```
speciesPattenAll = Flatten[Table[{i, j, k, l, p},
                          L表格
                  」玉平
    \{i, -1, 1\}, \{j, -1, 1\}, \{k, -1, 1\}, \{l, -1, 1\}, \{p, -1, 1\}], 4];
deletePatten1 = Flatten[Table[{i, j, k, l, p}, {i, 0, 1},
               压平
                      |表格
    {j, 0, 1}, {k, 0, 1}, {l, 0, 1}, {p, 0, 1}], 4];
deletePatten2 = Flatten[Table[{i, j, k, l, p}, {i, -1, 0},
               压平
                       __表格
    {j,-1,0}, {k,-1,0}, {l,-1,0}, {p,-1,0}], {4};
speciesPatten = Complement[speciesPattenAll, deletePatten1, deletePatten2];
(*This function return all possible reactant
matrices corresponding to a stoichiometric matrix*)
coresAlpha[capitalN_] := Block[{n = capitalN},
  alpha = Table[0, {i, 4}, {j, 5}];
         L表格
  oneposi = Position[n, 1];
           位置
  zeroposi = Position[n, 0];
            位置
  minusoneposi = Position[n, -1];
                |位置
  Do[alpha[oneposi[i, 1], oneposi[i, 2]] = 0, {i, 1, Length@oneposi}];
  Do[alpha[minusoneposi[i, 1]], minusoneposi[i, 2]] = 1,
   {i, 1, Length@minusoneposi}];
         上长度
  coefs = Tuples[{0, 1}, Length@zeroposi];
  Table[temp = alpha;
   Do[temp[zeroposi[i, 1]], zeroposi[i, 2]] = coefs[j, i],
    {i, 1, Length@zeroposi}];
          |长度
   temp, {j, 1, Length@coefs}]
]
```

```
(*For two matrices A and B with the same size,
      LFor循环
    if rowcolTally[{A,1}]=rowcolTally[{B,1}],
    then A can be obtained by swapping the rows and
     columns from B (i.e., A and B are naturally equivalent)*)
    rowcolTally[{A_, index_}] := Block[{a = A, ind = index},
      aa = speciesPatten[a];
      rowA = Tally[Sort[Tally /@ Sort /@ aa]];
                 colA = Tally[Sort[Tally /@ Sort /@ Transpose@aa]];
                  |排序 |重复次数 |排序
      {{rowA, colA}, ind}
In[54]:= ParallelSow[expr_] := Sow[expr];
    SetSharedFunction[ParallelSow]
    し设置共享函数
In[46]:= S = 4;
    m = 5;
    allh = Table[Symbol["h" <> ToString[i]], {i, 1, s}];
                              上转换为字符串
           L表格 L符号
    (*We start by finding out all stoichiometric matrices
     (namely capitalN) that admit a positive steady state*)
    capitalNWithSteadyState = Reap[ParallelDo[
                              L收获 L并行Do循环
          capitalN = {speciesPatten[i],
            speciesPatten[[j]], speciesPatten[[k]], speciesPatten[[l]]};
          If[MatrixRank[capitalN] # 4, Continue[]];
          └… └矩阵的秩
                                      | 继续
          ker = NullSpace@capitalN;
               零空间
          If[Length@ker # 1, Continue[]];
         L… L长度
                            |继续
          If[Cases[ker[1], Except[(a_ /; a > 0)]] # {}, Continue[]];
          └… |模式匹配
                          |除了
          ParallelSow[{i, j, k, l}];
          , \{i, 1, 180\}, \{j, i+1, 180\}, \{k, j+1, 180\}, \{l, k+1, 180\}]]; //
     AbsoluteTiming
     绝对时间
Out[•]= {5047.25, Null}
```

In[7]:= capitalNWithSteadyState[2][1]

```
\{\{41, 42, 48, 83\}, \{41, 42, 48, 84\}, \{41, 42, 48, 97\}, \{41, 42, 48, 98\},
        {41, 42, 48, 143}, {41, 42, 48, 144}, {41, 42, 48, 145}, {41, 42, 48, 146},
        \{41, 42, 48, 147\}, \{41, 42, 48, 148\}, \{41, 42, 48, 149\}, \{41, 42, 48, 152\},
         \cdots 2514983 \cdots, {24, 155, 163, 171}, {24, 155, 164, 165},
Out[7]=
        \{24, 155, 164, 171\}, \{24, 156, 163, 168\}, \{24, 156, 163, 171\},
        {24, 156, 163, 174}, {24, 156, 164, 174}, {24, 156, 166, 174},
        \{24, 163, 165, 171\}, \{24, 163, 168, 171\}, \{24, 164, 165, 171\}\}
       大型输出
                 显示更少
                            显示更多
                                      显示全部
                                                设定大小限制...
```

Info]:= Length@capitalNWithSteadyState[2][1]

Out[]= 2515006

In[22]:= allcapitalNwithindex =

Transpose@{capitalNWithSteadyState[2][1], Range[2515006]}

```
\{\{41, 42, 48, 83\}, 1\}, \{\{41, 42, 48, 84\}, 2\}, \{\{41, 42, 48, 97\}, 3\},
         \{\{41, 42, 48, 98\}, 4\}, \{\{41, 42, 48, 143\}, 5\}, \{\{41, 42, 48, 144\}, 6\},
         \{\{41, 42, 48, 145\}, 7\}, \dots 2514992\dots\}, \{\{24, 156, 163, 171\}, 2515000\},
         \{\{24, 156, 163, 174\}, 2515001\}, \{\{24, 156, 164, 174\}, 2515002\},
Out[22]=
         \{\{24, 156, 166, 174\}, 2515003\}, \{\{24, 163, 165, 171\}, 2515004\},
         \{\{24, 163, 168, 171\}, 2515005\}, \{\{24, 164, 165, 171\}, 2515006\}\}
        大型输出
                   显示更少
                             显示更多
                                        显示全部
                                                   设定大小限制...
```

In[25]:= alltally = ParallelMap[rowcolTally, allcapitalNwithindex] // AbsoluteTiming

```
\{211.102, \{\{\{\{\{-1,3\},\{1,2\}\},1\},\{\{\{-1,1\},\{0,2\},\{1,2\}\},1\},
               \{\{\{-1,3\},\{0,1\},\{1,1\}\},2\}\},\{\{\{\{-1,1\},\{1,3\}\},1\},
               \{\{\{-1,3\},\{0,1\}\},1\},\{\{\{-1,2\},\{0,1\},\{1,1\}\},3\}\}\},1\},
           \cdots 2515004 \cdots, \{\{\{\{\{-1,2\},\{1,3\}\},1\},\{\{\{-1,2\},\{0,1\},\{1,2\}\},3\}\},
Out[25]=
              \{\{\{\{-1,1\},\{1,3\}\},1\},\{\{\{-1,2\},\{1,2\}\},1\},\{\{\{-1,3\},\{0,1\}\},1\},
               \{\{\{0,1\},\{1,3\}\},1\},\{\{\{-1,2\},\{0,1\},\{1,1\}\},1\}\}\},2515006\}\}\}
        大型输出
                   显示更少
                              显示更多
                                         显示全部
                                                    设定大小限制...
```

```
ln[34]:= allunitally = DeleteDuplicates[alltally[2]], #1[1]] == #2[1]] &];
                   L删除重复元素
```

```
(*All indexes of nonequivalent capitalN*)

allindex = Transpose[allunitally] [2];

[转置

In[39]:= Length@allindex

长度

Out[39]= 8436
```

```
(*All 4s5m reactions with Hopf
 上全部
 bifurcations. The first number is the index in allindex,
the second number is the index in the corresponding result of coresAlpha. *)
count = 0;
SetSharedVariable[count]
し设置共享变量
Monitor[reactionsWithHB = Reap[ParallelDo[
                          L收获 L并行Do循环
       count = Max[count, i];
              L最大值
       capitalN = speciesPatten[capitalNWithSteadyState[2][1][allindex[i]]];
       ker = NullSpace@capitalN;
            零空间
       alphas = coresAlpha[capitalN];
       Do[alpha = alphas[j];
      IDo循环
        J = capitalN.DiagonalMatrix[ker[1]].
                    | 对角矩阵
          Transpose[alpha].DiagonalMatrix[allh];
                            L对角矩阵
          |转置
        a4 = Det[-J];
            __行列式
        If[a4 == 0, Continue[]];
        如果
                  L继续
        If [Cases [Expand [ (a4 - h1 h2 h3 h4 h5) * 2],
           Except[(a_*b___/; a < 0)]] == {}, Continue[]];
        a1 = Tr[-J];
            上迹
        a2 =
         Det[J[{1, 2}, {1, 2}]] + Det[J[{1, 3}, {1, 3}]] + Det[J[{1, 4}, {1, 4}]] +
          Det[J[{2,3},{2,3}]] + Det[J[{2,4},{2,4}]] + Det[J[{3,4},{3,4}]];
                                  _ 行列式
        a3 = -Det[J[{1, 2, 3}, {1, 2, 3}]] - Det[J[{1, 2, 4}, {1, 2, 4}]] -
          Det[J[{1, 3, 4}, {1, 3, 4}]] - Det[J[{2, 3, 4}, {2, 3, 4}]];
        dH3 = a1 * a2 * a3 - a3 * a3 - a1 * a1 * a4;
        If[Cases[Expand[(dH3) * 2], Except[(a_* b_{--} /; a > 0)]] == {},
                [展开
        [… |模…
                                    [除了
         Continue[], ParallelSow[{i, j}];];
         L继续
        , {j, 1, Length@alphas}];
       , {i, 1, 8436}]]; // AbsoluteTiming, count]
                          L绝对时间
```

Out[145]= { 164.229, Null}

In[244]:= reactionsWithHB[2][1]

```
\{673, 5\}, \{673, 23\}, \{673, 25\}, \{673, 55\}, \{673, 133\}, \{673, 172\}, \{291, 11\},
          \{674, 28\}, \{291, 27\}, \{674, 87\}, \{100, 12\}, \{291, 69\}, \{291, 85\}, \{484, 105\},
          \{195, 69\}, \{484, 106\}, \{195, 101\}, \{484, 149\}, \{484, 233\}, \{484, 234\},
          \{102, 283\}, \{102, 295\}, \{389, 98\}, \{389, 146\}, \{102, 364\}, \{389, 169\},
          \{295, 22\}, \{389, 182\}, \{102, 411\}, \dots, \{7864, 332\}, \{7864, 334\},
          \{7864, 348\}, \{7864, 362\}, \{7864, 364\}, \{7864, 518\}, \{7864, 520\}, \{7864, 551\},
Out[244]=
          \{7864, 552\}, \{7864, 559\}, \{7864, 575\}, \{7864, 615\}, \{7864, 623\},
          \{7864, 774\}, \{7864, 815\}, \{7864, 831\}, \{7864, 844\}, \{7864, 860\},
          \{7865, 97\}, \{7866, 28\}, \{7866, 32\}, \{7866, 50\}, \{7866, 92\}, \{7866, 158\},
          \{7866, 196\}, \{7866, 200\}, \{7866, 204\}, \{7866, 215\}, \{7866, 387\}\}
                                         显示全部
                   显示更少
                              显示更多
                                                    设定大小限制..
         大型输出
In[146]:= Length[reactionsWithHB[2][1]]
Out[146]= 35 169
```

```
In[267]:= all4s5mReactionswithHB = ParallelTable[temp2 = reactionsWithHB[[2]][[1]][i]];
                               并行产生表格
         capitalN =
          speciesPatten[capitalNWithSteadyState[2][1][allindex[temp2[1]]]]];
         alpha = coresAlpha[capitalN] [temp2[2]]];
         beta = alpha + capitalN;
         Transpose[{alpha, beta}], {i, 1, 35169}];
        _转置
In[270]:= Export["/Users/aspirin/Desktop/all4s5mReactionswithHB.txt",
      all4s5mReactionswithHB, "Table"]
```

Out[270]= /Users/aspirin/Desktop/all4s5mReactionswithHB.txt