

ASSIGNMENT - 4

(4P3)

→ 1 Read dataset $x_i^9 = 7.6$; $y_i^9 = 157$
 $n_s = 2$ $x_i^9 = 7.1$; $y_i^9 = 174$

$\eta = 0.1$, epochs = 1 , $m = 1$

→ 2 iteration set to 1

→ 3 sample $i = 1$

→ 4 Cal. $y = mx_i^9 + c$

$$y_1 = (7.6) - 1 = 6.6$$

→ 5 Cal. error

$$E = \frac{1}{2} (y_i^9 - mx_i^9 + c)^2$$

$$= \frac{1}{2} (157 - 117.6 - 1)^2$$

$$= \frac{1}{2} \times 11011.28$$

→ 6 Cal. gradients of error

$$\frac{dE}{dm} = -(y_i^9 - mx_i^9 - c) x_i^9$$

$$= -((157 - 117.6) - 1) 7.6$$

$$= -1127.84$$

$$\frac{dE}{dc} = -(y_i^9 - mx_i^9 - c)$$

$$= -148.4$$

→ 7 Cal. step length Δm & Δc

$$\Delta m = \eta \left[\frac{\partial E}{\partial m} \right] = -0.1 (-1127.84) = 112.784$$

$$\Delta c = -\eta \left[\frac{\partial E}{\partial c} \right] = 14.84$$

→ 8 update m & c

$$m = m + \Delta m = 113.78$$

$$c = c + \Delta c = 13.84$$

→ 9 sample $i = i + 1 = 2$

$$i < n_s = 2 < 2, \text{ false}$$

back again to ④

$$y = mx_i^9 + c$$

$$= 113.78 (7.1) + 13.84$$

$$y_2 = 821.878$$

$$E = \frac{1}{2} [174 - (113.78)(7.1) + 13.84]^2$$

$$= -309.999$$

$$\frac{\partial E}{\partial m} = -(y_i^9 - mx_i^9 - c) x_i^9$$

$$= -(174 - 113.78(7.1) - 13.84) 7.1$$

$$\frac{\partial E}{\partial m} = 4598.5132$$

$$\frac{\partial E}{\partial c} = -(y_i^9 - mx_i^9 - c)$$

$$= -(174 - 113.78(7.1) - 13.84)$$

$$= 647.678$$

— cal. step length

$$\Delta m = -\eta \frac{\partial E}{\partial m} = -0.1 (4598.513) \\ = -459.8513$$

$$\Delta c = -\eta \frac{\partial E}{\partial c} = -0.1 (647.678) \\ = -64.7678$$

— update m & c

$$m = m + \Delta m = 113.78 - 459.85 \\ = -346.07$$

$$c = c + \Delta c = 13.84 - 64.769 \\ = -50.929$$

— $i = i + 1 = 3$

$$\text{if } (i < n_s) = 3 < 2$$

next...

— w) iter = iter 1 = 1 + 1 = 2

$$\text{if } (\text{iter} > \text{epochs})$$

2 > 1 ✓ : next

— ii) Cal. MSE error = $\frac{1}{n_s} \sum_{i=1}^{n_s} (y_i^o - y_i)^2$

$$= \frac{1}{2} (y_1^o - y_1)^2 + \frac{1}{2} (y_2^o - y_2)^2$$

$$= \frac{1}{2} (157 - 6.6)^2 + \frac{1}{2} (174 - 821.67)^2$$

$$= 221048.29, \text{ RMSE} = 470.15$$