Semantic similarity and machine learning with ontologies

A brief introduction

Robert Hoehndorf

https://github.com/bio-ontology-research-group/ontology-tutorial

Semantic similarity: some examples

- Are cyclin dependent kinases *functionally* more similar to lipid kinases or to riboflavin kinases? How about *phenotypically*?
- Which protein in the *mouse* is functionally most similar to the zebrafish *gustducin* protein?
- Which mouse knockout resembles Bardet-Biedl Syndrome 8?
- Are there mouse knockouts that resemble the side effects of diclofenac?
- Which genetic disease produces similar symptoms to ebola?
- Does functional similarity correlate with phenotypic similarity?

Semantic similarity

semantic similarity measures:

- for words, terms, classes
- role of background knowledge:
 - ► statistical/distributional semantics, large corpora
 - ontologies: (graph) topology
- similarity measures: hand-crafted or data-driven?

Semantic similarity or machine learning

- semantic similarity measures are mostly hand-crafted
 - ► capture certain intuition about what constitutes "similarity"
 - different measures for different kinds of similarity
 - usually interpretable (and explainable)

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 - ► capture certain intuition about what constitutes "similarity"
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 - usually interpretable (and explainable)
- machine learning methods are mostly data-driven
 - ▶ the architecture of the model is still hand-crafted
 - usually hard to interpret

Ontologies and graphs

- semantic similarity measures and machine learning models on ontologies can be graph-based, feature-based, or model-based
 - graph-based: ontology as a graph
 - ► feature-based: extract (or obtain) features for classes/relations (e.g., from axioms)
 - ▶ model-based: define similarity within (special) Σ -structures

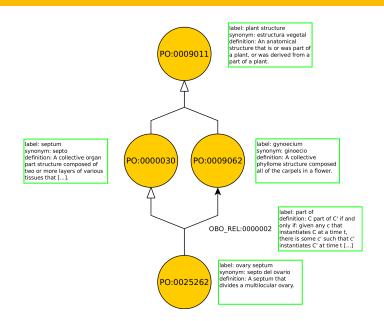
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 - ightharpoonup model-based: define similarity within (special) Σ -structures
- we may need to generate graphs from ontologies
 - ▶ is-a relations are easy (this is just owl:subClassOf)
 - how about part-of, regulates, precedes, etc.?
 - disjointness, universal vs. existential quantification, cardinality restrictions, intersection, union, negation?

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 - disjointness, universal vs. existential quantification, cardinality restrictions, intersection, union, negation?
- relational patterns are implicit in OWL axioms
 - design patterns as "relations" between classes

Relations as patterns



Relations as patterns

• ...

• X SubClassOf: Y: $X \xrightarrow{\text{is-a}} Y$ • X SubClassOf: part-of some Y: $X \xrightarrow{\text{part-of}} Y$ • X SubClassOf: regulates some Y: $X \xrightarrow{\text{regulates}} Y$ • X DisjointWith: Y: $X \xleftarrow{\text{disjoint}} Y$ • X EquivalentTo: Y: $X \xleftarrow{\equiv} Y$, $\{X,Y\}$

NB: in bio-ontologies, the OBO Relation Ontology defines these patterns

Asserted and inferred

- relation patterns can be asserted or inferred
- X SubClassOf: part-of some Y
- Y SubClassOf: part-of some Z
- part-of o part-of SubPropertyOf: part-of
- $\bullet \vdash X \text{ SubClassOf: } part-of some Z$
- Therefore: $X \xrightarrow{\text{part-of}} Z$
- ullet \Rightarrow we should use deductive inference to generate these patterns

Semantic similarity

- We want to use background knowledge in ontologies to
 - ▶ determine similarity between classes,
 - instances,
 - ▶ and entities with ontology annotations

- semantic similarity measures similarity between classes
- semantic similarity measures similarity between instances of classes
- semantic similarity measures similarity between entities annotated with classes
- ullet \Rightarrow reduce all of this to similarity between classes

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 - weaker form: sim(x, x) > sim(x, y) for all $x \neq y$

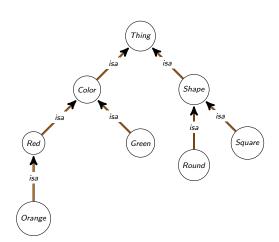
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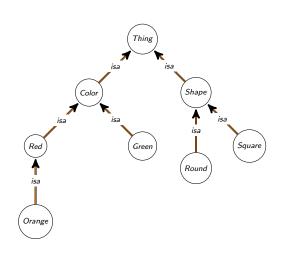
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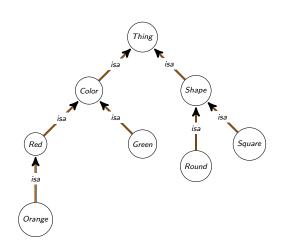
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- ullet sim is a normalized similarity measure if it has values in [0,1]

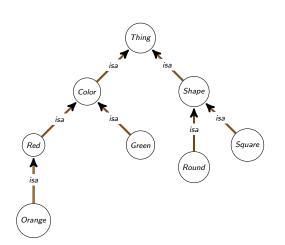




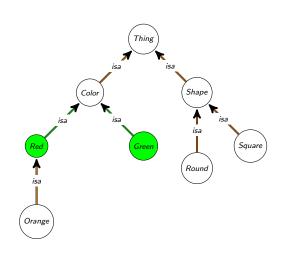
 distance on shortest path (Rada et al., 1989)



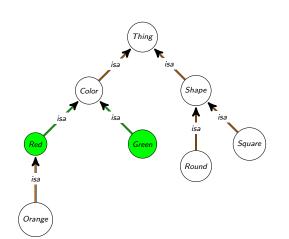
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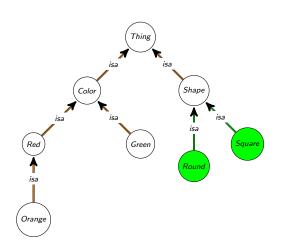
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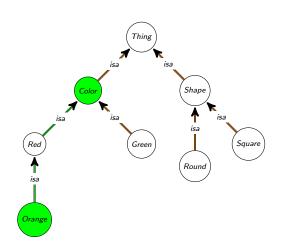
distance on shortest path



- distance on shortest path
- distance(green, red)2
- $sim_{Rada}(green, red) = \frac{1}{3}$



- distance on shortest path
- distance(square, round) = 2
 - $sim_{Rada}(square, round) = \frac{1}{3}$



- distance on shortest path
- distance(orange, color) = 2
 - $sim_{Rada}(orange, color) = \frac{1}{3}$

• shortest path is not always intuitive

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- account for different edge types
 - non-uniform edge weighting

• term specificity measure $\sigma: C \mapsto \mathbb{R}$:

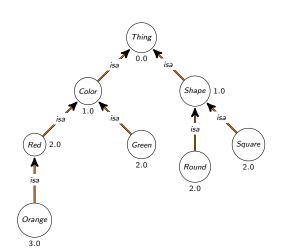
- term specificity measure $\sigma: C \mapsto \mathbb{R}$:
 - $ightharpoonup x \sqsubseteq y o \sigma(x) \ge \sigma(y)$
- intrinsic:
 - $ightharpoonup \sigma(x) = f(depth(x))$
 - $ightharpoonup \sigma(x) = f(A(x))$ (for ancestors A(x))
 - $\sigma(x) = f(D(x))$ (for descendants D(x))
 - many more, e.g., Zhou et al.:

$$\sigma(x) = k \cdot \left(1 - \frac{\log |D(x)|}{\log |C|}\right) + (1 - k) \frac{\log depth(x)}{\log depth(G_T)}$$

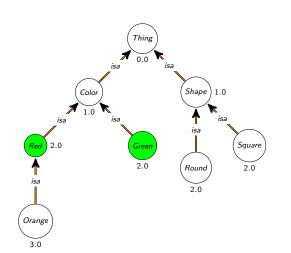
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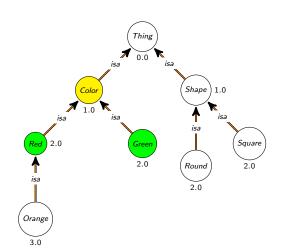
- extrinsic:
 - $ightharpoonup \sigma(x)$ defined as a function of instances (or annotations) I
 - note: the number of instances monotonically decreases with increasing depth in taxonomies
 - ► Resnik 1995: $elC_{Resnik}(x) = -\log p(x)$ (with $p(x) = \frac{|I(x)|}{|I|}$)
 - in biology, one of the most popular specificity measure when annotations are present



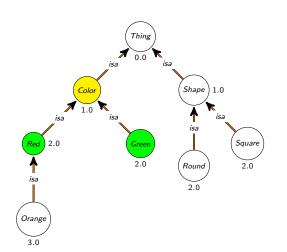
 Resnik 1995: similarity between x and y is the information content of the most informative common ancestor



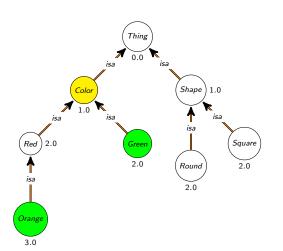
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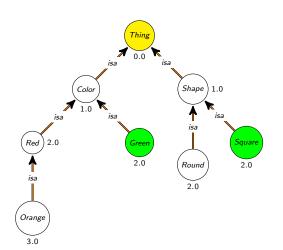
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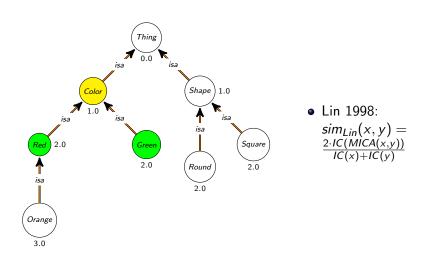


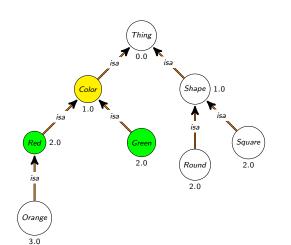
- Resnik 1995: similarity between x and y is the information content of the most informative common ancestor
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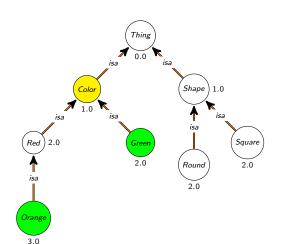
- Resnik 1995: similarity between x and y is the information content of the most informative common ancestor
 - $sim_{Resnik}(Square, Orange) \ 0.0$

- (Red, Green) and (Orange, Green) have the same similarity
- need to incorporate the specificity of the compared classes





- Lin 1998: $sim_{Lin}(x, y) = \frac{2 \cdot IC(MICA(x,y))}{IC(x) + IC(y)}$
- $sim_{Lin}(Green, Red) = 0.5$



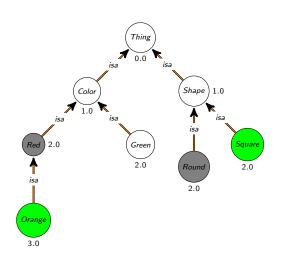
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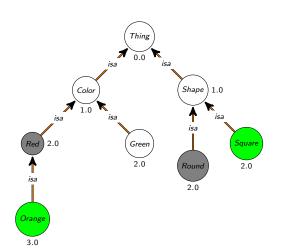
 $sim_{Lin}(Green, Orange) = 0.4$

- many(!) others:
 - ▶ Jiang & Conrath 1997
 - ► Mazandu & Mulder 2013
 - ► Schlicker et al. 2009
 - ▶ ..

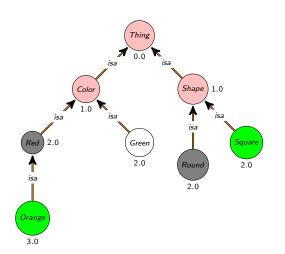
- we only looked at comparing pairs of classes
- mostly, we want to compare sets of classes
 - set of GO annotations
 - set of signs and symptoms
 - set of phenotypes
- two approaches:
 - compare each class individually, then merge
 - directly set-based similarity measures



 similarity between a square-and-orange thing and a round-and-red thing



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- Pesquita et al., 2007: $simGIC(X, Y) = \sum_{c \in A(X) \cap A(Y)} IC(c) \sum_{c \in A(X) \cup A(Y)} IC(c)$



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- $simGIC(so, rr) = \frac{2}{11}$

- alternatively: use different merging strategies
- common: average, maximum, best-matching average

▶ Average:
$$sim_A(X, Y) = \frac{\sum_{x \in X} \sum_{y \in Y} sim(x, y)}{|X| \times |Y|}$$

Max average: $sim_{MA}(X, Y) = \frac{1}{|X|} \sum_{x \in X} \max_{y \in Y} sim(x, y)$

▶ Best match average: $sim_{BMA}(X,Y) = \frac{sim_{MA}(X,Y) + sim_{MA}(Y,X)}{2}$

- Semantic Measures Library:
 - comprehensive Java library
 - ▶ http://www.semantic-measures-library.org/
- R packages: GOSim, GOSemSim, HPOSim, LSAfun, ontologySimilarity,...
- Python: sematch, fastsemsim (GO only)

Applications of semantic similarity

- no obvious choice of similarity measure
- depends on application
 - e.g., predicting PPIs in different organisms through similarity may benefit from a different similarity measure!
- different similarity measures may react differently to biases in data
- needs some testing and experience

Applications of semantic similarity

Recommendations:

- use Resnik's information content measure
- use Resnik's similarity
- use Best Match Average
- use the full ontology
- classify your ontology using an automated reasoner before applying semantic similarity
 - although many ontologies come pre-classified
- ⇒ but there are many exceptions
 - ▶ similar location ⇒ use location subset of GO
 - ▶ developmental phenotypes ⇒ use developmental branch of phenotype ontology

4,000 genetic diseases in OMIM, 6,000 in OrphaNet, have an unknown molecular basis

OMIM[®]

Online Mendelian Inheritance in Man®

An Online Catalog of Human Genes and Genetic Disorders

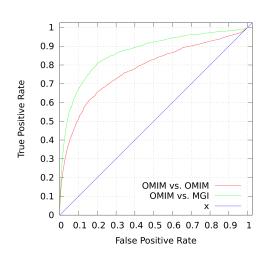
Prefix	Autosomal	X Linked	Y Linked	Mitochondrial	Totals
* Gene description	12,750	627	48	35	13,460
+ Gene and phenotype, combined	250	14	0	2	266
# Phenotype description, molecular basis known	2,836	240	4	28	3,108
% Phenotype description or locus, molecular basis unknown	1,628	135	5	0	1,768
Other, mainly phenotypes with suspected mendelian basis	1,819	130	2	0	1,951
Totals	19,283	1,146	59	65	20,553



Semantic similarity over phenotype ontologies measures phenotypic similarity

- semantic similarity: similarity measure based on information contained in the axioms/structure of an ontology
 - ▶ anatomy: front limb hind limb vs. front limb eye
 - ► function: detection of salty taste detection of sweet taste vs. detection of salty taste apoptosis
 - ▶ quality: red orange vs. red green vs. red round
- ullet \Rightarrow phenotypic similarity combines similarity between anatomy, function, and quality

	GENOTYPE			
ALSM1(NM_015120.4) [c.10775delC] + [-]	B6.Cg-Alms1 ^{foz/fox} /J	kcnj11c14/c14; insr4143/+(AB)		
0,6				
obesity, diabetes mellitus, insulin resistance	increased food intake, hyperglycemia, insulin resistance	increased weight, adipose tissue volume, glucose homeostasis altered		
	PHENOTYPE	1		



• AUC (OMIM): 0.82

• AUC (MGI): 0.90

Bassoe Syndrome

Signs and symptoms

- skeletal:
 - kyphosis, hypertensible joints, cubitus valgus
- muscular:
 - hypotonia, muscle hypotrophy, amyotrophy
- behavior:
 - ► abnormal gait, amimia
- visual:
 - cataract, strabismus
- reproductive:
 - hypogonadism, hypogenitalism, abnormal ovaries, hypoplastic testis, reduced fertility

Bassoe Syndrome

HIP1 mouse phenotypes

Bassoe Syndrome:

- kyphosis, hypertensible joints, cubitus valgus
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Mouse phenotypes:

- kyphosis, abnormal spine curvature, lordosis
- abnormal muscle morphology
- abnormal gait, hypoactivity, tremors
- nuclear cataracts, microphthalmia
- testicular atrophy, male infertility

An integrative, translational approach to understanding rare and orphan genetically based diseases. Interface Focus, 2013.

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Mouse phenotypes:

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- abnormal muscle morphology, muscle hypotrophy, muscle wasting
- abnormal gait, hypoactivity, tremors, failure to thrive, ataxia
- nuclear cataracts, microphthalmia
- testicular atrophy, male infertility, ovarian abnormalities, testicular degeneration, increased apoptosis of postmeiotic spermatids, oligospermia

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Machine learning with ontologies: approaches

- syntactic: treat axioms as "sentences" using language models
- graph-based: treat ontologies as graphs (like in semantic similarity)
- model-theoretic: encode model-theoretic semantics in optimization

Ontologies: axioms, not graphs!

Overview	Browse DLQuery Download
Annotation	Value
label	B cell apoptotic process
definition	Any apoptotic process in a B cell, a lymphocyte of B lineage with the phenotype CD19-positive and capable of B cell mediated immunity.
class	http://purl.obolibrary.org/obo/GO_0001783
ontology	GO-PLUS
Equivalent	apoptotic process and (occurs in some B cell)
SubClassOf	occurs in some B cell, lymphocyte apoptotic process
id	GO:0001783
has_obo_name	space biological_process

Ontologies: axioms, not graphs!

Gene Ontology:

- behavior DisjointWith: 'developmental process'
- behavior SubclassOf: only-in-taxon some metazoa
- 'cell proliferation' DisjointWith: in-taxon some fungi
- 'cell growth' EquivalentTo: growth and ('results in growth of' some cell)

• ...

Ontology embeddings

Definition

Let $O = (\Sigma = (C, R, I); ax; \vdash)$ be an ontology with a set of classes C, a set of relations R, a set of instances I, a set of axioms ax and an inference relation \vdash . An ontology embedding is a function $f_{\eta}: C \cup R \cup I \mapsto \mathbb{R}^n$ (or $\Sigma(O) \mapsto \mathbb{R}^n$.

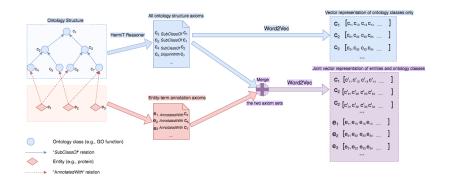
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For example, we can use co-occurrence within ax^{\vdash} to constrain the embedding function, where the constraints on co-occurrence are formulated using the Word2Vec skipgram model.

Onto2Vec



Word2Vec

Maximize:

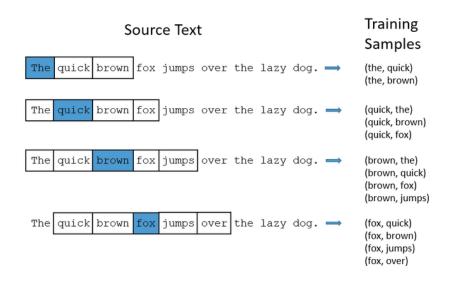
$$\frac{1}{N} \sum_{n=1}^{N} \sum_{-c \le j \le c, j \ne 0} \log p(w_{n+j}|w_n) \tag{1}$$

with

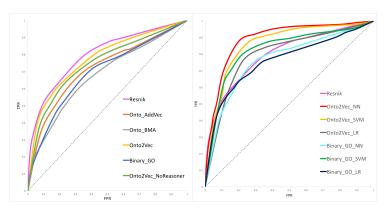
$$p(w_o|w_i) = \frac{\exp(v_{w_o}^{\prime T} v_{w_i})}{\sum_{w=1}^{W} \exp(v_w^{\prime T} v_{w_i})}$$
(2)

(at least conceptually; different strategies are used to approximate Eqn. 2)

Word2Vec

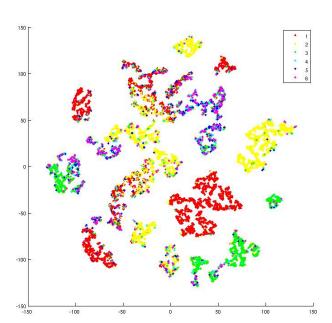


Predicting PPIs: trainable similarity measures



Smaili et al. Onto2Vec: joint vector-based representation of biological entities and their ontology-based annotations.

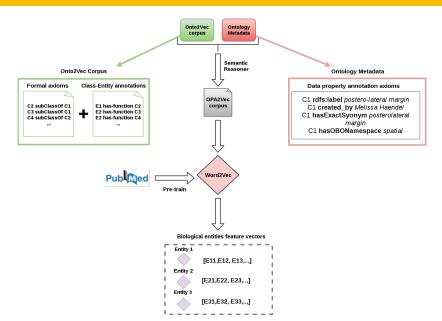
Visualizing embeddings



Combination with text

- ontologies contain more than axioms:
 - ▶ labels, synonyms, definitions, authors, etc.
- Description Logic axioms != natural language
- transfer learning: learn on one domain/task, apply to another
 - e.g.: learn on literature, apply to ontologies
 - words have "meaning" in literature, Description Logic symbols have "meaning" in ontology axioms
- Ontologies Plus Annotations 2 Vec (OPA2Vec) combines both

Ontologies Plus Annotations 2 Vec



Axioms contribute to prediction tasks: GO and GO-PLUS

	Human	Yeast	Arabidopsis
GO_Onto2Vec	0.7660	0.7701	0.7559
GO_Onto2Vec_NN	0.8779	0.8711	0.8364
GO_plus_Onto2Vec	0.7880	0.7943	0.7889
$GO_plus_Onto2Vec_NN$	0.9021	0.8937	0.8834

Evaluating individual axioms

Testing how much each ontologies' axioms contribute to predictions:

	Hu	ıman	Arabidopsis		
	Onto2Vec	Onto2Vec_NN	Onto2Vec	Onto2Vec_NN	
GO (Baseline)	0.7660	0.8779	0.7559	0.8364	
ChEBI	0.7899(+0.0239)	0.8914(+0.0135)	0.7703(+0.0144)	0.8518(+0.0154	
PO	0.7752(+0.0092)	0.8776(-0.0003)	0.7671(+0.0112)	0.8469(+0.0105)	
CL	0.7743(+0.0083)	0.8810(+0.0031)	0.7612(+0.0053)	0.8371(+0.0007)	
PATO	0.7657(-0.0003)	0.8768(-0.0011)	0.7563(+0.0004)	0.8380(+0.0016)	

Evaluating definitions

Testing how much each ontologies' annotation properties contribute to predictions:

	F	luman	Arabidopsis		
	Onto2Vec	Onto2Vec_NN	Onto2Vec	Onto2Vec_NN	
GO (Baseline)	0.8727	0.9033	0.8613	0.8903	
ChEBI	0.8571(-0.0156)	0.8801(-0.0232)	0.8601(-0.0012)	0.8880(-0.0023)	
PO	0.8680(-0.0047)	0.8824(-0.0209)	0.8632(+0.0019)	0.8908(+0.0005)	
CL	0.8811(+0.0084)	0.9037(+0.0004)	0.8614(+0.0001)	0.8899(-0.0004)	
PATO	0.8562(-0.0165)	0.8711(-0.0322)	0.8544(-0.0069)	0.8860(-0.0043)	

OPA2Vec

- https:
 //github.com/bio-ontology-research-group/opa2vec
- command line tool
 - input: OWL ontology, set of entities with annotations/associations
 - output: vectors for each class and entity
- includes Elk and HermiT
- limitations: word-based
 - completely ignores any semantics!

More

https://github.com/bio-ontology-research-group/ontology-tutorial

- more slides
 - ontology theory
 - machine learning
 - applications
- code examples, executable notebooks, all dockerized!
 - predict gene-disease associations through phenotype similarity
 - protein-protein interactions