

Final mark

Year 11 Specialist Mathematics



/50

Semester 1, March 2021

Test 1: Combinatorics and Introduction to Proofs

Weighting: 6%

[Australian Curriculum Reference Numbers: 1.3.1-1.3.5, 1.1.1-1.1.9, 2.1.5]

Total Time: 50min Total Marks =	50			
Student Name:				
Teacher:				
TO BE PROVIDED BY THE STUDENT				
Standard Items: Pens, pencils, eraser, sharpener, correction tape/fluid, highlighters, rule	∍r.			
Special Items:				
 Drawing instruments, templates A maximum of three CAS calculators satisfying the conditions set by the Curriculum Council for use in the Calculator Allowed section only 				
TO BE PROVIDED TO THE STUDENT				
A formula sheet will be provided				
INSTRUCTIONS TO STUDENTS:				
You are required to attempt ALL questions.				
Write answers in the spaces provided beneath each question.				
Marks are shown with the questions.				
Show all working clearly, in sufficient detail to allow your answers to be checked readily and for marks to be answered for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks.				
It is recommended that students do not use a pencil, except in diagrams				
Part A – Calculator - Free (30 minutes)	/30			
Part B – Calculator Assumed (20 minutes)	/20			

4	C	-:-1			ment:
1.	l An	CIMAR	TNA	CTATA	mont

"All squares have two equal pairs of parallel sides"

- a) State the inverse of the statement.
- b) State the converse of the statement.
- c) State the contrapositive of the original statement.

d) Is the original statement necessary and sufficient? Justify your answer.

[1,1,1,2 = 5 marks]

- 2. A pencil case contains a variety of red, blue, black, and green pens.
 - a) How many pens do you need to have to be certain of having six pens of the same colour?

What is the smallest number of pens you can have in the pencil case to ensure you have at least 4 red pens, or 1 green pen, or 2 blue pens, or 5 black pens?

- 3.
- a) Prove the following by proving its contrapositive. Note: (same parity means both odd or both even)

If x and y are two integers for which x + y is even, then x and y have the same parity.

b) Prove the following statement by proving its contrapositive:

$$\forall p \in \mathbb{Z}, p^2 odd \Rightarrow p odd$$

4.	4. Evaluate the following:	Part A: Calculator-Free Section (30 minutes
	a) 9P_4	
	b) ¹² C ₉	
		[1,2 = 3 marks
5.	5. Determine the value of $^{n-1}P_2$ if it is known t	hat $7 \times {}^{n}P_{2} = 6 \times {}^{n+1}P_{2}$ for $n > 0$.
		[5 marks
5.	5. To prove that $\sqrt{3}$ is irrational, we first assume contradiction. Use mathematical notation to	

*** End of Calculator - Free Section ***

[3 marks]



Year 11 Specialist Mathematics



Semester 1, March 2021

Part B: Calculator Assumed Section

Time Allowed: 20 minutes

	Marks =	20
Student Name:		
Teacher:		

INSTRUCTIONS TO STUDENTS:

- You are allowed a CAS calculator
- You are not allowed any notes
- A formula sheet will be provided

You are required to attempt ALL questions.

Write answers in the spaces provided beneath each question.

Marks are shown with the questions.

Show all working clearly, in sufficient detail to allow your answers to be checked readily and for marks to be answered for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks.

It is recommended that students do not use a pencil, except in diagrams

Melville SHS Page | 5

- 1. A large circular table at a restaurant has 9 people from an office seated at random around it.
 - a) What is the probability of Mark being seated between David and Peter?

b) Fiona and David do not like each other very much and do not wish to sit next to each other. How many seating arrangements are possible provided Mark is seated between David and Peter, *and* Fiona and David do not sit together?

- 2.
- a) How many "words" can be formed using the letters from the word ENTERPRISES if you must use every letter?

b) How many 4-letter "words" can be formed using the letters from the word ENTERPRISES?

[2,7 = 9 marks]

Melville SHS Page | 7

3. There are 255 Year 11 students at Melville SHS. Of these students, 68 study Physics and 44 study Computer Science. 29 students study Chemistry and Physics, 14 study Physics and Computer Science and 19 study Computer Science and Chemistry. 9 students study all 3 subjects and 126 students study none of these subjects.

Use the inclusion-exclusion principle to determine the probability that a Year 11 student chosen at random studies chemistry but not Physics or Computer Science.

[5 marks]

Melville SHS Page | 8