

# Student Name MARKING KEY

#### Mathematics Applications U3&4 2日 えつら Eastern Goldfields College

Test 3 - Calculator Free Section

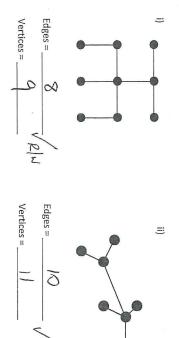
Question 1 [7 marks: 2, 1, 2, 2]

Working Time: 30 minutes

Total Marks: 31 marks

A tree graph is a planar graph with no cycles. It is an undirected graph in which any two vertices are connected by exactly one path. The following questions all refer to tree graphs.

a) For the following trees state the number of vertices and the number of edges.



<u>b</u> Draw a tree with 4 vertices and 3 edges.



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c) Is it possible to draw a tree with 4 vertices and 5 edges? Explain your answer.

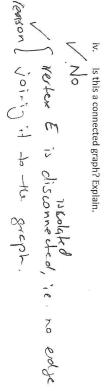
reason / a cycle will be formed. No cycle? a) Use the tree in part a) i) above and Euler's formula to, explain why tree graphs are all planar. 19+1-8-2. 2 = 2 = ). treis cre plenar + f=1 - each edge is a bridge only I regus 41 Heter

#### Question 2 [8 marks: 5, 1, 2]

- a) Consider the graph on the right.
- Which vertex is adjacent to A? B
- The loop in the graph connects which vertex to itself?

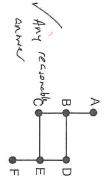






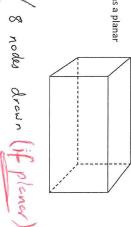
b) Draw a sub-graph of the graph on the right.





c) Represent the following three-dimensional prism as a planar graph.





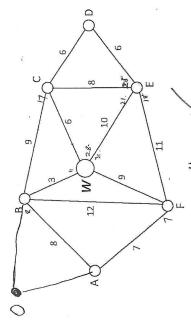
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### Question 3 [10 marks: 1, 2, 3, 4]

The graph on the right shows the location of a warehouse, W. This warehouse supplies timber to six factories A, B, C, D, E and F. The number along the edges indicates the length (in kilometres) of the connecting roads.



- a) What is the degree of vertex W?
- b) A delivery van is at vertex A. It must make a delivery to vertex E before returning to the warehouse. Determine the minimum distance travelled on this journey,

- c) A salesman wants to leave the warehouse and visit every factory once before returning to the
  - i. What is the 'mathematical term used to describe the route he is going to take? Hamiltonian only i. What
- e eyele. V coped pot Replace pot (open). 4-F-A-8-6-0-6-w Vstert tend on m N-18-A-F-E-D-C-W. ii. Define a route that he could take.
  - d) The company wishes to lease an office which is adjacent to two of the factories.
- Draw one possible location for the company on the graph, including one road to each of the adjacent factories.  $\sqrt{\Delta \omega_{\gamma}} = v \approx 170$ What impact will these two extra roads have on the degree of the vertices?

The owner wishes to check for any competitors along the route. Will the owner have to complete an open or closed trail if she wants to travel along every edge only once?

#### Question 4 [6 marks: 2, 2, 2]

In a netball competition there are four teams participating.

a) If every team needs to play each other exactly once, how many games are required for the

b) Draw the graph showing how each team can play each other, what type of graph would this be?



c) If two more teams join the competition how many more games are required to be played in order

15-6= 9 more games Total 15 games for each team to still play each other exactly once?



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Test 3 - Calculator Assumed Section

Total Marks: 20 marks

Question 1 [6 marks: 3, 2, 1]
Consider the following undirected graph.



a) Construct the adjacency matrix, M, for the above digraph.

b) Calculate  $\mathcal{M}^2$  and explain the significance of the zero elements in this matrix.

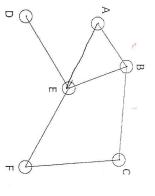
c) Identify a practical situation that could be represented by this network.

7 X. Bus route sould not withheredges? Any reasonable animal

#### Question 2 [3 marks: 1, 2]

A treasure hunt is being organised and a graph showing where prizes are hidden is shown right.

a) Show a semi-Hamiltonian path which you could walk in order to collect all the prizes.

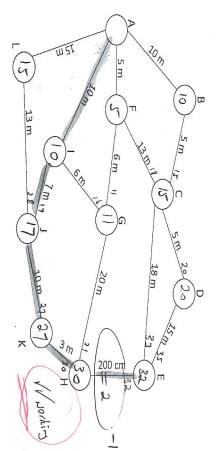


b) Is it possible to create an Eulerian circuit foothe treasure hunt by adding exactly one edge? If so, what is the pathway, if not, explain why?

## Question 3 [11 marks – 4, 1, 6]

The following network shows some of the corridors running through a large hospital. Most of the thoroughfare through this hospital is from A to E.

corridors. The cost of upgrading is \$95/metre. their budget they decided to upgrade the shortest path from A to E as these would be the most used The hospital receives some funding to upgrade some of the finishings in the corridors. In order to maximise



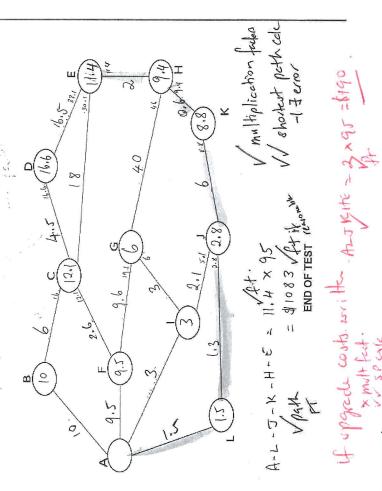
a) What is the shortest distance from A to E and what is this pathway?

b) What is the cost of upgrading the shortest path from A to E?

Upon further discussions it appears that not all the corridors require the same amount of work to upgrade and therefore the costs of upgrading each corridor are not equal. The following table shows the multiplication factor in the costs of upgrading each corridor relative to the lengths.

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c) Taking into account the multiplication factors, which path from A to E should the hospital upgrade in order to minimise costs? Clearly state this path and the total cost of upgrading it. Use the blank network below to assist with your answer.



ALT KHE = 2,0 × 95 = \$190.

