Chapter-16 Application of Derivatives

EE24BTECH11008-ASLIN GARVASIS

9)	The slope of the tangent to a curve $y = f(x)$ at $[x, f(x)]$
	is $2x + 1$. If the curve passes through the point $(1, 2)$, then
	the area bounded by the curve, the x axis and the line
	x = 1 is

(1995S)

- a) $\frac{5}{6}$ b) $\frac{6}{5}$ c) $\frac{1}{6}$

- 10) If $f(x) = \frac{x}{\sin x}$ and $g(x) = \frac{x}{\tan x}$, where $0 < x \le 1$, then in

(1997-2 Marks)

- a) both f(x) and g(x) are increasing functions
- b) both f(x) and g(x) are decreasing functions
- c) f(x) is an increasing function
- d) g(x) is an increasing function
- 11) The function $f(x) = \sin^4 x + \cos^4 x$ increases if

(1999-2 Marks)

- a) $0 < x < \frac{\pi}{8}$
- 12) Consider the following statements in S and R
 - S: Both $\sin x$ and $\cos x$ are decreasing functions in the interval $(\frac{\pi}{2}, \pi)$

R: If a differentiable function decreases in an interval (a,b), then its derivative also decreases in (a,b)

Which of the following is true?

- a) Both S and R are wrong
- b) Both S and R are correct, but R is not the correct explanation of S
- c) S is correct and R is the correct explanation for S
- d) S is correct and R is wrong
- 13) Let $f(x) = \int e^x (x-1)(x-2) dx$ Then f decreases in the interval (2000S)
 - a) $(-\infty, -2)$
 - b) (-2, -1)
 - (1,2)
 - d) $(2, +\infty)$
- 14) If the normal to the curve y = f(x) at the point (3,4) makes an angle $\frac{3\pi}{4}$ with the positive x- axis, then f'(3) =(2000S)
 - a) -1

- b) $\frac{-3}{4}$ c) $\frac{4}{3}$

15)

$$Let f(x) = \begin{cases} |x| & \text{for } 0 < x \le 2, \\ 1 & \text{for } x = 0 \end{cases}$$

Then at x = 0, f has

(2000S)

- a) a local maximum
- b) a local minimum
- c) no local maximum
- d) no extremum

16) For all
$$x \in (0, 1)$$
 (2000S)

- a) $e^x < 1 + x$
- b) $\log_{e} (1 + x) < x$
- c) $\sin x > x$
- d) $\log_e(x) > x$

17) If
$$f(x) = xe^{x(1-x)}$$
, then $f(x)$ is (2001S)

- a) increasing on $\left[\frac{-1}{2}, 1\right]$ b) decreasing on R
- c) increasing on R
- d) decreasing on $\left[\frac{-1}{2}, 1\right]$
- 18) The tiangle formed by the tangent to the curve $f(x) = x^2 + bx - b$ at the point (1, 1) and the coordinate axes, lies in the first quadrant. If its area is 2, then the value ofb is (2001S)
 - a) -1
 - b) 3
 - c) -3
- 19) Let $f(x) = (1 + b^2)x^2 + 2bx + 1$ and let m(b) be the minimum value of f(x). As b varies, the range of m(b)
 - a) [0, 1]
 - b) $(0,\frac{1}{2})$
 - c) $\left[\frac{1}{2}, 1\right]$
- 20) The length of a longest interval in which the function $3 \sin x - 4 \sin^3 x$ is increasing, is
 - a) $\frac{\pi}{3}$

 - c) $\frac{3\pi}{2}$

- d) π
- 21) The point(s) on the curve $y^3 + 3x^2 = 12y$ where the tangent is vertical, is(are)

 - a) $\left(\pm \frac{4}{\sqrt{3}}, -2\right)$ b) $\left(\pm \sqrt{\frac{11}{3}}, 1\right)$ c) (0, 0)d) $\left(\pm \frac{4}{\sqrt{3}}, 2\right)$
- 22) In [0,1] Lagranges Mean Value Theorem is NOT applicable to (2003S)
 - a) $f(x) = \begin{cases} \frac{1}{2} - x & x < \frac{1}{2} \\ \left(\frac{1}{2} - x\right)^2 & x \ge \frac{1}{2} \end{cases}$
 - b) $f(x) = \begin{cases} \frac{\sin x}{x} & x \neq 0\\ 1 & x = 0 \end{cases}$
 - c) f(x) = x|x|
 - d) f(x) = |x|
- 23) A tangent is drawn to ellipse $\frac{x^2}{27} + y^2 = 1$ at $\left(3\sqrt{3}\cos\theta, \sin\theta\right) \left(where\theta \in \left(0, \frac{\pi}{2}\right).\right)$ Then the value of θ such that sum of intercepts on axes made by this (2003S)tangent is minimum, is

 - a) $\frac{\pi}{3}$ b) $\frac{\pi}{6}$ c) $\frac{\pi}{8}$ d) $\frac{\pi}{4}$