

puzzle

The Code

```
1.The "main.py":
# Asmaa Gamal
#Assignment 1
# Electronics & Communications department
#using informed and uninfoormed search Algorithms to solve 8-puzzle
import math
import timeit
                                                                #Measure execution
time of small code
                  import heappush, heappop, heapify
from heapq
from ClassOfStates import State
                                                                #importing from
class
from collections import deque
from GUI import GUI,
                    import GUI,print cyan
# -----The 8-Puzzle Game -----
print(" -----8-puzzle Game using (BFS, DFS,& A*) search algorithms------
print("------Welcome to the game-----
----")
#initialization
goal_state = [0, 1, 2, 3, 4, 5, 6, 7, 8]
goal node = State #Goal node is a full class which has depth, state, key, total cost,... etc
initial state = list()
#zero initialization
board_len = 0
board_side = 0
nodes expanded = 0
moves = list() #there is another global moves in the export fun below
costs = set()
#----BFS-----
                                 #passing the initial state to BFS algorism
def bfs(start state):
   global goal node
   explored= set(); queue = deque([State(start state, None, None, 0, 0, 0)]) #queue=frontier
#q=deque([])
   while queue: #frontier is not empty
      node = queue.popleft() #node= state object #remove and return the first in or the most
left element
      explored.add(node.map)
      if node.state == goal state: #node=State object # accessing the state in the class to
compare it with the goal if success
          goal node = node
          return queue
      neighbors = expand(node)
      for neighbor in neighbors:
          if neighbor.map not in explored:
```

queue.append(neighbor) #queue==frontier

```
#-----DFS------
def dfs(start state):
  global goal node
  explored=set(); stack = list([State(start state, None, None, 0, 0, 0)]) #here this means:
list = stack, queue =deque
  while stack:
                                                      #frontier = stack
is not empty
     node = stack.pop()
     explored.add(node.map)
                                                      #node= state object
     if node.state == goal state:
        goal node = node
        return stack
     neighbors = reversed(expand(node))
                                                     #because it's a
stack
     for neighbor in neighbors:
        if neighbor.map not in explored:
           stack.append(neighbor)
           explored.add(neighbor.map)
#----Manhattan distance
def h(state):
  return sum(    abs(b % board_side - g % board_side) + abs(b//board_side - g//board_side)
         for b, g in ( ( state.index(i), goal_state.index(i) ) for i in range(1,
board len) ) #board len=9
#----Euclidean distance
def eclidean h(state):
  ecl sum = 0
  for i in range(1, 9):
     brd= state.index(i) ; gl = goal_state.index(i)
     x = (brd % 3 - gl % 3) ** 2
     y = (brd // 3 - gl // 3) ** 2
     ecl sum += math.sqrt(x+y)
  return ecl sum
  # the above code lines in this fun are the same as saying:
  return sum( math.sqrt( ((b % board side - g % board side) **2 + (b//board side -
for b, g in ( ( state.index(i), goal state.index(i) ) for i in range(1,
board len) )
          ) #board len=9
#-----A* algorithm code ------
def ast(start state):
  print('-----')
  global goal_node
```

```
explored=set(); heap=list(); heap entry={}
                                                          #dic #frontier=heap #not used in
any thing below counter = itertools.count()
   key = h(start state)
                                                          #heuristics manhattan distance
   root = State(start state, None, None, 0, 0, key)
                                                          #root=neighbor
   entry = (key, 0, root)
                                                          #tuple does not change
   heappush (heap, entry)
   heap entry[root.map] = entry
   while heap:
       node = heappop(heap)
       explored.add(node[2].map)
       if node[2].state == goal state:
           goal node = node[2]
           return heap
       neighbors = expand(node[2])
       for neighbor in neighbors:
           neighbor.key = neighbor.cost + h(neighbor.state)
           entry = (neighbor.key, neighbor.move, neighbor)
                                                        #neighbor.move means the
element neighbor in the list move
           if neighbor.map not in explored:
              heappush (heap, entry)
              explored.add(neighbor.map)
              heap entry[neighbor.map] = entry
           elif neighbor.map in heap_entry and neighbor.key < heap_entry[neighbor.map][2].key:</pre>
              hindex = heap.index((heap entry[neighbor.map][2].key,
                                 heap entry[neighbor.map][2].move,
                                 heap entry[neighbor.map][2]))
              heap[int(hindex)] = entry
              heap entry[neighbor.map] = entry
              heapify(heap)
                                                              #trannsform a list into a
heap
#-----A* algorithm code ------
def euclidean ast(start state):
   global goal node
   explored=set(); heap=list(); heap_entry={}
                                                             #dic #frontier=heap #not used
in any thing below counter = itertools.count()
   key = eclidean h(start state)
                                                              #heuristics manhattan
distance
   root = State(start state, None, None, 0, 0, key)
                                                              #root=neighbor
   entry = (key, 0, root) #tuple does not change
   heappush (heap, entry)
```

```
heap entry[root.map] = entry
    while heap:
        node = heappop(heap)
        explored.add(node[2].map)
        if node[2].state == goal state:
           goal node = node[2]
            return heap
        neighbors = expand(node[2])
        for neighbor in neighbors:
            neighbor.key = neighbor.cost + eclidean h(neighbor.state)
            entry = (neighbor.key, neighbor.move, neighbor)
                                                                             #neighbor.move means
the element neighbor in the list move
            if neighbor.map not in explored:
                heappush (heap, entry)
                explored.add(neighbor.map)
                heap entry[neighbor.map] = entry
            elif neighbor.map in heap entry and neighbor.key < heap entry[neighbor.map][2].key:</pre>
                hindex = heap.index((heap entry[neighbor.map][2].key,
                                     heap entry[neighbor.map][2].move,
                                     heap entry[neighbor.map][2]))
                heap[int(hindex)] = entry
                heap entry[neighbor.map] = entry
                heapify(heap) #trannsform a list into a heap
                     -----Actions & paths -----
def move(state, position):
   new state = state[:]
                                                                                         #every
element in the array
    index = new state.index(0)
    if position == 1: # Up
        if index not in range(0, board side):
\#impossible = [0,1,2]
            temp = new state[index - board side]
#board side=3
            new state[index - board side] = new state[index]
            new state[index] = temp
            return new state
        else:
            return None
    if position == 2: # Down
```

if index not in range(board len - board side, board len):

```
\#impossible=range(9-3,9)=[6,7,8]
           temp = new state[index + board side]
           new state[index + board side] = new state[index]
           new state[index] = temp
           return new state
       else:
           return None
   if position == 3: # Left
       if index not in range(0, board len, board side):
           temp = new state[index - 1]
           new_state[index - 1] = new_state[index]
           new state[index] = temp
           return new state
       else:
           return None
   if position == 4: # Right
       if index not in range(board_side - 1, board_len, board_side):
           temp = new state[index + 1]
           new state[index + 1] = new state[index]
           new state[index] = temp
           return new state
       else:
           return None
def expand(node):
   global nodes expanded
   nodes expanded += 1
   neighbors = list()
   neighbors.append(State(move(node.state, 1), node, 1, node.depth + 1, node.cost + 1, 0)) #up
# state, parent, move, depth, cost, key
   neighbors.append(State(move(node.state, 2), node, 2, node.depth + 1, node.cost + 1, 0))
   neighbors.append(State(move(node.state, 3), node, 3, node.depth + 1, node.cost + 1, 0))
   neighbors.append(State(move(node.state, 4), node, 4, node.depth + 1, node.cost + 1, 0))
#right
   nodes = [neighbor for neighbor in neighbors if neighbor.state]
   return nodes
               ----- preparing of the output stage-----
def backtrace():
   current node = goal node
   while initial state != current node.state:
       if current node.move == 1:
          movement = 'Up'
       elif current node.move == 2:
          movement = 'Down'
```

elif current node.move == 3:

```
movement = 'Left'
      else:
         movement = 'Right'
      moves.insert(0, movement)
      current node = current node.parent
                                                                             #the
parent node will be considered as a currnt node for the comming check or iteration
   return moves
def export( time ):
   global moves
   global nodes expanded
   moves = backtrace()
   print('1.Path To Goal: ',end = '')
   print cyan(str(moves))
   print('2.Cost Of Path: ' , end = '')
   print cyan(str(len(moves)))
   print('3.Nodes Expanded:', end = '')
   print_cyan(str(nodes_expanded))
   print('4.Search Depth: ' , end = '')
                                              #search depth = max search depth i found
in it my goal
   print cyan(str(goal node.depth))
   print('5.Running Time: ', end = '')
   print cyan( format( time , '.8f'))
   # clearing everything in case we call the export method again in the A* algorithm using the
Euclidean distance
   moves = []
   nodes expanded=0
   goal node.depth = {}
def inputread(configuration):
                                       # populates a configuration thing
   global board_len, board_side
   data = configuration.split(",")
   for element in data:
      initial state.append(int(element)) #adding elements
   board len = len(initial state)
   board side = int(board_len ** 0.5)
                                       #sqrt root of 9 = 3
#-----the main ------
def main(algorithm, board):
   inputread(board)
                                         #calling the read fun or method
   if algor type == 'A*' or algor type == 'a*' or algor type == 'a star'or algor type == 'A
STAR'or algor type == 'A Star'or algor type == 'A star'or algor type == 'A* ':
      print('------A* Using Euclidean Distance Heuristics-----')
      start = timeit.default timer()
                                        # This will return the default time before
executing the next line
      euclidean ast(initial state)
      stop = timeit.default timer()
                                         # This will return the default time after
```

executing the above previous line

```
export( stop-start)
   function = function_map[algorithm]
                                      #google told me that this tricky line we use when
we wanna put the name of the calling algorithm from the user
   start = timeit.default timer()
                                       #This will return the default time before
executing the next line
   function(initial state)
                                       #This will return the default time after
   stop = timeit.default timer()
executing the above previous line
   export( stop-start)
   print('-----the Graphical user interface of the "8-Puzzle Game" is working in a new
window now -----')
  sol = backtrace()
                                        # sol=moves
   GUI (initial state, sol)
                                        #if the algorithm choosen by the user is A^* , then
i will make the Gui for manhatten distance heuristics only , in order not to duplicate the root
and destroy the current tk, 34an md514 nfsy fe 7warat
function map ={
   'BFS': bfs, 'bfs': bfs,
   'DFS': dfs,'dfs': dfs,
   'A*' : ast, 'a*':ast, 'a star':ast, 'A STAR':ast, 'A Star':ast, 'A star':ast
#----- from the user------
algor type = input("Enter the algorithm type u wanna use...For ex, type works like these>>
BFS,DFS,A* : ")
initial board = input("Enter your initial state..For ex>> 0,8,7,6,5,4,3,2,1 or 1,2,5,3,4,0,6,7,8
print('the program is running now! just wait for a second and the program will print your output
in details')
main(algor type,initial board)
```

2.The "ClassOfStates.py":

return self.map == other.map

return self.map < other.map</pre>

```
# Asmaa Gamal
#state class of Assignment 1
# Electronics & Communications department
#using informed and uninformed search Algorithms to solve 8-puzzle
class State:
    #depth = {} #i won't use it but it is to solve a warning as what stack overflow told me here:
https://stackoverflow.com/questions/28172008/pycharm-visual-warning-about-unresolved-attribute-reference
    def init (self, state, parent, move, depth, cost, key):
        self.state = state
       self.parent = parent
       self.move = move
       self.depth = depth
       self.cost = cost
       self.key = key
       if self.state:
           self.map = ''.join(str(e) for e in self.state) #map = for loop of the whole elements in all
2d or 4 d or n dimensions so al map btmsk each element we te apply 31eh al change elle ana 3awza 23mloh
```

def eq (self, other): #to transform the num into str to compare and find if equal

def lt (self, other): #to transform the num into str to compare and find if less than

```
3.The "GUI.py":
#state class of Assignment 1
# Electronics & Communications department
#using informed and uninformed search Algorithms to solve 8-puzzle
# -----visualization-----
from tkinter import *
tk = Tk()
ANSI RESET = "\u001B[0m"]
ANSICYAN = "\u001B[36m"]
def print_cyan(msg):
   print(f"{ANSI_CYAN}{msg}{ANSI_RESET}")
def init button(num):
   if num == 0:
       return Label(tk, text=num, font='Times 25 bold', bg='grey', fg='black', height=4, width=8)
    else:
       return Label(tk, text=num, font='Times 25 bold', bg='cyan3', fg='black', height=4, width=8)
def shuffle(index, target,puzzle): #puzzle=initial state
    temp = puzzle[target]
    puzzle[target] = 0
   puzzle[index] = temp
def GUI(puzzle, sol):
                                   #puzzle=initial state
    tk.title("
                              GUI Solver Of The 8-Puzzle Game")
   index = 0
   button0 = init_button(puzzle[0])
   button0.grid(row=3, column=0)
   button1 = init_button(puzzle[1])
   button1.grid(row=3, column=1)
   button2 = init button(puzzle[2])
   button2.grid(row=3, column=2)
   button3 = init_button(puzzle[3])
   button3.grid(row=4, column=0)
   button4 = init button(puzzle[4])
   button4.grid(row=4, column=1)
   button5 = init button(puzzle[5])
   button5.grid(row=4, column=2)
   button6 = init button(puzzle[6])
   button6.grid(row=5, column=0)
   button7 = init_button(puzzle[7])
   button7.grid(row=5, column=1)
   button8 = init button(puzzle[8])
   button8.grid(row=5, column=2)
    def fun(index):
       zero_place = puzzle.index(0)
       target = 0
       if zero place == 0:
           if sol[index] == 'Down':
               target = 3
               button0["text"] = button3["text"]
               button0["bg"] = 'cyan2'
               tk.update()
               button3["text"] = 0
               button3["bg"] = 'grey'
               tk.update()
           elif sol[index] == 'Right':
               target = 1
               button0["text"] = button1["text"]
               button0["bg"] = 'cyan2'
               tk.update()
               button1["text"] = 0
```

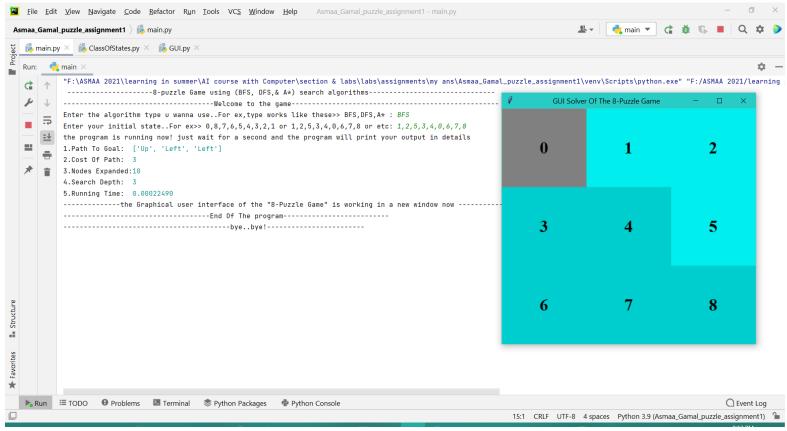
```
button1["bq"] = 'grey'
        tk.update()
    shuffle(zero place, target,puzzle)
elif zero place == 1:
   if sol[index] == 'Left':
       target = 0
       button1["text"] = button0["text"]
       button1["bq"] = 'cyan2'
        tk.update()
       button0["text"] = 0
       button0["bg"] = 'grey'
        tk.update()
   elif sol[index] == 'Down':
       target = 4
       button1["text"] = button4["text"]
       button1["bg"] = 'cyan2'
       tk.update()
       button4["text"] = 0
       button4["bg"] = 'grey'
        tk.update()
   elif sol[index] == 'Right':
       target = 2
       button1["text"] = button2["text"]
       button1["bg"] = 'cyan2'
        tk.update()
       button2["text"] = 0
       button2["bg"] = 'grey'
       tk.update()
    shuffle(zero place, target,puzzle)
elif zero place == 2:
   if sol[index] == 'Left':
        target = 1
       button2["text"] = button1["text"]
       button2["bg"] = 'cyan2'
       tk.update()
       button1["text"] = 0
       button1["bg"] = 'grey'
       tk.update()
   elif sol[index] == 'Down':
        target = 5
        button2["text"] = button5["text"]
       button2["bg"] = 'cyan2'
       tk.update()
       button5["text"] = 0
       button5["bg"] = 'grey'
        tk.update()
   shuffle(zero place, target,puzzle)
elif zero place == 3:
   if sol[index] == 'Up':
        target = 0
       button3["text"] = button0["text"]
       button3["bg"] = 'cyan2'
        tk.update()
       button0["text"] = 0
       button0["bg"] = 'grey'
        tk.update()
   elif sol[index] == 'Down':
        target = 6
       button3["text"] = button6["text"]
       button3["bq"] = 'cyan2'
       tk.update()
       button6["text"] = 0
       button6["bg"] = 'grey'
       tk.update()
   elif sol[index] == 'Right':
       target = 4
        button3["text"] = button4["text"]
       button3["bq"] = 'cyan2'
        tk.update()
       button4["text"] = 0
       button4["bg"] = 'grey'
        tk.update()
    shuffle(zero_place, target,puzzle)
elif zero place == 4:
   if sol[index] == 'Up':
```

```
target = 1
       button4["text"] = button1["text"]
       button4["bg"] = 'cyan2'
       tk.update()
       button1["text"] = 0
       button1["bg"] = 'grey'
       tk.update()
   elif sol[index] == 'Left':
       target = 3
        button4["text"] = button3["text"]
        button4["bg"] = 'cyan2'
        tk.update()
       button3["text"] = 0
       button3["bg"] = 'grey'
       tk.update()
   elif sol[index] == 'Down':
       target = 7
       button4["text"] = button7["text"]
       button4["bg"] = 'cyan2'
       tk.update()
       button7["text"] = 0
       button7["bg"] = 'grey'
        tk.update()
   elif sol[index] == 'Right':
        target = 5
        button4["text"] = button5["text"]
       button4["bg"] = 'cyan2'
       tk.update()
       button5["text"] = 0
       button5["bg"] = 'grey'
       tk.update()
    shuffle(zero place, target,puzzle)
elif zero place == 5:
   if sol[index] == 'Up':
       target = 2
       button5["text"] = button2["text"]
       button5["bg"] = 'cyan2'
        tk.update()
        button2["text"] = 0
       button2["bg"] = 'grey'
       tk.update()
   elif sol[index] == 'Left':
       target = 4
       button5["text"] = button4["text"]
       button5["bg"] = 'cyan2'
       tk.update()
       button4["text"] = 0
       button4["bg"] = 'grey'
        tk.update()
   elif sol[index] == 'Down':
        target = 8
       button5["text"] = button8["text"]
       button5["bg"] = 'cyan2'
       tk.update()
       button8["text"] = 0
       button8["bg"] = 'grey'
       tk.update()
    shuffle(zero_place, target,puzzle)
elif zero_place == 6:
   if sol[index] == 'Up':
       target = 3
       button6["text"] = button3["text"]
       button6["bg"] = 'cyan2'
       tk.update()
       button3["text"] = 0
       button3["bg"] = 'grey'
       tk.update()
   elif sol[index] == 'Right':
        target = 7
        button6["text"] = button7["text"]
       button6["bg"] = 'cyan2'
        tk.update()
       button7["text"] = 0
        button7["bg"] = 'grey'
```

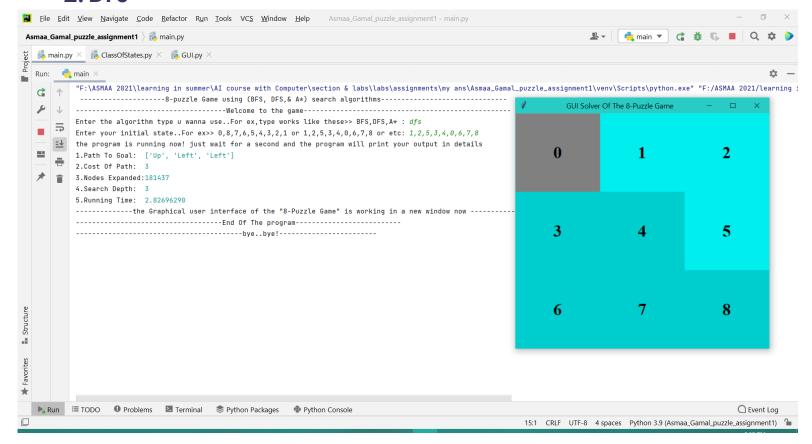
```
tk.update()
        shuffle(zero place, target,puzzle)
    elif zero place == 7:
        if sol[index] == 'Up':
           target = 4
            button7["text"] = button4["text"]
           button7["bg"] = 'cyan2'
            tk.update()
            button4["text"] = 0
            button4["bg"] = 'grey'
            tk.update()
        elif sol[index] == 'Left':
            target = 6
            button7["text"] = button6["text"]
           button7["bg"] = 'cyan2'
           tk.update()
           button6["text"] = 0
            button6["bg"] = 'grey'
            tk.update()
        elif sol[index] == 'Right':
            target = 8
            button7["text"] = button8["text"]
           button7["bg"] = 'cyan2'
            tk.update()
            button8["text"] = 0
           button8["bg"] = 'grey'
            tk.update()
        shuffle(zero_place, target,puzzle)
    elif zero place == 8:
        if sol[index] == 'Up':
            target = 5
            button8["text"] = button5["text"]
           button8["bg"] = 'cyan2'
           tk.update()
           button5["text"] = 0
           button5["bg"] = 'grey'
           tk.update()
        elif sol[index] == 'Left':
            target = 7
            button8["text"] = button7["text"]
            button8["bg"] = 'cyan2'
            tk.update()
           button7["text"] = 0
           button7["bg"] = 'grey'
            tk.update()
        shuffle(zero_place, target, puzzle)
    if index != len(sol) - 1:
        index += 1
        tk.after(650, fun,index)
    index += 1
tk.after(3000, fun,index)
tk.mainloop()
```

Screenshots Of Some Runs

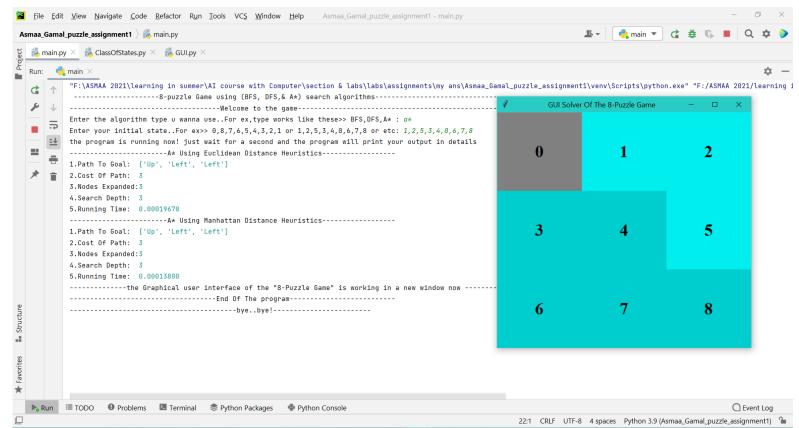
1. BFS



2. DFS



3. A*



Data Structures Used

- Stack (list)
- Queue(list)
- Heap(list)
- Tuples
- Set
- Dictionary

Algorithms

BFS search

```
function BREADTH-FIRST-SEARCH(initialState, goalTest)

returns Success or Failure:

frontier = Queue.new(initialState)
explored = Set.new()

while not frontier.isEmpty():
    state = frontier.dequeue()
    explored.add(state)

if goalTest(state):
    return Success(state)

for neighbor in state.neighbors():
    if neighbor not in frontier ∪ explored:
        frontier.enqueue(neighbor)

return Failure
```

DFS search

return FAILURE

```
function DEPTH-FIRST-SEARCH(initialState, goalTest)
    returns Success or Failure:

frontier = Stack.new(initialState)
    explored = Set.new()

while not frontier.isEmpty():
    state = frontier.pop()
    explored.add(state)

if goalTest(state):
    return Success(state)

for neighbor in state.neighbors():
    if neighbor not in frontier ∪ explored:
        frontier.push(neighbor)
```

A* search

return FAILURE

```
function A-STAR-SEARCH(initialState, goalTest)
    returns SUCCESS or FAILURE: /* Cost f(n) = g(n) + h(n) */
    frontier = Heap.new(initialState)
    explored = Set.new()

while not frontier.isEmpty():
    state = frontier.deleteMin()
    explored.add(state)

if goalTest(state):
    return SUCCESS(state)

for neighbor in state.neighbors():
    if neighbor not in frontier ∪ explored:
        frontier.insert(neighbor)
    else if neighbor in frontier:
        frontier.decreaseKey(neighbor)
```

Example Shows A summary of my work

[1,2,5,3,4,0,6,7,8]

Data	BFS	DFS	A* (Euclidean)	A* (Manhattan)
Path to goal	['Up', 'Left', 'Left']	['Up', 'Left', 'Left']	['Up', 'Left', 'Left',]	['Up', 'Left', 'Left']
cost	3	3	3	9
Node expanded	10	181437	3	3
Search depth	3	3	3	3
Running time	0.00022490	2.82696290	0.00019670	0.0001380

From this above example, also from more complicated sequence examples outputs in the coming few photos, like: 0,8,7,6,5,4,3,2,1, and finally from the below two equations we can find out that the Manhattan distance heuristics are more admissible than the Euclidean distance heuristics.

1. Manhattan Distance

It is the sum of absolute values of differences in the goal's x and y coordinates and the current cell's x and y coordinates respectively,

$$h = abs(current_cell:x - goal:x) + abs(current_cell:y - goal:y)$$

2. Euclidean Distance

It is the distance between the current cell and the goal cell using the distance formula

$$h = sqrt((current_cell:x - goal:x)^2 + (current_cell.y - goal:y)^2)$$

```
"F:\ASMAA 2021\learning in summer\AI course with Computer\section & labs\labs\assignments\my ans\Asmaa_Gamal_puzzle_assignment1\venv\Scripts\python.exe" "F:/ASMAA 2021/learning
   -----8-puzzle Game using (BFS, DFS,& A*) search algorithms------
 Enter the algorithm type u wanna use..For ex,type works like these>> BFS,DFS,A* : A*
Enter your initial state.. For ex>> 0.8,7,6,5,4,3,2,1 or 1,2,5,3,4,0,6,7,8 or etc: 0.8,7,6,5,4,3,2,1
the program is running now! just wait for a second and the program will print your output in details
 ------A* Using Euclidean Distance Heuristics------
1.Path To Goal: ['Right', 'Down', 'Down', 'Right', 'Up', 'Up', 'Left', 'Down', 'Down', 'Left', 'Up', 'Right', 'Down', 'Right', 'Up', 'Left', 'Left', 'Down', 'Right', 'Up', 'Left', 'Left', 'Down', 'Right', 'Up', 'Left', 'Down', 'Right', 'Up', 'Left', 'Down', 'Right', 'Up', 'Left', 'Down', 'Right', 'Up', 'Left', 'Left', 'Down', 'Right', 'Up', 'Left', 'Left',
2.Cost Of Path: 30
3.Nodes Expanded: 29367
4. Search Depth: 30
5.Running Time: 1.57665620
 ------A* Using Manhattan Distance Heuristics------A*
1.Path To Goal: ['Right', 'Down', 'Down', 'Right', 'Up', 'Up', 'Left', 'Down', 'Left', 'Up', 'Right', 'Down', 'Right', 'Up', 'Left', 'Left', 'Lef
2.Cost Of Path: 30
3.Nodes Expanded: 12893
4.Search Depth: 30
5.Running Time: 0.90166270
 ------the Graphical user interface of the "8-Puzzle Game" is working in a new window now ---------
 -----End Of The program------
                  -----bye..bye!-----
```

Because the Manhattan output is better in the:

- 1. Time: its speed or running time is better (as it doesn't need to use the math.sqrt)
- 2.Memory: Num of "nodes expanded" is better.

Although, the distance of Euclidean diagonal is less than the distance of the absolute differences in the goal's x and y coordinates and the current cell's x and y coordinates respectively

But Manhattan here is more admissible because the only allowed moves here in the 8-puzzle game are the horizontal and the vertical moves only. This means that we can't move diagonally as what the Euclidean distance assumption says. So, the output numbers using the Manhattan distance of this 8-puzzle game here are more admissible ^^.