

$$E = \frac{1}{2} (y_i - m_1 x_i^2 - m_2 x_i - c)^2$$

$$\frac{\partial E}{\partial m_1} = -x_i^2 (y_i - m_1 x_i^2 - m_2 x_i - c)$$

$$\frac{\partial E}{\partial c} = -(y_i - m_1 x_i^2 - m_2 x_i - c)$$

$$\frac{\partial E}{\partial m_2} = -x_i (y_i - m_1 x_i^2 - m_2 x_i - c)$$

$$m_1 = 10, m_2 = 5, c = 12, \text{eta} = 0.001, \text{epochs} = 1$$

$$\begin{aligned} \nabla m_1 &= -x_1^2 (y_1 - m_1 x_1^2 - m_2 x_1 - c) \\ &= -7.6^2 (157 - 10(7.6)^2 - 5(7.6) - 12) \\ &= 57.76 (150.12) \Rightarrow 27181.856 \end{aligned}$$

$$\begin{aligned} \nabla m_2 &= -x_1 (y_1 - m_1 x_1^2 - m_2 x_1 - c) \\ &= -7.6 (157 - 10(7.6)^2 - 5(7.6) - 12) \\ &= 3576.56 \end{aligned}$$

$$\begin{aligned} \nabla c &= -(y_1 - m_1 x_1^2 - m_2 x_1 - c) \Rightarrow -(157 - 10(7.6)^2 - 5(7.6) - 12) \\ &= 812.6 \end{aligned}$$

$$m_1 = m_1 - \eta \times \nabla m_1 = 10 - 0.001 \times 27181.856 = -17.18185$$

$$m_2 = m_2 - \eta \times \nabla m_2 = 5 - 0.001 \times 3576.56 = -1.42364$$

$$c = c - \eta \times \nabla c = 12 - 0.001 \times 812.6 = 11.1874$$

Sample 2:  $\nabla m_1 = -x_2^2 (y_2 - m_1 x_2^2 - m_2 x_2 - c)$

$$\begin{aligned} &= -71^2 (174 + 10(7.1)^2 - 1.423(7.1) - 11.1874) \\ &= -52341.8814 \end{aligned}$$

$$\begin{aligned} \nabla m_2 &= -x_2 (y_2 - m_1 x_2^2 - m_2 x_2 - c) \\ &= -71 (174 + 17.181(7.1)^2 + 1.423(7.1) - 11.1874) \\ &= -7376.971 \end{aligned}$$

$$\begin{aligned} \nabla c &= -(y_2 - m_1 x_2^2 - m_2 x_2 - c) \\ &= -(174 + 17.181(7.1)^2 + 1.423(7.1) - 11.187) \\ &= -1039.01051 \end{aligned}$$

$$\begin{aligned}
 m_1 &= m_1 - \eta \times \nabla m_1 = -17.18 - 0.001 \times -52341 = 899.213 \\
 m_2 &= m_2 - \eta \times \nabla m_2 = -1.42 - 0.001 \times -7376 = 5.956 \\
 c &= c - \eta \times \nabla c = 11.18 - 0.001 \times -1039 = 12.219
 \end{aligned}$$