EE24BTECH11008 - Aslin Garvasis

Ouestion:

Constuct a triangle whose sides are 3.6cm, 3.0cm and 4.8cm. Bisect the smallest angle and measure each part.

Solution:

: The smallest angle is associated with the opposite smallest side.

Variable	value	Description
A	$\begin{pmatrix} 0 \\ 0 \end{pmatrix}$	coordinates of first point
В	$\begin{pmatrix} 4.8 \\ 0 \end{pmatrix}$	coordinates of second point
С	$\begin{pmatrix} 2.81 \\ 2.24 \end{pmatrix}$	coordinates of third point
D	-	intersection of angle bisector of A in BC

TABLE 0: Input parameters

The angle bisector of a triangle of a triangle divides the opposite side into two parts proportional to the other two sides of the triangle.

$$\therefore ||AC|| = 3.6 \tag{0.1}$$

$$\therefore ||AB|| = 4.8 \tag{0.2}$$

$$\therefore ||BC|| = 3 \tag{0.3}$$

$$\therefore \mathbf{D} = \frac{\|AC\| \cdot \mathbf{B} + \|AB\| \cdot \mathbf{C}}{\|AC\| + \|BC\|} \tag{0.4}$$

$$\implies \mathbf{D} = 3.6 \binom{4.8}{0} + 4.8 \binom{2.81}{2.24} = \binom{3.66}{1.28} \tag{0.5}$$

$$\Rightarrow \mathbf{D} = 3.6 \begin{pmatrix} 4.8 \\ 0 \end{pmatrix} + 4.8 \begin{pmatrix} 2.81 \\ 2.24 \end{pmatrix} = \begin{pmatrix} 3.66 \\ 1.28 \end{pmatrix}$$

$$\Rightarrow \|BD\| = \frac{\|BC\| \|AB\|}{\|AB\| + \|AC\|} = 1.71$$

$$\Rightarrow \|CD\| = \frac{\|BC\| \|AC\|}{\|AB\| + \|AC\|} = 1.28$$
(0.5)
$$(0.5)$$

$$\implies ||CD|| = \frac{||BC|| \, ||AC||}{||AB|| + ||AC||} = 1.28 \tag{0.7}$$

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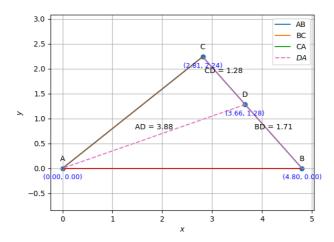


Fig. 0.1: Plot of points A, B, C and D