FINAL EXAMINATION ECON 103, STATISTICS FOR ECONOMISTS

May 9th, 2016

YOU HAVE 120 MINUTES TO COMPLETE THIS EXAM. GRAPHING CALCULATORS, NOTES, AND TEXTBOOKS ARE NOT PERMITTED.

I pledge that, in taking and preparing for this exam, I have abided by the University of Pennsylvania's Code of Academic Integrity. I am aware that any violations of the code will result in a failing grade for this course.

Name:			
Student ID $\#$:			
Signature:			

Question:	1	2	3	4	5	Total
Points:	50	30	30	30	60	200
Score:						

Instructions: Answer all questions in the space provided, continuing on the back of the page if you run out of space. Show your work for full credit but be aware that writing down irrelevant information will not gain you points. Be sure to sign the academic integrity statement above and to write your name and student ID number on *each page* in the space provided. Make sure that you have all pages of the exam before starting.

Warning: If you continue writing after we call time, even if this is only to fill in your name, twenty-five points will be deducted from your final score. In addition, two points will be deducted for each page on which you do not write your name and student ID.

- 1. This question concerns the so-called "Rademacher" random variable, a very simple discrete RV that we did not study in Econ 103: it takes on the values -1 and 1 with equal probability and never takes on any other values.
- [4] (a) Suppose $X \sim \text{Rademacher}$. Calculate E[X]

(b) Suppose $X \sim \text{Rademacher. Calculate } Var[X]$

(c) Write out the CDF of the Rademacher RV.

[8] (d) Suppose $X_1, X_2, X_3 \sim$ iid Rademacher and define $Z = X_1 + X_2 + X_3$. Write out the support set and pmf of Z.

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10	(e)	Write an R function called rrad that makes iid Rademacher draws. a single argument n the number of iid draws and return a vector of	
10	(f)	Using the function rrad that you constructed in the preceding part that uses 10000 simulation replications to approximate the probabilit of 100 iid Rademacher draws will be larger than 10.	
8	(g)	Use the Central Limit Theorem to calculate the approximate value of that you wrote simulation code to approximate in the preceding par	

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- 2. Answer each of the following: show your work or explain briefly, as applicable.
- [5] (a) Let $Y \sim N(\mu = -2, \sigma^2 = 25)$. Approximately what is P(Y > 8)?
- [5] (b) Let X be a continuous RV with pdf f(x) and support set $(-\infty, \infty)$. Write down the expression for P(X > 2) in terms of f.
- [5] (c) Let $Z = X^2$ where $X \sim N(0,1)$. What kind of RV is Z? If it has any parameters, what values do they take?

(d) The Exponential(λ) random variable is a continuous RV that we did not study in class. It has one parameter, $\lambda > 0$, its support set is $[0, \infty)$ and its CDF is given by $F(x) = 1 - e^{-\lambda x}$. Calculate the pdf of this RV.

(e) Use the Shortcut Rule to prove that Cov(X, aY) = aCov(X, Y) for any RVs X, Y and any constant a.

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3. Suppose we have two independent random samples: $X_1, \ldots, X_{10} \sim \text{iid } N(\mu_x, \sigma_X^2 = 10)$ and $Y_1, \ldots, Y_{10} \sim \text{iid } N(\mu_Y, \sigma_Y^2 = 10)$ and we wish to test $H_0: \mu_X = \mu_Y$ against the two-sided alternative at the 5% level. Derive an expression for the power of this test as a function of the true, unknown difference of population means $\Delta = \mu_X - \mu_Y$. Your solution should involve the R command pnorm.

- 4. Grace polled a random sample of 800 US voters and asked them two yes or no questions:
 - Q1 (CAR) Do you own a car?
 - Q2 (TAX) Do you favor raising the federal gasoline tax to combat climate change?

The following cross-tab contains the results of Grace's poll:

		CA	AR	
		yes	no	
TAX	yes	255	137	392
IAA	no	350	58	408
		605	195	n = 800

	3	(a)	What	is	Grace's	estimate	of	the	fraction	of	US	voters	who	favor	raising	the	tax'
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4	(b)	Grace decides to test the null hypothesis that half of US voters favor raising the tax. What is the value of her test statistic? Be sure to fully impose the null.
5	(c)	Write down the R code that Grace would use to compute the two-sided p-value given for her test from the preceding part.
3	(d)	Continuing from the preceding part, would Grace reject her null hypothesis against the two-sided alternative at the 10% significance level?
12	(e)	Next Grace decides to test the null hypothesis that equal fractions of car-owners and non-car-owners support raising the gasoline tax. What is the value of her test statistic? Be sure to fully impose the null.
3	(f)	Continuing from the preceding part, would Grace reject her null hypothesis against the two-sided alternative with $\alpha=0.01?$
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5. This question concerns an R dataframe called trump that contains data for all 227 precincts in the 2016 New Hampshire Republican presidential primary. Here are the first few rows of the data:

```
> head(trump)
```

```
town d_trump pvi hhinc
1 Acworth 41.61074 Rep 57.26225
2 Albany 43.20000 Rep 58.55520
3 Alexandria 53.00546 Dem 56.25000
4 Allenstown 49.07010 Dem 54.76777
5 Alstead 45.19573 Rep 61.07143
6 Alton 42.74953 Dem 65.61787
```

Each row is a precinct: town gives the name of the precinct, while d_trump gives Donald Trump's vote share in percentage points. The column pvi is a dummy variable constructed from the Cook Partisan Voter Index. A value of Rep indicates that the precinct leans Republican: it voted more Republican than the US as a whole in recent presidential elections. In contrast, a value of Dem indicates that the precinct leans Democratic: it voted more Democratic than the US as a whole in recent presidential elections. Finally, hhinc gives the average household income in a given precinct in thousands of US dollars. To take one particular example, consider row #3: Donald Trump won 53% of the vote in Alexandria, a precinct with an average household income of \$56,250 and that voted more Democratic that the US as a whole in presidential elections from the recent past. To answer this question you will need the regression results and figures from the last two pages of this exam. I suggest that you tear these out for easy reference.

(a) Write R code to generate the boxplot comparing hhinc by pvi shown on the last page of the exam. You do not need to include the titles.

(b) Briefly describe what the results of the boxplot from the preceding part suggest.

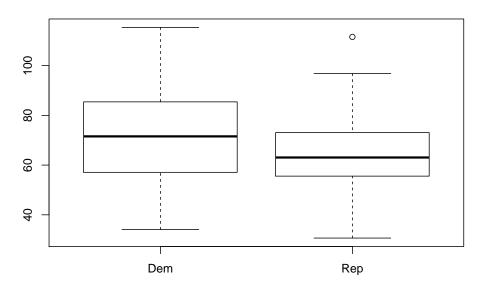
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[5] (g)	Continuing from the preceding part, is there a statistically significant relationship between Trump's vote share and hhinc at the 5% level based on a two-sided test?
[5] (f)	Suppose we want to predict Trump's vote share using hhinc only. Which set of regression results should we consult? For two precincts that differ by \$10,000 in average household income how would we predict Trump's vote shares to differ?
10 (e)	The final page of this exam shows to histograms of hinc: one for Democratic-leaning precincts and one for Republican-leaning precincts. Write R code to produce the plot for Republican-leaning precincts. You do not need to include the titles
[5] (d)	Construct an approximate 95% confidence interval for the difference of hhinc between Democratic-leaning and Republican-leaning precincts.
(c)	What is the average value of hhinc in Democratic-leaning precincts?

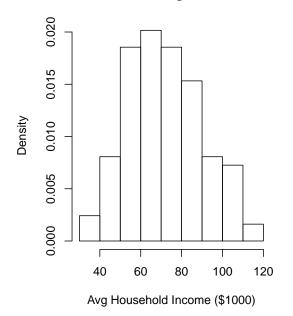
5	(h)	Where did Trump perform better: in Republican-leaning precincts or Democratic-leaning ones? How much better on average?
5	(i)	There are two sets of regression results that use <i>both</i> hhinc and pvi to predict Trump's vote share. Which are they? Briefly explain how these two regressions differ in the way that they use the two variables to make their predictions.
6	(j)	Is there evidence of a difference in the relationship between Trump's vote share and hhinc in Democratic-leaning versus Republican-leaning precincts? Explain briefly and justify your answer using a confidence interval.
4	(k)	Which regression most accurately predicts Trump's vote share? How accurate is it?
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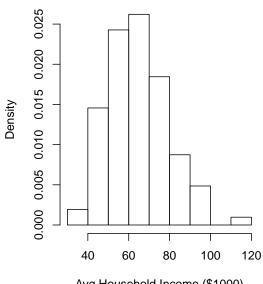
Avg Household Income (\$1000) by PVI



Dem-Leaning Precincts



Rep-Leaning Precincts



Avg Household Income (\$1000)

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