

2024-January Session-01-30-2024-shift-1

EE24BTECH11008-ASLIN GARVASIS

- 1) A line passing through the point A (9, 0) makes an angle of 30° with the positive direction of x-axis. If this line is rotated about A through an angle of 15° in the clockwise direction, then its equation in the new position is
 - a) $\frac{y}{\sqrt{3}-2} + x = 9$
 - b) $\frac{x}{\sqrt{3}-2} + y = 9$
 - c) $\frac{x}{\sqrt{3}+2} + y = 9$
 - d) $\frac{y}{\sqrt{3}+2} + x = 9$
- 2) Let S_n denote the sum of first n terms of an arithmetic progression. If $S_{20} = 790$ and $S_{10} = 145$, then $S_{15} - S_5$ is :
 - a) 395
 - b) 390
 - c) 405
 - d) 410
- 3) If $z = x + iy$, $xy \neq 0$, satisfies the equation $z^2 + i\bar{z} = 0$, then $|z^2|$ is equal to :
 - a) 9
 - b) 1
 - c) 4
 - d) $\frac{1}{4}$
- 4) Let $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$ and $\vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$ be two vectors such that $|\vec{a}| = 1$; $\vec{a} \cdot \vec{b} = 2$ and $|b| = 4$. If $\vec{c} = 2(\vec{a} \times \vec{b}) - 3\vec{b}$, then the angle between \vec{b} and \vec{c} is equal to :
 - a) $\cos^{-1}\left(\frac{2}{\sqrt{3}}\right)$
 - b) $\cos^{-1}\left(\frac{-1}{\sqrt{3}}\right)$
 - c) $\cos^{-1}\left(\frac{-\sqrt{3}}{2}\right)$
 - d) $\cos^{-1}\left(\frac{2}{3}\right)$
- 5) The maximum area of a triangle whose one vertex is at (0,0) and the other two vertices lie on the curve $y = -2x^2 + 54$ at points (x,y) and (-x,y) where $y > 0$ is :
 - a) 88
 - b) 122
 - c) 92
 - d) 108
- 6) The value of $\lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{n^3}{(n^2+k^2)(n^2+3k^2)}$ is
 - a) $\frac{(2\sqrt{3}+3)\pi}{24}$
 - b) $\frac{13\pi}{8(4\sqrt{3}+3)}$
 - c) $\frac{13(2\sqrt{3}-3)\pi}{8}$
 - d) $\frac{\pi}{8(2\sqrt{3}+3)}$
- 7) Let $g : \mathbf{R} \rightarrow \mathbf{R}$ be a non constant twice differential such that $g'\left(\frac{1}{2}\right) = g'\left(\frac{3}{2}\right)$. If a real valued function f is defined as $f(x) = \frac{1}{2}(g(x) + g(2-x))$, then
 - a) $f'(x) = 0$ for atleast two x in $(0, 2)$
 - b) $f'(x) = 0$ for exactly one x in $(0, 1)$
 - c) $f'(x) = 0$ for no x in $(0, 1)$
 - d) $f'\left(\frac{3}{2}\right) + f'\left(\frac{1}{2}\right) = 1$
- 8) The area (in square units) of the region bounded by the parabola $y^2 = 4(x-2)$ and the line $y = 2x - 8$
 - a) 8
 - b) 9
 - c) 6
 - d) 7
- 9) Let $y = y(x)$ be the solution of the differential equation $\sec x dy + \{2(1-x)\tan x + x(2-x)\} dx = 0$ such that $y(0) = 2$. Then $y(2)$ is equal to :
 - a) 2
 - b) $2\{1 - \sin(2)\}$
 - c) $2\{\sin(2) + 1\}$
 - d) 1
- 10) Let (α, β, γ) be the foot of perpendicular from the point (1, 2, 3) on the line $\frac{x+3}{5} = \frac{y-1}{2} = \frac{z+4}{3}$, then $19(\alpha + \beta + \gamma)$ is equal to :

- a) 102
- b) 101
- c) 99
- d) 100

d) $\frac{2}{\sqrt{5}}$

- 11) Two integers x and y are chosen with replacement from the set $\{0, 1, 2, 3, \dots, 10\}$. Then the probability that $|x - y| > 5$ is :

- a) $\frac{30}{121}$
- b) $\frac{62}{121}$
- c) $\frac{60}{121}$
- d) $\frac{31}{121}$

- 12) If the domain of the function

$$f(x) = \cos^{-1}\left(\frac{2 - |x|}{4}\right) + (\log_e(3 - x))^{-1}$$

is $[\alpha, \beta] - \{y, \beta\}$, then $\alpha + \beta + \gamma$ is equal to :

- a) 12
- b) 9
- c) 11
- d) 8

- 13) Consider the system of linear equation $x + y + z = 4\mu$, $x + 2y + 2\lambda z = 10\mu$, $x + 3y + 4\lambda^2 z = \mu^2 + 15$ where $\lambda, \mu \in \mathbf{R}$. Which one of the following statements is NOT correct ?

- a) The system has unique solution if $\lambda \neq \frac{1}{2}$ and $\mu \neq 1, 15$
- b) The system is inconsistent if $\lambda = \frac{1}{2}$ and $\mu \neq 1$
- c) The system has infinite number of solutions if $\lambda = \frac{1}{2}$ and $\mu = 15$
- d) The system is consistent if $\lambda \neq \frac{1}{2}$

- 14) If the circles $(x + 1)^2 + (y + 2)^2 = r^2$ and $x^2 + y^2 - 4x - 4y + 4 = 0$ intersect at exactly two distinct points, then

- a) $5 < r < 9$
- b) $0 < r < 7$
- c) $3 < r < 7$
- d) $\frac{1}{2} < r < 7$

- 15) If the length of the minor axis of ellipse is equal to half of the distance between the foci, then the eccentricity of the ellipse is :

- a) $\frac{\sqrt{5}}{3}$
- b) $\frac{\sqrt{3}}{2}$
- c) $\frac{1}{\sqrt{3}}$