Floating Point, RISC-V Intro

Discussion 3: September 16, 2019

1 Floating Point

The IEEE 754 standard defines a binary representation for floating point values using three fields.

- The sign determines the sign of the number (0 for positive, 1 for negative).
- The *exponent* is in **biased notation**. For instance, the bias is $127 (2^{8-1} 1)$ for single-precision floating point numbers.
- The *significand* or *mantissa* is akin to unsigned integers, but used to store a fraction instead of an integer.

The below table shows the bit breakdown for the single precision (32-bit) representation. The leftmost bit is the MSB and the rightmost bit is the LSB.

1	8	23
Sign	Exponent	Mantissa/Significand/Fraction

For normalized floats:

Value = $(-1)^{Sign} * 2^{Exp-Bias} * 1.$ significand₂

For denormalized floats:

Value = $(-1)^{Sign} * 2^{Exp-Bias+1} * 0$.significand₂

Exponent	Significand	Meaning
0	Anything	Denorm
1-254	Anything	Normal
255	0	Infinity
255	Nonzero	NaN

Note that in the above table, our exponent has values from 0 to 255. When translating between binary and decimal floating point values, we must remember that there is a bias for the exponent.

- 1.1 How many zeroes can be represented using a float?
- 1.2 What is the largest finite positive value that can be stored using a single precision float?
- 1.3 What is the smallest positive value that can be stored using a single precision float?
- 1.4 What is the smallest positive normalized value that can be stored using a single precision float?

- 1.5 Cover the following single-precision floating point numbers from binary to decimal or from decimal to binary. You may leave your answer as an expression.
 - 0x00000000 39.5625
 - 8.25 0xFF94BEEF
 - 0x00000F00

2 More Floating Point Representation

Not every number can be represented perfectly using floating point. For example, $\frac{1}{3}$ can only be approximated and thus must be rounded in any attempt to represent it. For this question, we will only look at positive numbers.

- 2.1 What is the next smallest number larger than 2 that can be represented completely?
- 2.2 What is the next smallest number larger than 4 that can be represented completely?
- 2.3 Define stepsize to be the distance between some value x and the smallest value larger than x that can be completely represented. What is the step size for 2? 4?
- Now let's see if we can generalize the stepsize for normalized numbers (we can do so for denorms as well, but we won't in this question). If we are given a normalized number that is not the largest representable normalized number with exponent value x and with significand value y, what is the stepsize at that value? Hint: There are 23 significand bits.
- 2.5 Now let's apply this technique. What is the largest odd number that we can represent? Part 4 should be very useful in finding this answer.

3 RISC-V: A Rundown

RISC-V is an assembly language, which is comprised of simple instructions that each do a single task such as addition or storing a chunk of data to memory.

For example, on the left is a line of C code and on the right is a chunk of RISC-V code that accomplishes the same thing.

```
// x -> s0, &y -> s1

int x = 5, y[2]; addi s0, x0, 5

y[0] = x; sw s0, 0(s1)

y[1] = x * x; mul t0, s0, s0

sw t0, 4(s1)
```

[3.1] Can you figure out what each line in the RISC-V code is doing?

4 Registers

In RISC-V, we have two methods of storing data: main memory and registers. Registers are much faster than using main memory, but are very limited in space (32 bits each). Note that you should ALWAYS use the named registers (e.g. $\mathfrak{s0}$ rather than $\mathfrak{x8}$).

Register(s)	Alt.	Description
x0	zero	The zero register, always zero
x1	ra	The return address register, stores where functions should return
x2	sp	The stack pointer, where the stack ends
x5-x7, x28-x31	t0-t6	The temporary registers
x8-x9, x18-x27	s0-s11	The saved registers
x10-x17	a0-a7	The argument registers, a0-a1 are also return value

[4.1] Can you convert each instruction's registers to the other form?

```
add s0, zero, a1 --> or x18, x1, x30 -->
```

5 Basic Instructions

For your reference, here are some of the basic instructions for arithmetic operations and dealing with memory (Note: ARG1 is argument register 1, ARG2 is argument register 2, and DR is destination register):

[inst]	[destination register] [argument register 1] [argument register 2]	
add	Adds the two argument registers and stores in destination register	
xor	Exclusive or's the two argument registers and stores in destination register	
mul	Multiplies the two argument registers and stores in destination register	
sll	Logical left shifts ARG1 by ARG2 and stores in DR	
srl	Logical right shifts ARG1 by ARG2 and stores in DR	
sra	Arithmetic right shifts ARG1 by ARG2 and stores in DR	
slt/u	If ARG1 < ARG2, stores 1 in DR, otherwise stores 0, u does unsigned comparison	

[inst]	[register] [offset]([register containing base address])		
sw	Stores the contents of the register to the address+offset in memory		
lw	Takes the contents of address+offset in memory and stores in the register		
[inst]	[argument register 1] [argument register 2] [label]		
beq	If $ARG1 == ARG2$, moves to label		
bne	If ARG1 != ARG2, moves to label		
[inst]	[destination register] [label]		
jal	Stores the next instruction's address into DR and moves to label		

You may also see that there is an "i" at the end of certain instructions, such as addi, slli, etc. This means that ARG2 becomes an "immediate" or an integer instead of using a register. There are also immediates in some other instructions such as **sw** and **lw**. NOTE: The size of an immediate in any given instruction depends on what type of instruction it is (more on this soon!).

5.1 Assume we have an array in memory that contains int* arr = {1,2,3,4,5,6,0}. Let register s0 hold the address of the zeroth element in arr. You may assume integers are four-bytes and our values are word-aligned. What do the snippets of RISC-V code do? Assume that all the instructions are run one after the other in the same context.

a)
$$lw t0, 12(s0)$$
 -->

6 C to RISC-V

[6.1] Translate between the C and RISC-V verbatim

```
RISC-V
// s0 -> a, s1 -> b
// s2 -> c, s3 -> z
int a = 4, b = 5, c = 6, z;
z = a + b + c + 10;
// s0 -> int * p = intArr;
// s1 -> a;
*p = 0;
int a = 2;
p[1] = p[a] = a;
// s0 -> a, s1 -> b
int a = 5, b = 10;
if(a + a == b) {
   a = 0;
} else {
   b = a - 1;
}
                                           addi s0, x0, 0
                                           addi s1, x0, 1
                                           addi t0, x0, 30
                                       loop:
                                           beq s0, t0, exit
                                           add s1, s1, s1
                                           addi s0, s0, 1
                                           jal x0, loop
                                       exit:
// s0 -> n, s1 -> sum
// assume n > 0 to start
for(int sum = 0; n > 0; n--) {
 sum += n;
}
```