

## Problem 1

### Constraint Satisfaction Problem

Variables =  $\{E_{ij} \text{ for all edges}\}$

Domains =  $\{x: 0 \leq x < n(\text{Variables})\}$

Constraints

- $\forall E_{ij} \forall E_{xy}, |E_{ij} - E_{xy}| = 1 \Rightarrow i = y \vee j = x$
- $\forall E_{ij} \forall E_{xy}, i \neq x \wedge j \neq y \Rightarrow E_{ij} \neq E_{xy}$

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Explanation: Variables are edges of the given graph.

Domain is range of sequence numbers from 0 to length of variables.

First constraint guarantees that if two edges are assigned 2 consecutive sequence numbers, they must share a common node. (i.e. lifting pencil is not possible)

Second constraint guarantees that each edge is assigned to a different number. Every value in domain is assigned to a single edge.

## Problem 2

### → FOL Representation

- All dogs are animal.

$$\forall x \text{ Dog}(x) \Rightarrow \text{Animal}(x)$$

- Not all robots can carry objects.

$$\neg \forall x \text{ Robot}(x) \Rightarrow \text{carries}(x, \text{object})$$

- Everyone who graduated from high school also graduated from prim. school.

$$\forall x \text{ Graduated}(x, \text{High school}) \Rightarrow \text{Graduated}(x, \text{Primary school})$$

- Some students did not take AI course.

$$\exists x \text{ Student}(x) \wedge \neg \text{Take}(x, \text{AI})$$

- There is only one table.

$$\exists x \forall y \text{ Table}(x) \wedge \text{Table}(y) \Rightarrow x=y$$

- There is a teacher who only talk to other teachers that are teaching Phy.

$$\exists x \forall y \text{ Teacher}(x) \wedge \text{Teacher}(y) \wedge \text{Talks}(x, y) \Rightarrow \text{Teaches}(y, \text{Physics})$$

### → FOL and Resolution

#### a) Constructing the knowledge base

- $\text{Student}(\text{Arda}, x) \wedge \text{Student}(\text{Cihan}, x) \wedge \text{Student}(\text{Gomez}, x) \wedge \text{University}(U)$
- $\text{Language}(\text{English}) \wedge \text{Language}(\text{French}) \wedge \text{Language}(\text{Russian}) \wedge \text{Language}(\text{Turkish})$
- $\forall x \text{ Student}(x, U) \Rightarrow \text{Speaks}(x, \text{Turkish})$
- $\forall x \text{ Student}(x, U) \Rightarrow \text{Speaks}(x, \text{English}) \vee \text{Speaks}(x, \text{Russian}) \vee \text{Speaks}(x, \text{French})$
- $\text{Food}(\text{Fish}) \wedge \text{Food}(\text{Hamburger})$
- $\text{Music}(\text{Classic}) \wedge \text{Music}(\text{Tazz}) \wedge \text{Music}(\text{Rock})$
- $\forall x \text{ Student}(x, U) \wedge \text{Speaks}(x, \text{French}) \Rightarrow \text{Likes}(x, \text{Tazz}) \wedge \neg \text{Likes}(x, \text{Rock})$
- $\forall x \text{ Student}(x, U) \wedge \text{Speaks}(x, \text{Russian}) \Rightarrow \text{Likes}(x, \text{Rock})$
- $\forall x \text{ Student}(x, U) \wedge \text{Likes}(x, \text{Hamburger}) \Rightarrow \text{Speaks}(x, \text{English})$
- $\forall x \text{ Student}(x, U) \wedge \neg \text{Likes}(x, \text{Hamburger}) \Rightarrow \neg \text{Speaks}(x, \text{English})$
- $\text{Likes}(\text{Arda}, \text{Tazz}) \wedge \text{Likes}(\text{Arda}, \text{Fish}) \wedge \neg \text{Likes}(\text{Arda}, \text{Classic}) \wedge \neg \text{Likes}(\text{Arda}, \text{Rock}) \wedge \neg \text{Likes}(\text{Arda}, \text{Hamburger})$
- $\forall x \text{ Music}(x) \wedge \text{Likes}(\text{Arda}, x) \Rightarrow \neg \text{Likes}(\text{Cihan}, x)$
- $\forall x \text{ Music}(x) \wedge \neg \text{Likes}(\text{Arda}, x) \Rightarrow \text{Likes}(\text{Cihan}, x)$
- $\text{Likes}(\text{Cihan}, \text{Fish}) \wedge \neg \text{Likes}(\text{Cihan}, \text{Hamburger})$
- $\text{Likes}(\text{Gomez}, \text{Fish}) \wedge \text{Likes}(\text{Gomez}, \text{Hamburger}) \wedge \text{Likes}(\text{Gomez}, \text{Classic}) \wedge \neg \text{Likes}(\text{Gomez}, \text{Tazz}) \wedge \neg \text{Likes}(\text{Gomez}, \text{Rock})$

### Problem 3

In this question we are asked to implement a minimax agent to solve a turn-based sudoku game. To do so, I have created a class to keep the game state (grid and turn) and a class to perform required operations by minimax algorithm (successors, terminal\_test, utility etc.) The code is documented so it should be self explanatory. The minimax and alpha-beta pruning algorithms are exact copy from lecture slides.

In order to run the code "numpy" should be installed.  
python3 main.py input.txt a  $\rightarrow$  alpha beta  
python3 main.py input.txt m  $\rightarrow$  minimax

I've tested both algorithms with given text file. Standard minimax couldn't find a solution. Alpha-beta pruning found the solution in 38.58 seconds by evaluating 367 770 nodes.