

Math Exercise

1. $[25, 2, -3, -23]$

2. 2×4

3. 2×3

4. $u + v = (-0.5, 1.5)$

$v + w = (5.5, 2.5)$

$u + w = (2, 1)$

$u + v + w = (3.5, 2.5)$

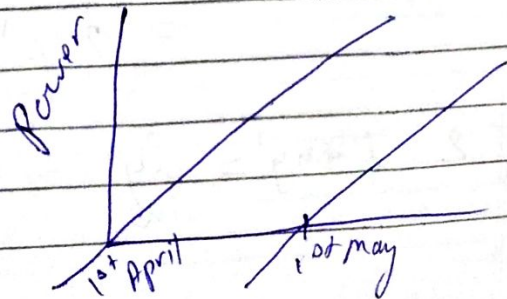
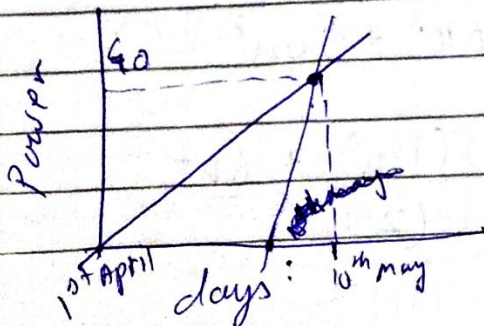
Jill problem

~~Let y is the power generated by~~

1) 10th May

2) • Total Energy = $40 \text{ kJ} + 40 \text{ kJ} = 80 \text{ kJ}$

3) Mark II will never be able to generate power as much as Mark I



Calculus - Problem

$$1. \frac{dy}{dn} = -15n^2$$

$$2. \frac{dy}{dn} = 4n + 2$$

$$3. \frac{dy}{dn} = 50n^4 - 18n^2 - 1$$

$$4. \frac{dy}{dn} = 2n + 2$$

$$\left. \frac{dy}{dn} \right|_{n=2} = 4 + 2 = 6$$

$$\left. \frac{dy}{dn} \right|_{n=1} = 2 \times (-1) + 2 = 0$$

Calculus Problem

$$\begin{aligned}
 1. \quad f'(n) &= \frac{dy}{dn} = (2n^3 + 5n^2)(4n + 6) + (2n^2 + 6n)(8n^2 + 10n) \\
 &= 8n^4 + 20n^3 + 12n^3 + 30n^2 \\
 &\quad + 12n^4 + 36n^3 + 20n^3 + 60n^2 \\
 &= 20n^4 + 88n^3 + 90n^2
 \end{aligned}$$

$$2. \quad \frac{dy}{dn} = \frac{(2-n)(18n) + 6n^2}{(2-n)^2}$$

$$= \frac{36n - 18n^2 + 6n^2}{(2-n)^2}$$

$$= \frac{36n - 12n^2}{(2-n)^2}$$

$$3. \quad \frac{dy}{dx} = 2(3n+1) \times 3 = 6(3n+1)$$

$$4. \quad g' = \frac{dy}{dx} = 6(n^2+5n)^5 (2n+5)$$

$$5. \quad f'(n) = \frac{d}{dn} f(n) = -1(n^4+1)^5 + 7 \times 5(n^4+1)^4 \times 4n^3$$

$$= \frac{-20n^3(n^4+1)^4}{(n^4+1)^5 + 7}$$

Z-score :- Z-score tells how many standard deviations away a data point is from the mean.

$$Z\text{-score} = \frac{(n - \text{mean})}{\text{std. deviation}}$$

Outliners :- If the Z score of a point is more than 3, it indicates that the data point is quite different from the other data points. Such a data point can be an outlier.

p-value: helps us determine how likely it is to get a particular result when the null hypothesis is assumed to be true. It is the probability of getting a sample like ours or more extreme than ours if the null hypothesis is correct. Therefore, if the null hypothesis is assumed to be true, the p-value gives us an estimate of how "strange" our sample is.

If the p-value is very small (≤ 0.05), then our sample is strange, and this means that our assumption that the null hypothesis is correct is most likely to be false. Thus we reject it.

Comparing Means with t-tests

The t-test is a common method for comparing the mean of one group to a value or the mean of one group to another. T-test are very useful because they usually perform well in the face of minor to moderate departure from normality of the underlying group distribution.

Suppose you have two independent Groups:

	Group 1	Group 2
mean	\bar{x}_1	\bar{x}_2
variance	s_1^2	s_2^2

$$t\text{-test} = T = \frac{|\bar{x}_1 - \bar{x}_2|}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

Where n_1 : no. of sample in Group 1
 n_2 : no. of samples in Group 2

Confidence Interval

A confidence interval is how much uncertainty there is with any particular statistic. Confidence intervals are often used with a margin of error. It tells you how confident you can be that the results from a poll or survey reflect you would expect to find if it were possible to survey the entire population.

If you have one small set of data, we will use the t-distribution instead of normal distribution.

$$C.I = \bar{x} \pm t \frac{s}{\sqrt{n}}$$

ANOVA Test

An ANOVA test is a way to find out if survey or experiment results are significant. In other words, they help you to figure

out if you need to reject null hypothesis or accept the alternate hypothesis.

$$F = \frac{\text{Between group variation}}{\text{Within group variation}}$$

Null hypothesis

It is a type of conjecture used in statistics that propose that there is no difference between certain characteristic of a population or data-generating process.

Alternative hypothesis

Alternative hypothesis is just an alternative to the null hypothesis.

Random Variable :- It is a variable whose value is unknown or a function that assign values to each of an experiment's outcomes. A random variable is most common in probability and

Discrete vs. Continuous Variable

If a variable can take on any value between two specified values it is called a continuous variable. Otherwise, it is called a discrete variable.

Probability Mass Function

It is the function which describes the probability associated with the random variable x .

$P(X=x)$ corresponds to the probability that the random variable x takes the value x .

Probability Density function

Some variables are not discrete. They can take on an infinite number of values in certain ranges. But we still need to describe the probability associated with it.

The equivalent of the probability mass function for continuous variables is called the probability density function.

Expected value

The expected value of a random variable X , denoted $E[X]$, is a generalization of the weighted average, and is intuitively the arithmetic mean of a large number of independent realizations of X .