2021-March Session-03-16-2021-shift-1

EE24BTECH11008-ASLIN GARVASIS

- 16) Let [x] denote greatest integer less than or equal to x. If for $n \in \mathbb{N}$, $(1 - x + x^3)^n = \sum_{j=0}^{3n} a_j x^j$, then $\sum_{j=0}^{\left[\frac{3n}{2}\right]} a_{2j} + 4\sum_{j=0}^{\left[\frac{3n-1}{2}\right]} a_{2j} + 1$ is
 - a) 2
 - b) 2^{n-1}
 - c) 1
 - d) n
- 17) If y = y(x) is the solution of the differential equation, $\frac{dy}{dx} + 2y \tan x = \sin x, y\left(\frac{\pi}{3}\right) = 0$, then the maximum value of the function y(x) over R is equal to:
 - a) 8
 - b) $\frac{1}{2}$
 - c) $-\frac{15}{4}$ d) $\frac{1}{8}$
- 18) The locus of the midpoints of the chord of the circle, $x^2 + y^2 = 25$ which is tangent to the hyperbola, $\frac{x^2}{9} - \frac{y^2}{16} = 1$ is :
 - a) $(x^2 + y^2)^2 16x^2 + 9y^2 = 0$
 - b) $(x^2 + y^2)^2 9x^2 + 144y^2 = 0$
 - c) $(x^2 + y^2)^2 9x^2 16y^2 = 0$
 - d) $(x^2 + y^2)^2 9x^2 + 16y^2 = 0$
- 19) The number of roots of the equation, $(81)^{\sin^2 x} + (81)^{\cos^2 x} = 30$ in the interval $[0, \pi]$ is equal to:
 - a) 3
 - b) 4
 - c) 8
 - d) 2
- 20) Let $\mathbf{S}_k = \sum_{r=1}^k \tan^{-1} \left(\frac{6^r}{2^{2r+1} + 3^{2r+1}} \right)$. Then $\lim_{k \to \infty} \mathbf{S}_k$ is equal to:
 - a) $tan^{-1}\left(\frac{3}{2}\right)$ b) $\frac{\pi}{2}$

- c) $\cot^{-1}(\frac{3}{2})$ d) $\tan^{-1}(3)$
- 21) Consider an arithmetic series and a geometric series having four initial terms from the set [11, 8, 21, 16, 26, 32, 4]. If the last terms of these series are the maximum possible four digit numbers, then the number of common terms in these two series is equal to ...

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22) Let $f:(0,2) \to \mathbf{R}$ be defined as

$$f(x) = \log_2\left(1 + \tan\left(\frac{\pi x}{4}\right)\right).$$

Then, $\lim_{n\to\infty} \frac{2}{n} \left(f\left(\frac{1}{n}\right) + f\left(\frac{2}{n}\right) + \dots + f(1) \right)$ is equal to ...

- 23) Let ABCD be a square of side of unit length. Let a circle C_1 centered at A with unit radius is drawn. Another circle C_2 which touches C_1 and the lines AD and AB are tangent to it, is also drawn. Let a tangent line from the point C to the circle C_2 meet the side AB at E. If the length of EB is $\alpha + \sqrt{3}\beta$, where α, β are integers, then $\alpha + \beta$ is equal to ...
- 24) If $\lim_{x\to 0} \frac{ae^x b\cos x + ce^{-x}}{x\sin x} = 2$, then a+b+c is equal to ...
- 25) The total number of 3X3 matrices A having entries from the set (0, 1, 2, 3) such that the sum of all the diagonal entries of AA^T is 9, is equal to ...
- 26) Let

$$P = \begin{bmatrix} -30 & 20 & 56 \\ 90 & 140 & 112 \\ 120 & 60 & 14 \end{bmatrix} \text{ and } A = \begin{bmatrix} 2 & 7 & \omega^2 \\ -1 & -\omega & 1 \\ 0 & -\omega & -\omega + 1 \end{bmatrix}$$

where $\omega = \frac{-1+i\sqrt{3}}{2}$, and I_3 be the identity matrix of order 3. If the determinant of the matrix $(P^{-1}AP - \mathbf{I}_3)^2$ is $\alpha\omega^2$, then the value of α is equal to ...

- 27) If the normal to the curve $y(x) = \int_0^x (2t^2 15t + 10t) dt$ at a point (a, b) is parallel to the line x + 3y = -5, a > 1, then the value of |a + 6b| is equal to ...
- 28) Let the curve y = y(x) be the solution of the differential equation, $\frac{dy}{dx} = 2(x+1)$. If the numerical value of area bounded by the curve y = y(x) and x- axis is $\frac{4\sqrt{8}}{3}$, then the value of y(1) is equal to ...
- 29) Let $f : \mathbf{R} \to \mathbf{R}$ be a continous function such that f(x) + f(x+1) = 2, for all $x \in \mathbf{R}$. If $\mathbf{I}_1 = \int_0^x f(x) dx$ and $\mathbf{I}_2 = \int_{-1}^3 f(x) dx$, then the value of $\mathbf{I}_1 + 2\mathbf{I}_2$ is equal to ...
- 30) Let z and w be two complex numbers such that $w = z\overline{z} 2z + 2$, $\left|\frac{z+i}{z-3i}\right| = 1$ and Re(w) has the minimum value. Then the minimum value of $n \in \mathbb{N}$ for which w^n is real, is equal to ...