiser window

The figure is showing the passband, lower stopband and upper stopband in the frequency domain.

Figure 4.4: Passband, lower stopband and upper stopband

The figure is showing the ideal outputs of the filter.

Figure 4.5: Ideal outputs

Finally, demonstrate the filter behaviour by using a sample signal and the output is showing in the figure.

Figure 4.6: sample signal's filtered output.

The filter output in the frequency domain.

Figure 4.7: Filter output in the frequency domain

# Conclusion

Kaiser Window technique is an effective method of planning a FIR filter under the closed form direct methodology, because of its adaptability, the design can oblige many plan prerequisites that are determined on the filter. It is additionally seen that the computational exertion of designing a filter in this strategy is little. Anyway the major downside of this filter configuration is the high order of filter required. There can be ideal filters of lower request that can accomplish similar determinations. At the point when actualized in equipment higher request filters can be wasteful because of the use of more unit delay adders and multipliers. In the product usage, higher order filters require more calculations per test. Further developed plan procedures must be utilized all together to get optimality.

# Bibliography

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- [3] UKEssays. (November 2018). Filter Design Using Rectangular Window And Kaiser Window Marketing Essay.  
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# **Appendix**

## **A.1 Matlab Code**