

## Assignment - I

Q. Show that if  $L$  is regular, so  $L - \{\lambda\}$ .

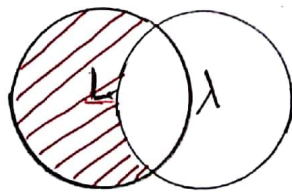
→ A language is regular, by definition, if you can create a DFA for it.

The regular languages are closed under the various operations. means result of the different operations are also regular.

Example: If  $L$  and  $\lambda$  is regular then

Union  $L \cup \lambda$ , intersection  $L \cap \lambda$ , and complement of  $L$  and  $\lambda$  are also regular, hence also relative complement  $L - \{\lambda\}$  is regular.

Consider the diagram --->



if  $L$  and  $\lambda$  is regular then  $L - \{\lambda\}$  is shown by red part of this diagram and it also regular. Same if  $\lambda \in L$  then  $L - \{\lambda\}$  is also regular.

## Assignment - II

Exhibit an algorithm that, given any regular language  $L$ , determine whether or not  $L = L^*$ .  
 $\text{Regular}(L) \rightarrow \text{Regular}(L^*)$ , but that does not mean that  $L = L^*$ . Just because two languages are both regular does not mean that they are the same regular language. For instance  $a^*$  and  $b^*$  are both regular languages, but this does not make them the same language.

A example of  $L \neq L^*$  would be the language  $L = a^*b^*$ , and thus  $L^* = (a^*b^*)^*$ . The string  $abab$  is part of  $L^*$  but not part of  $L$ .

As far as an algorithm goes, let me remind you that the concept of a regular language is one that can be parsed by a DFA - and for any given DFA, there is a single optional reduction of that DFA.