$$x(t) \Rightarrow \text{Tras formation} \qquad y(t) \Rightarrow \\ (\text{Ingresso}) \qquad \text{Tras formation} \qquad (\text{uscital}) \Rightarrow \\ y(t) = T[x(t)] \\ NB = \text{I'uscital'' y'' all' is tante} \quad \text{t'' non dipende} \\ \text{solo dall'ingresso'' x'' all' is tante} \quad \text{t''' mat dat} \\ x(t) = \text{per a octation} \\ x(t) = \text{per a octation} \\ \text{Se } x(t) = \text{q}x_1(t) + \text{b}x_2(t) \\ \text{dlove} \qquad y(t) = T[x(t)] = \text{a}T[x_1(t)] + \text{b}T[x_2(t)] \\ \text{dlove} \qquad y(t - \text{to}) = T[x(t - \text{to})] \\ \text{dlove} \qquad y(t - \text{to}) = T[x(t - \text{to})]$$

## E STAZIONARI (SLS)

$$\frac{S(t)}{T[\cdot]} = \frac{h(t)}{s}$$

$$h(t) = T [S(t)]$$

Se conosco la visposta impulsiva posso calcolare l'uscita del sistema quando in ingresso ho un segnale arbitrario

$$y(t) = x(t) \otimes h(t)$$

Dimostrazione

$$y(t) = T[x(t)] = T[x(t) \otimes d(t)] =$$

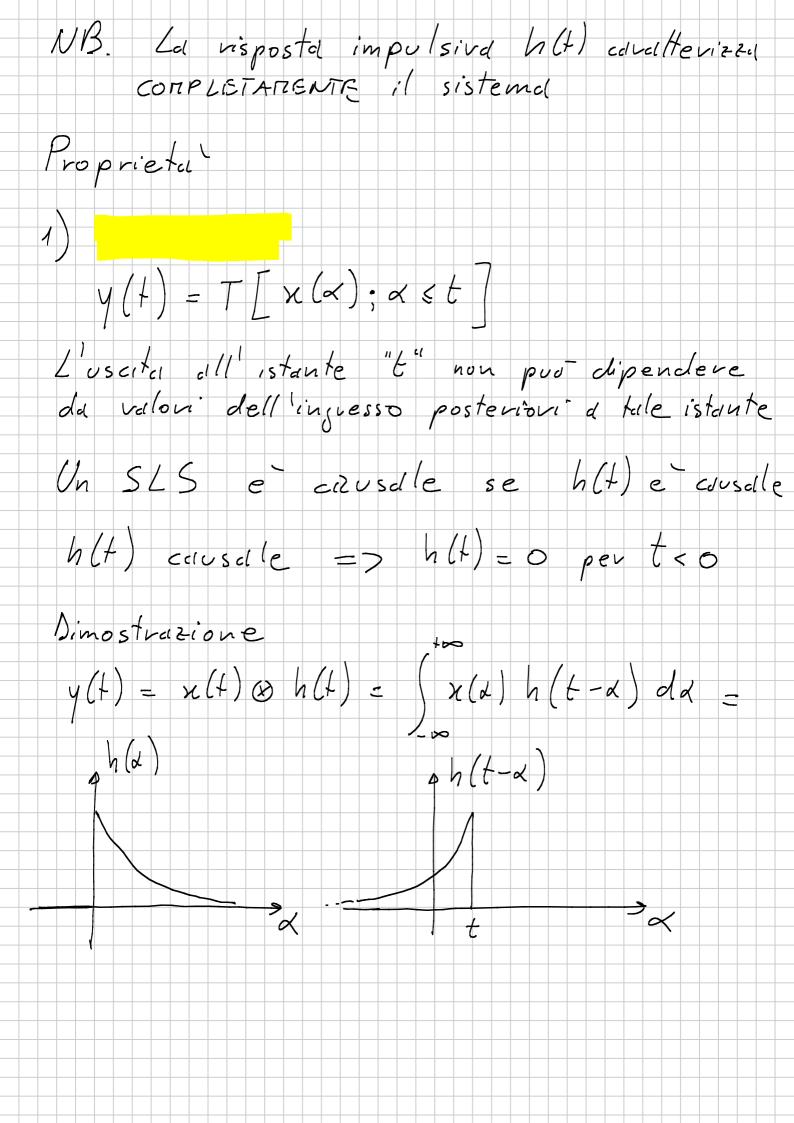
$$= T[x(t)] \times d(t) =$$

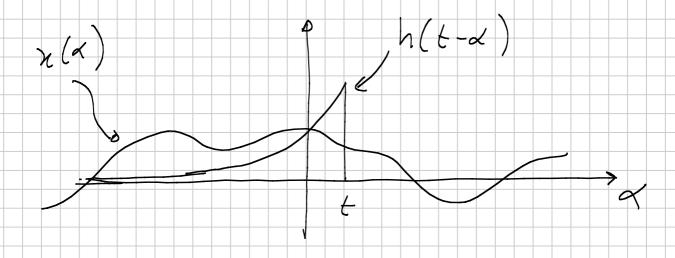
$$= T[x(t)] \times d(t) =$$

$$= T[x(t)] \times d(t) =$$

$$=\int_{-\infty}^{+\infty}\chi(\lambda)T\left[S(t-\lambda)\right]d\lambda=$$

$$= \int_{-\infty}^{+\infty} \chi(x) h(t-x) dx = \chi(t) \otimes h(t)$$





Il produtto  $\chi(\alpha)h(t-\alpha)=0$  per  $\alpha>t$ per cui y(t) non put dipendere da valori

dell'ingresso di  $\chi(t)$  posteriori à "t".

## 2) STABILITA

Se [x(t)] < M  $\forall t$  dlovel y(t) = T[x(t)] < K  $\forall t$  Pev S L S la stabilitat BIBO velle se e solo se  $|h(t)| dt < \infty$ 

Dimostruzione della sufficienzal

+00

|h(t)|=H<00

 $\langle M \rangle h (t-x) dx = M |h(x)| dx = MH$ quind: |4(+1) < K, K = MH ·) Sistemal senza memorial (istantaneo) Y(t) = T(x(t))dove "y" all isteinte "t" dipende solo del "u" all isteinte "t". ·) Sistemal con memorial É un sistemal per cui non valle la Delto y(+) = T[x(+)] il sistema e invertibile se esiste una trasformazione T-1[] tale che  $x(t) = T^{-1} \left[ Y(t) \right]$ 

$$x(t) = e^{\int_{-\infty}^{\infty} e^{\frac{t}{2\pi i} f t}} h(t) \int_{-\infty}^{\infty} h(t-d) dd = (t-d-\beta)$$

$$= \int_{-\infty}^{\infty} e^{\int_{-\infty}^{\infty} f(t-\beta)} h(\beta) d\beta = \int_{-\infty}^{\infty} e^{\int_{-\infty}^{\infty} f(t-\beta)} h(\beta) d\beta = \int_{-\infty}^{\infty} f(t-\beta) h(\beta) e^{\int_{-\infty}^{\infty} f(t-\beta)} d\beta = x(t) H(f)$$

$$= \int_{-\infty}^{\infty} h(f) \int_{-\infty}^{\infty} h(f) \int_{-\infty}^{\infty} h(f) e^{\int_{-\infty}^{\infty} f(t-\beta)} df = \int_{-\infty}^{\infty} de^{\int_{-\infty}^{\infty} h(f)} \int_{-\infty}^{\infty} h(f) e^{\int_{-\infty}^{\infty} f(t-\beta)} df = \int_{-\infty}^{\infty} de^{\int_{-\infty}^{\infty} h(f)} e^{\int_{-\infty}^{\infty} f(t-\beta)} df = \int_{-\infty}^{\infty} de^{\int_{-\infty}^{\infty} h(f)} e^{\int_{-\infty}^{\infty} f(f-\beta)} df = \int_{-\infty}^{\infty} de^{\int_{-\infty}^{\infty} h(f-\beta)} e^{\int_{-\infty}^{\infty} f(f-\beta)} df = \int_{-\infty}^{\infty} de^{\int_{-\infty}^{\infty} f(f-\beta)} e^{\int_{-\infty}^{\infty} f(f-\beta)} df = \int_{-\infty}^{\infty} de^{\int_{-\infty}^{\infty} f($$

III a definizione

 $H(\ell) \stackrel{\triangle}{=} \frac{Y(\ell)}{X(\ell)}$ 

$$u(t) = \int_{-\infty}^{t} \delta(t) dt$$

$$g(t) = \int_{-\infty}^{t} u(a) h(t-a) da = (t-a=\beta) = \int_{-\infty}^{t} h(\beta) u(t-\beta) d\beta = \int_{-\infty}^{t} h(\beta) d\beta$$

$$= \int_{-\infty}^{t} h(\beta) d\beta$$

$$= \int_{-\infty}^{t} h(\beta) d\beta$$

$$= \int_{-\infty}^{t} h(\beta) d\beta$$

$$= \int_{-\infty}^{t} h(\beta) d\beta$$

INTEGRAZIONE

$$w(t) = \int_{-\infty}^{t} x(a) da \qquad \frac{x(t)}{w(t)} = h(t) \qquad \frac{y(t)}{z(t)}$$

$$w(t) = x(t) \otimes u(t) = u(t) \otimes x(t)$$

$$z(t) = w(t) \otimes h(t) = \left[u(t) \otimes x(t)\right] \otimes h(t) =$$

$$= u(t) \otimes \left[x(t) \otimes h(t)\right] = u(t) \otimes y(t) =$$

$$= y(t) \otimes u(t) = \int_{-\infty}^{t} y(x) dx = z(t)$$

$$DERIVAZIONE$$

$$\text{La proportal dir derivatione si put decline}$$

$$\text{da quella olella integratione facendo on}$$

$$\text{nyionalmento inverso}$$

$$\frac{w(t)}{x(t)} = \int_{-\infty}^{t} x(x) dx \quad \text{allowa}$$

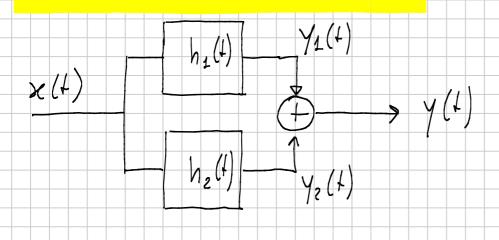
$$x(t) = \frac{d}{dt} w(t) = y(t) = \frac{d}{dt} z(t)$$

$$\frac{d}{dt} = \frac{d}{dt} v(t) = \frac{d}{dt} z(t)$$

$$\frac{d}{dt} = \frac{d}{dt} v(t)$$

$$\frac{d}{dt} = \frac{d}{dt} z(t)$$

$$\frac{d}{dt$$



$$Y(t) = Y_{1}(t) + Y_{2}(t) = X(t) \otimes h_{1}(t) + X(t) \otimes h_{2}(t) = X(t) \otimes h_{1}(t) + h_{2}(t) = X(t) \otimes h(t)$$

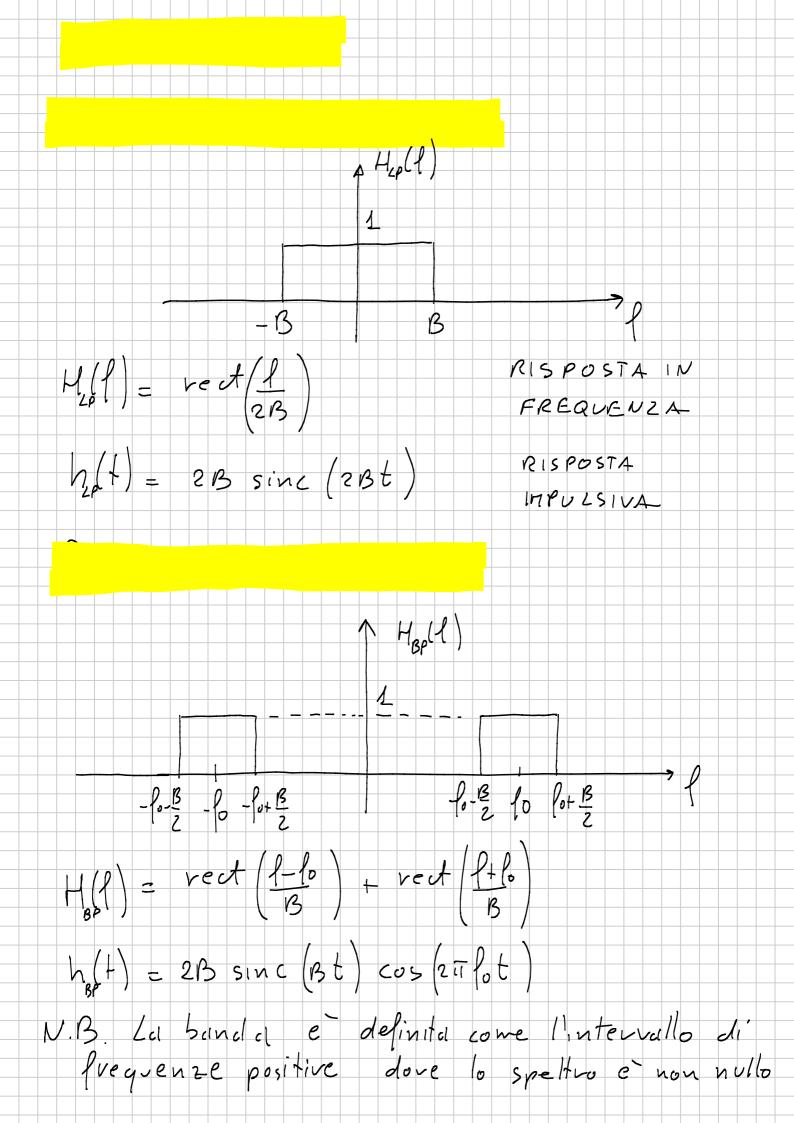
$$= X(t) \otimes [h_{1}(t) + h_{2}(t)] = X(t) \otimes h(t)$$

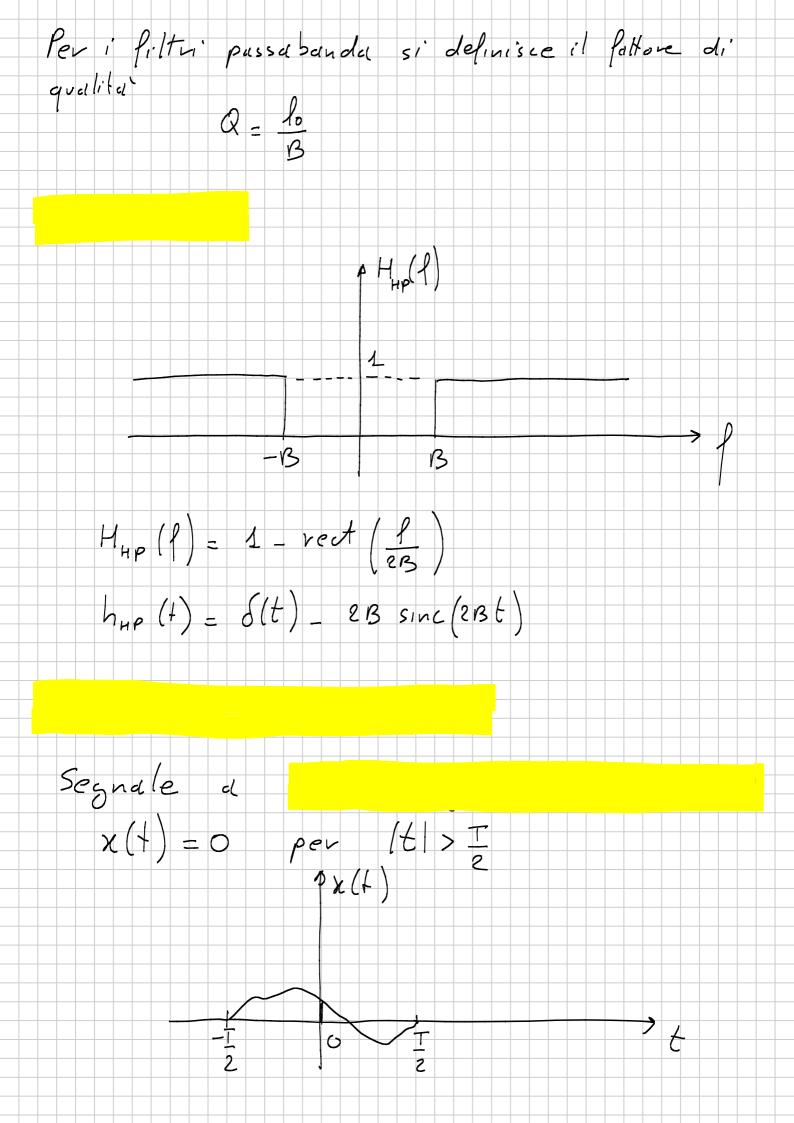
$$h(t) = h_{1}(t) + h_{2}(t)$$

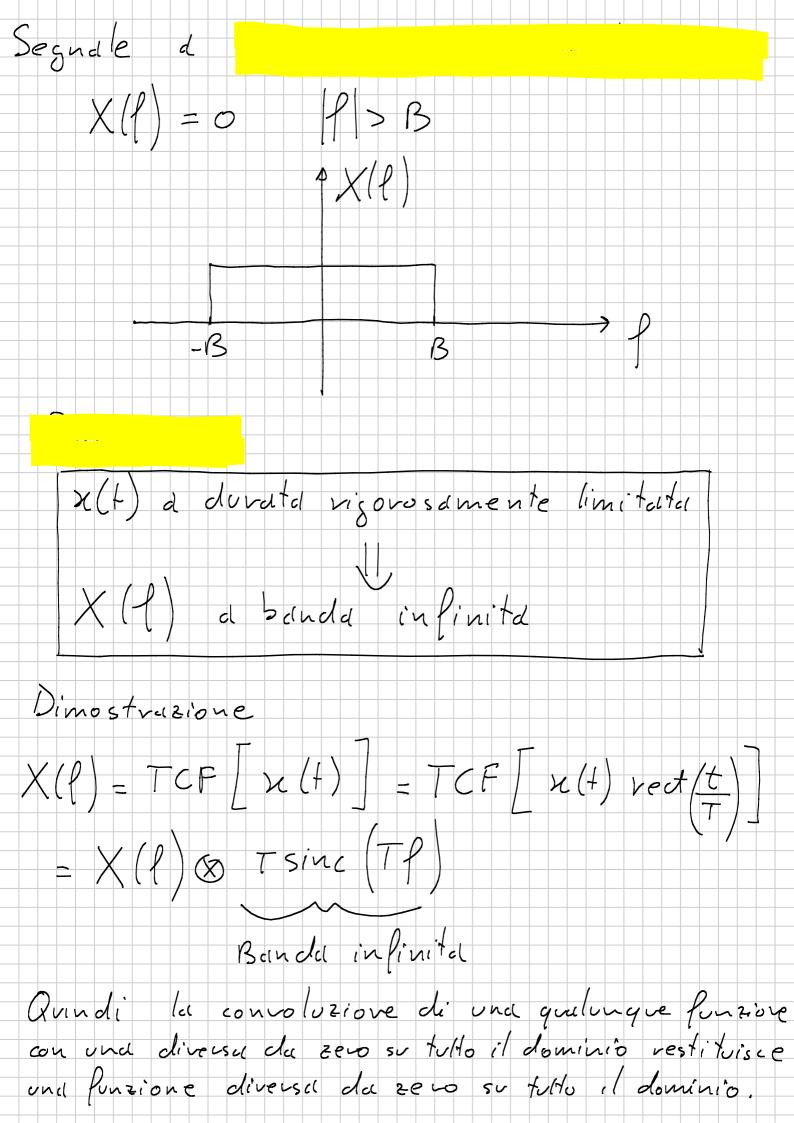
$$H(t) = H_{1}(t) + H_{2}(t)$$

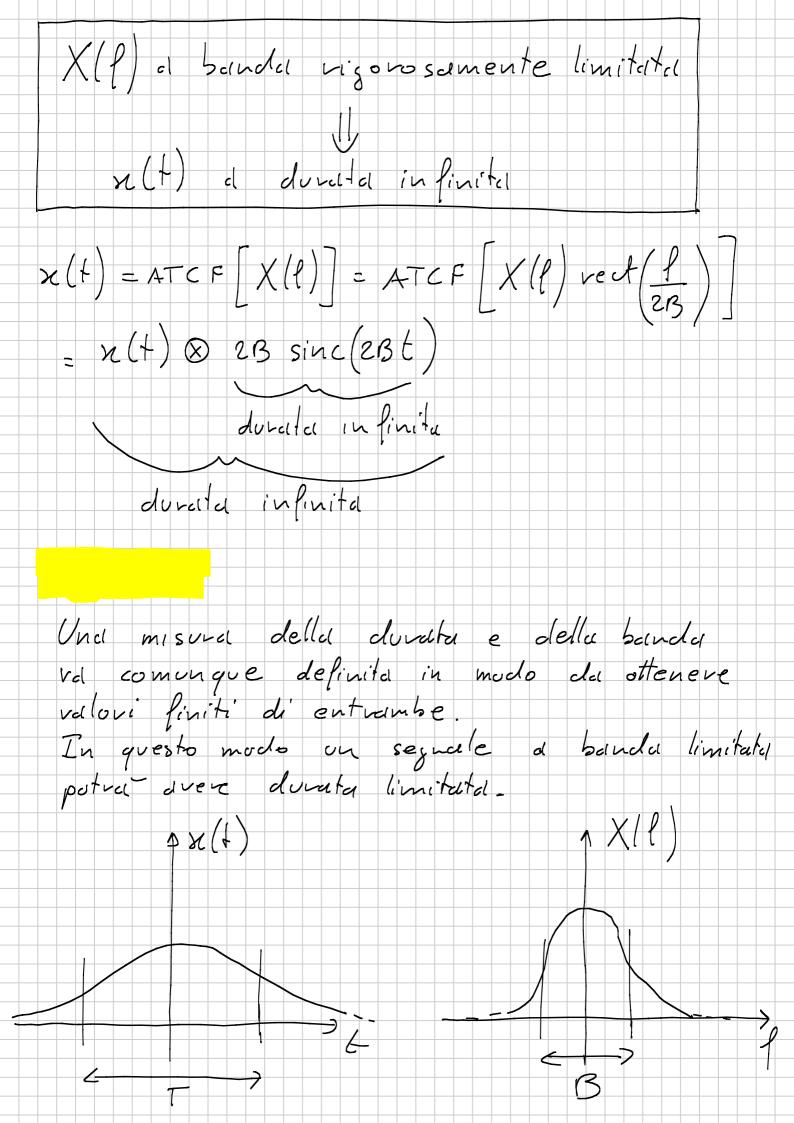
Spesso la visposta in ampiezea e rappresentata

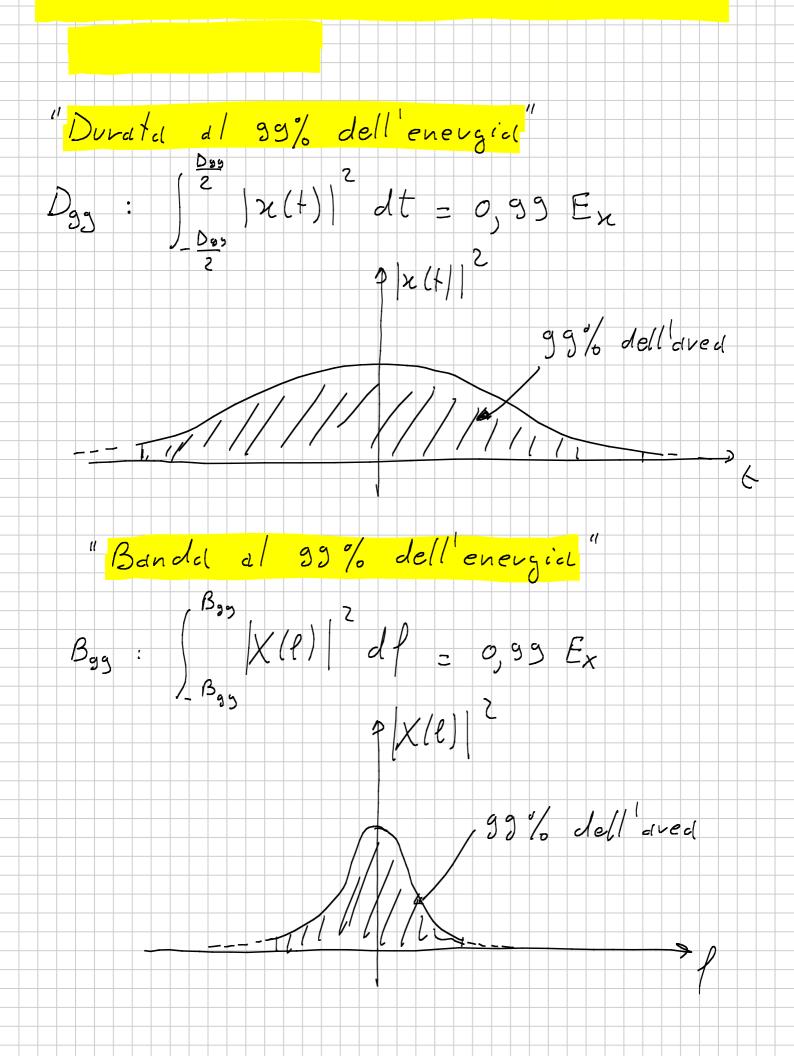
IN decibel (dB)  $X(\ell) | dB$   $X(\ell) | dB$ 

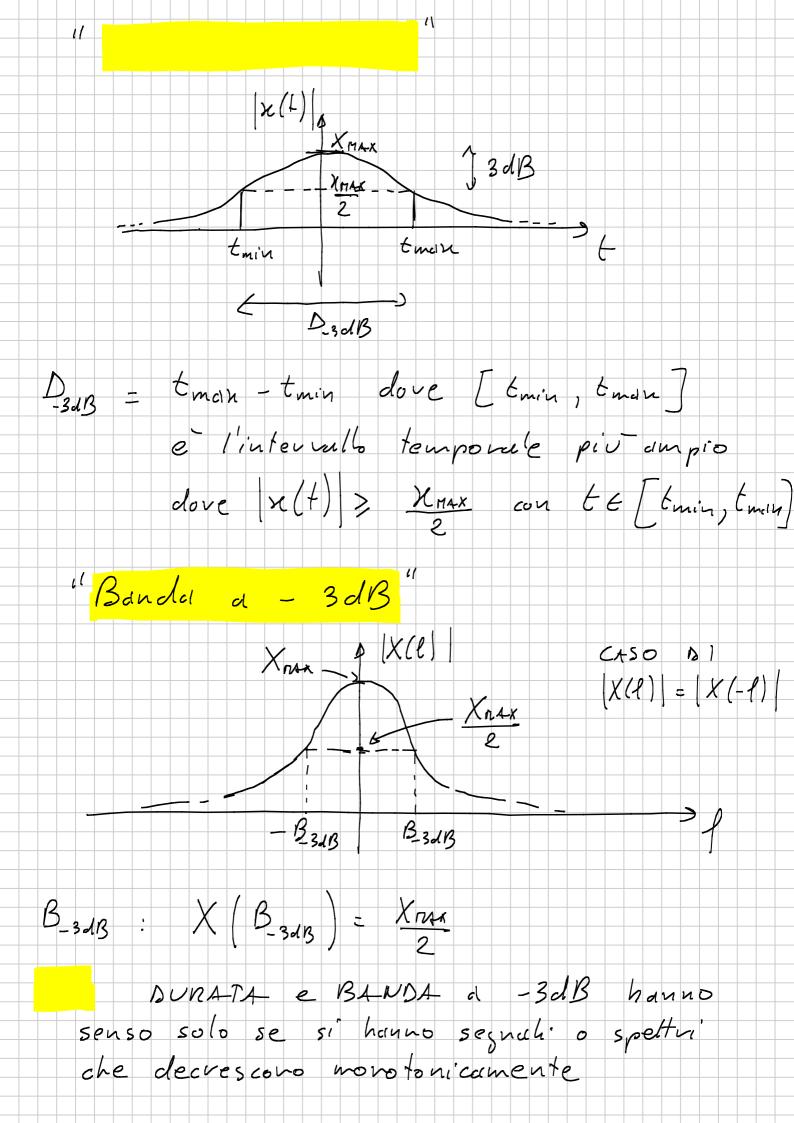


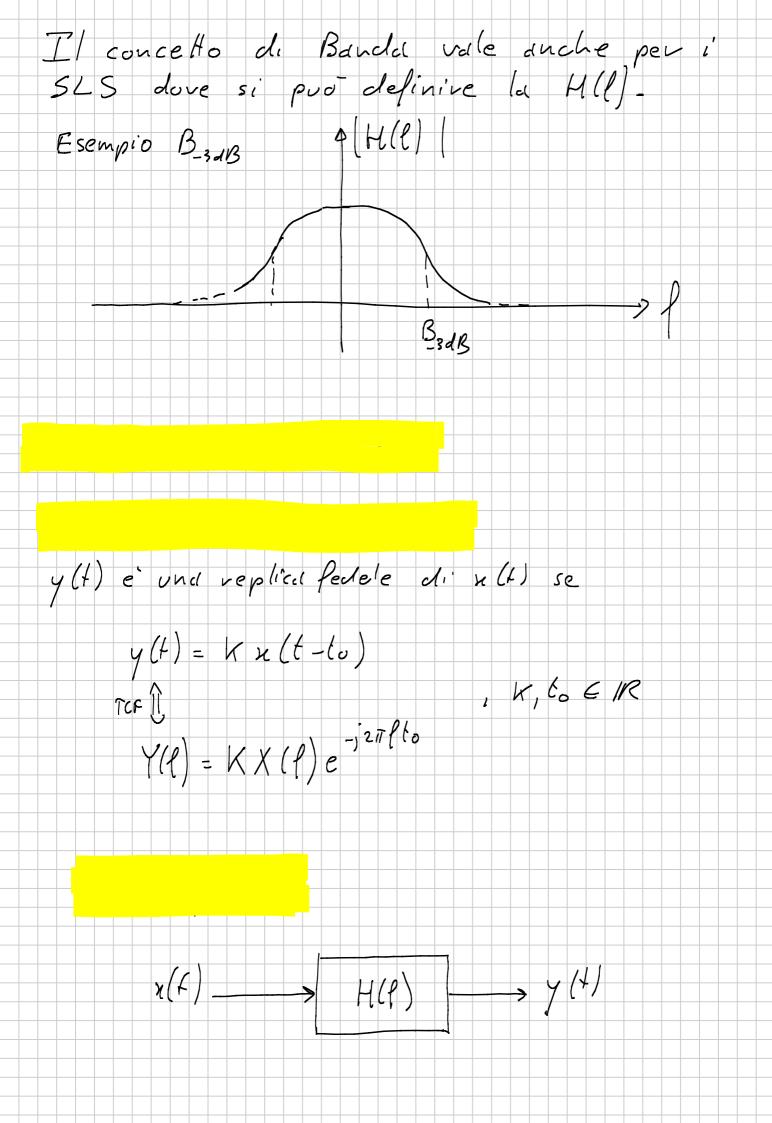


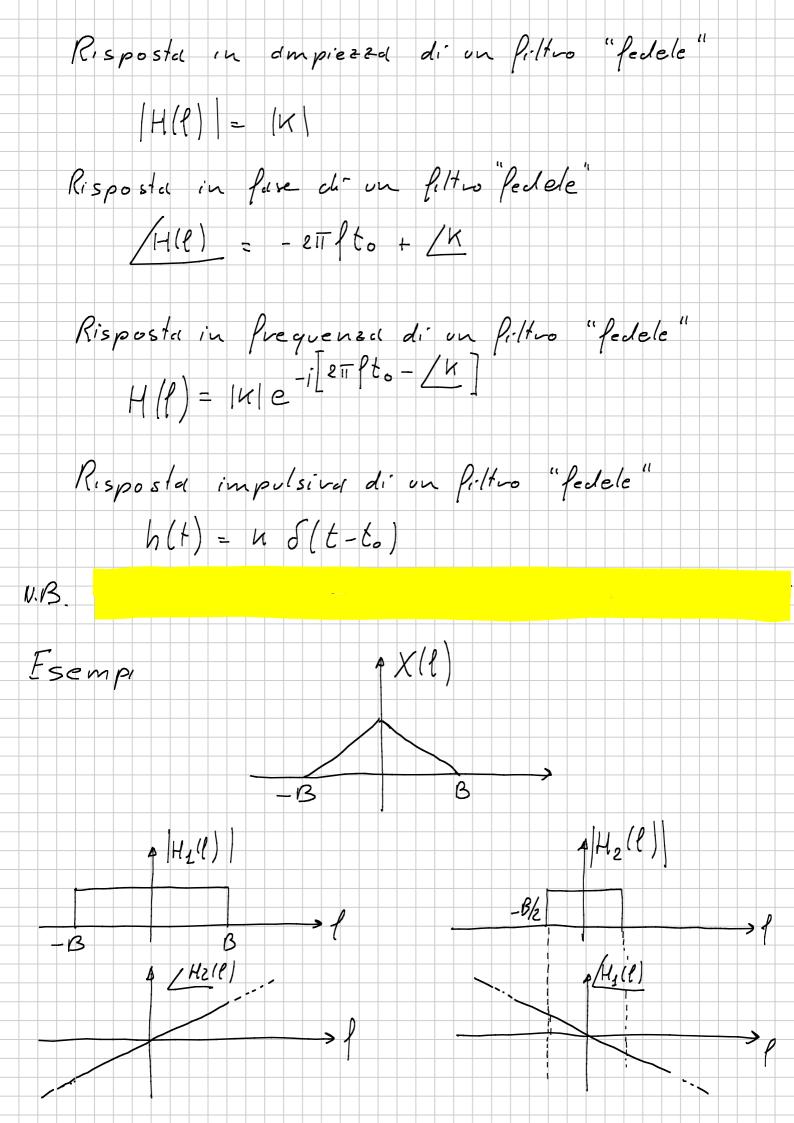


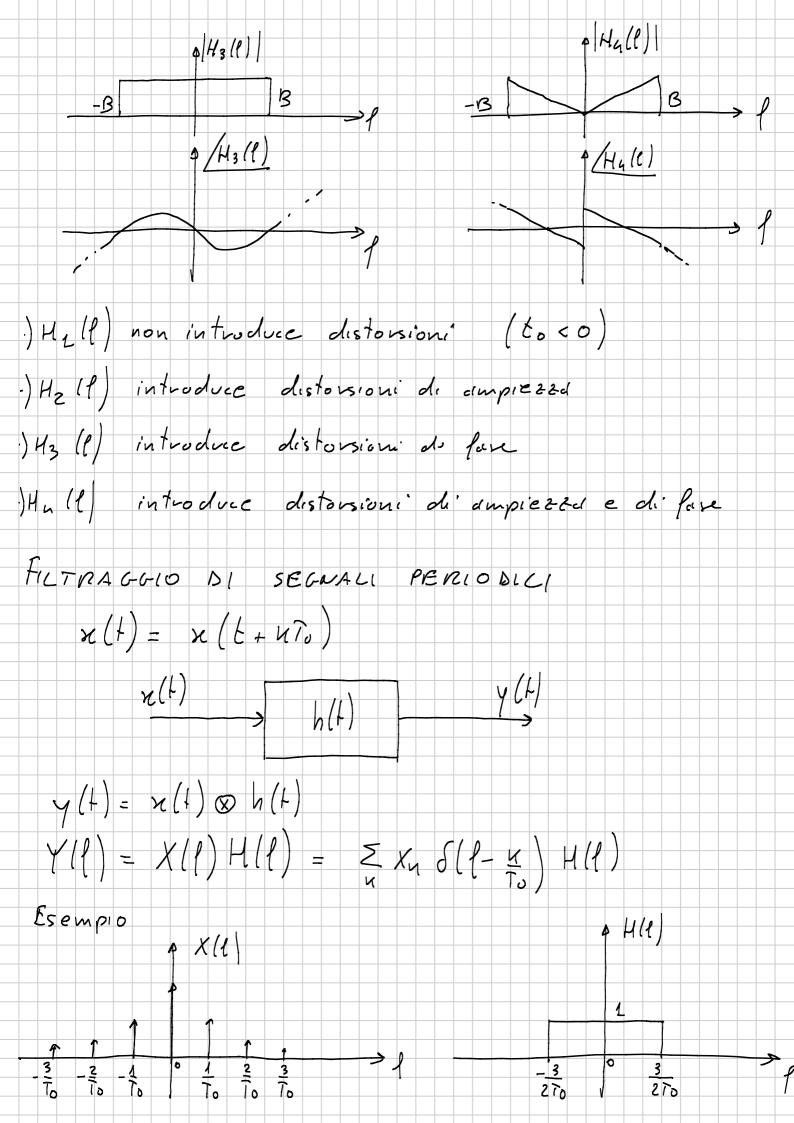


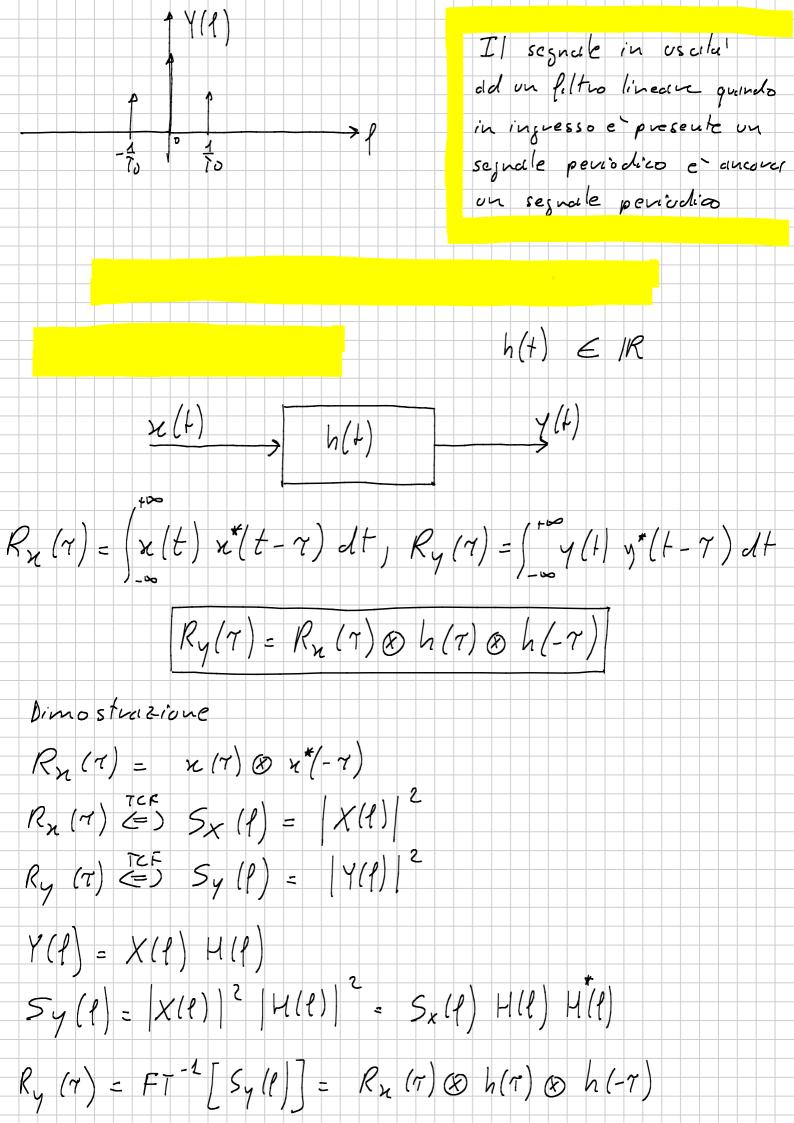












$$R_{x}(t) = x(t + \kappa T_{o})$$

$$R_{x}(t) = \frac{1}{T_{o}} \begin{cases} \frac{7}{2} \times (t) \times (t - 7) dt \\ \frac{7}{2} \times (7) = \frac{1}{T_{o}} \end{cases}$$

$$R_{y}(7) = \frac{1}{T_{o}} \begin{cases} \frac{7}{2} \times (t) \times (t - 7) dt \\ \frac{7}{2} \times (t) \times (t - 7) dt \end{cases}$$

$$R_{\gamma}(\tau) = R_{\gamma}(\tau) \otimes h(\tau) \otimes h(-\tau)$$

Dimostrazione

$$S_{y}(\ell) = |X(\ell)|^{2} |H(\ell)|^{2} = \sum_{k} |X_{k}|^{2} \delta(\ell - \frac{k}{10}) |$$

$$R_{\gamma}(\ell) = F_{1}^{-1} \left[ S_{\gamma}(\ell) \right] = R_{n}(\tau) \otimes h(\tau) \otimes h(-\tau)$$

$$R_{n}(\tau) = \lim_{T\to\infty} \frac{1}{T} \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} x(t) x(t-\tau) dt$$

$$S_{x}(\ell) = \lim_{T\to\infty} \frac{1}{T} \left[ X_{T}(\ell) \right]^{2}, \quad X_{T}(\ell) = FT \left[ x_{T}(\ell) \right]$$

$$x_{T}(\ell) = x(\ell) \operatorname{vect}(\frac{t}{T})$$

$$R_{\gamma}(\tau) = R_{\gamma}(\tau) \otimes h(\tau) \otimes h(-\tau)$$