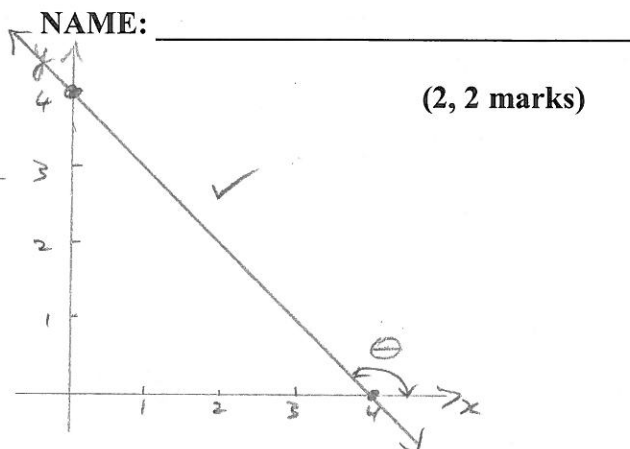


QUESTION 1

For the line  $3x + 3y = 12$

(a) Sketch the line

$x$	0	4
$y$	4	0



(2, 2 marks)

(b) Mark the angle of inclination the line makes with the  $x$  axis. Determine this angle. Justify your answer.

$$\text{gradient of line} = -\frac{4}{4} = -1$$

$$\tan \theta = -1$$

$$\therefore \theta = 180 - 45$$

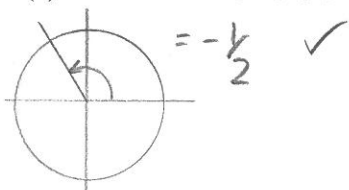
$$\theta = 135^\circ \checkmark \checkmark$$

QUESTION 2

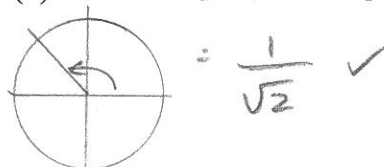
(1, 1 marks)

Express the following in terms of angles between  $0^\circ$  and  $90^\circ$  and state their exact value:

(a)  $\cos 120^\circ = -\cos 60^\circ$



(b)  $\sin 135^\circ = \sin 45^\circ$



QUESTION 3

(4 marks)

Find the exact value of  $\frac{\cos 60^\circ \cos 45^\circ}{\cos 30^\circ}$  expressed with a rational denominator.

$$\begin{aligned} &= \frac{\frac{1}{2} \times \frac{1}{\sqrt{2}}}{\frac{\sqrt{3}}{2}} = \frac{1}{2\sqrt{2}} \times \frac{2}{\sqrt{3}} \\ &= \frac{1}{\sqrt{2}} \times \frac{\sqrt{6}}{\sqrt{6}} \\ &= \frac{\sqrt{6}}{6} \end{aligned}$$

# QUESTION 4

(2, 3 marks)

(a) Shown below are four rules and their corresponding graphs. For each, state whether or not it satisfies the conditions to be a function.

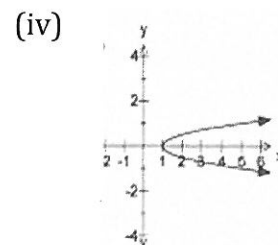
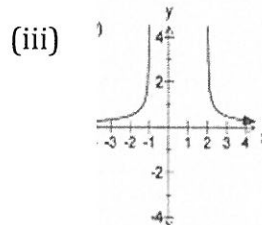
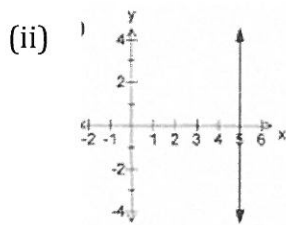
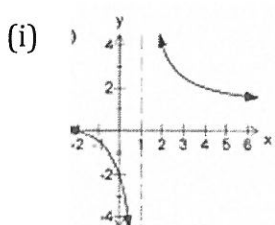
(i)  $y = \frac{3}{x-1} + 1$  Yes/No

(ii)  $x = 5$  Yes/No

✓✓

(iii)  $\frac{1}{\sqrt{x^2 - x - 2}}$  Yes/No

(iv)  $x - 4y^2 = 1$  Yes/No



(b) For each function, state its domain and range.

RULE	DOMAIN	RANGE
$y = \frac{3}{x-1} + 1$	$x \in \mathbb{R} \quad x \neq 1$	$y \in \mathbb{R} \quad y \neq 1 \quad \checkmark$
$x = 5$		
$\frac{1}{\sqrt{x^2 - x - 2}}$	$x \in \mathbb{R} \quad x < -1 \quad x > 2 \quad \checkmark$	$y \in \mathbb{R} \quad y > 0 \quad \checkmark$
$x - 4y^2 = 1$		

**QUESTION 5****(3 marks)**Simplify and express with a rational denominator:  $\frac{\sqrt{7}-6}{\sqrt{7}+6}$ 

$$\begin{aligned}
 \frac{\sqrt{7}-6}{\sqrt{7}+6} \times \frac{\sqrt{7}-6}{\sqrt{7}-6} &= \frac{(\sqrt{7}-6)(\sqrt{7}-6)}{(\sqrt{7}+6)(\sqrt{7}-6)} \\
 &= \frac{7-12\sqrt{7}+36}{7-36} \\
 &= \frac{43-12\sqrt{7}}{-29}
 \end{aligned}$$

**QUESTION 6****(2 marks)**Write  $255^\circ$  as an angle in radians as a simplified fraction in terms of  $\pi$ 

$$\begin{aligned}
 \pi \text{ radians} &= 180^\circ \\
 \frac{\pi}{180} &= 1^\circ \\
 \frac{\pi}{180} \times 255 \text{ radians} &= 255^\circ \\
 \frac{17\pi}{12} \text{ radians} &= 255^\circ
 \end{aligned}$$

**QUESTION 7****(1 mark)**A function is defined as  $f(x) = x^2 + 2x - 8$ . Write an expanded expression for  $f(2x)$ 

$$\begin{aligned}
 f(2x) &= (2x)^2 + 2(2x) - 8 \\
 &= 4x^2 + 4x - 8
 \end{aligned}$$

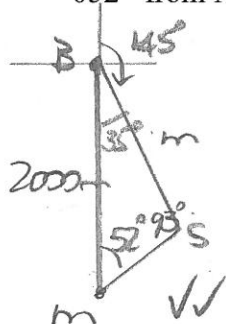
TIME ALLOWED : 40 MINUTES

TOTAL MARKS : 39

NAME: \_\_\_\_\_

QUESTION 8 (5 marks)

Three towns Brooks River (B), Fryman Mill (M) and Swann Place (S) are to cultivate the triangular piece of land that they immediately surround. M is 2000m due South of B. S is on a bearing of  $145^\circ$  from B and  $052^\circ$  from M. Calculate the area of this piece of land.



$$\frac{m}{\sin 52} = \frac{2000}{\sin 93}$$

$$m = 1578.18 \text{ m}$$

$$\text{Area}(\Delta) = \frac{1}{2} \times 2000 \times 1578.18 \times \sin 35^\circ$$

$$= 905209.36$$

$$= \underline{905209 \text{ m}^2} \quad \checkmark \checkmark$$

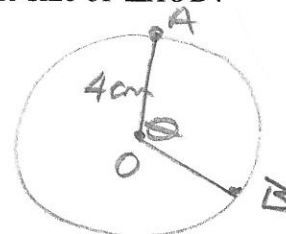
QUESTION 9 (3,1 marks)

The area of a sector AOB, in a circle centre O and radius 4 cm is  $\frac{16\pi}{3} \text{ cm}^2$ . Find the size of  $\angle AOB$ :

a. in radians in terms of  $\pi$ .

$$\text{Area}(\text{Sector}) = \frac{1}{2} r^2 \theta$$

$$\frac{16\pi}{3} = \frac{1}{2} \times 4^2 \times \theta \quad \angle AOB = \frac{2\pi}{3} \text{ radians} \quad \checkmark$$



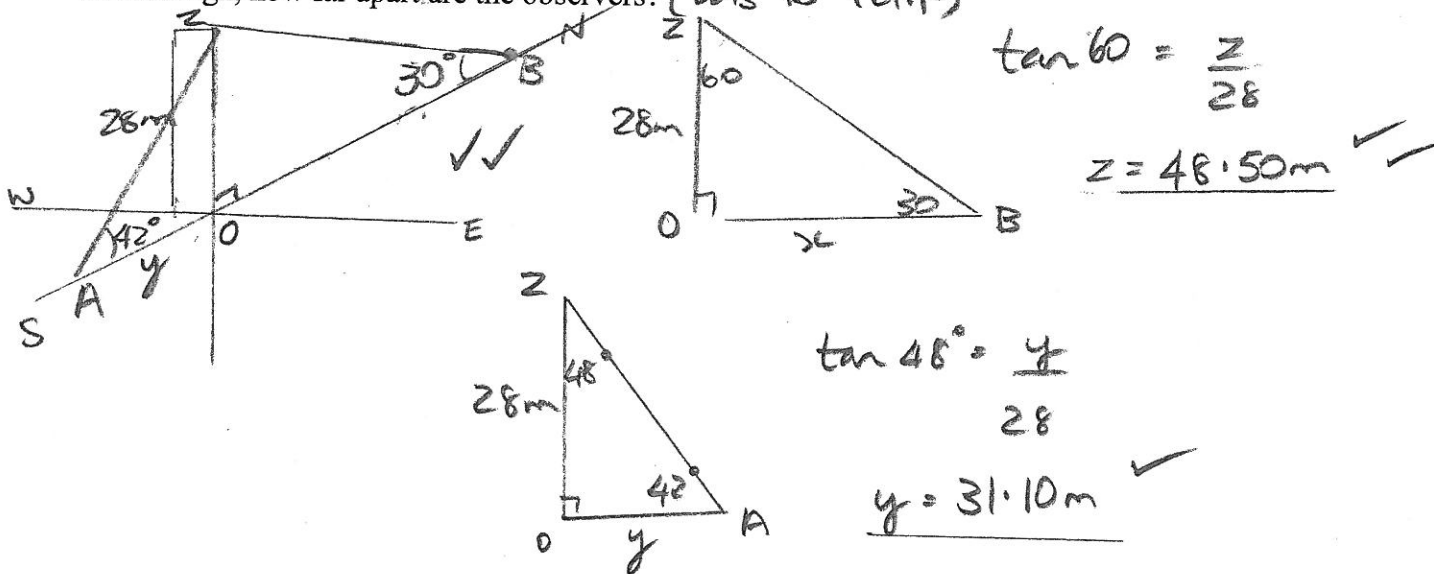
b. in degrees

$$\pi \text{ radians} = 180^\circ$$

$$\frac{2\pi}{3} \text{ rad} = 120^\circ \quad \checkmark$$

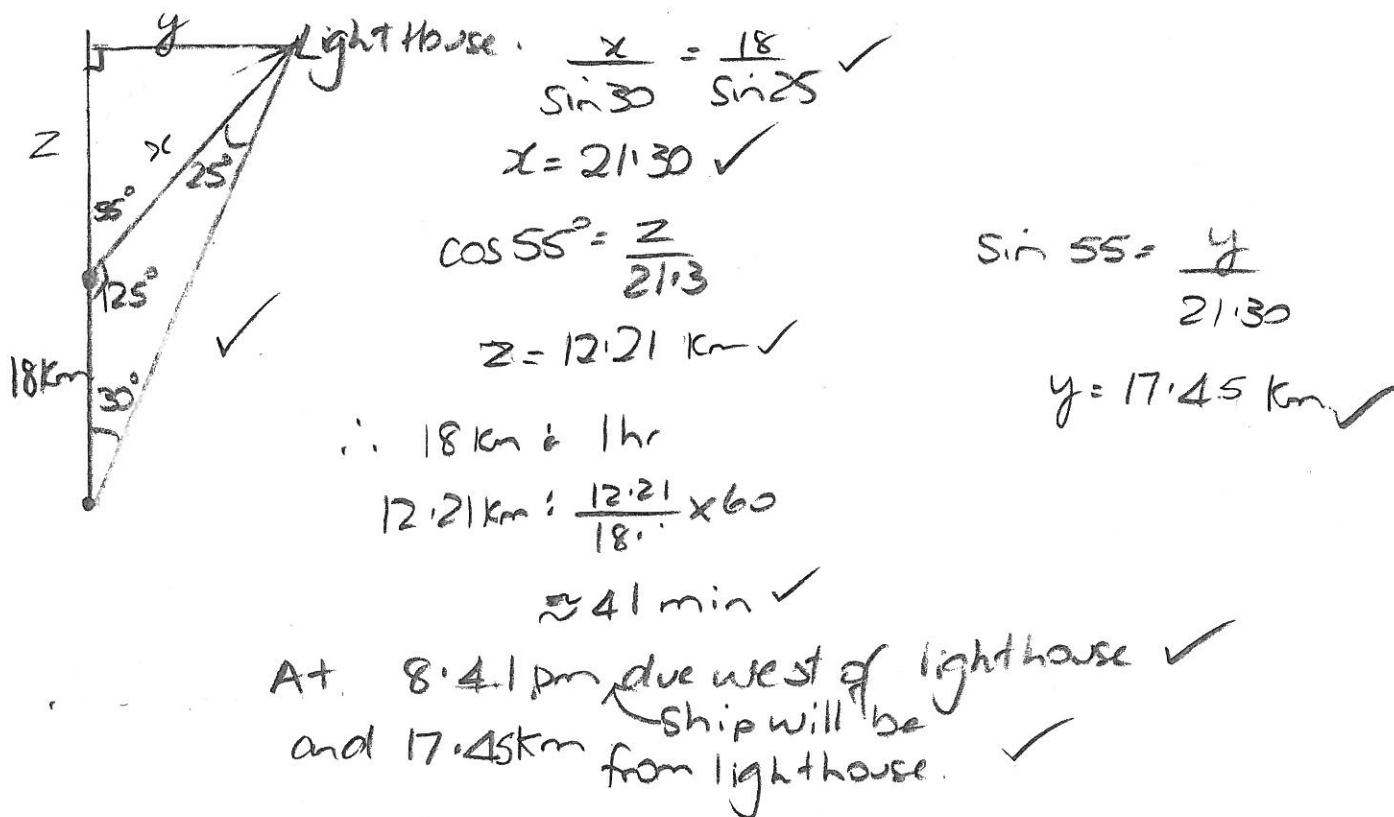
### QUESTION 10 (6 marks)

Two observers are on opposite sides of a tower, and collinear with its base. The first finds the angle of elevation of the top of the tower to be  $42^\circ$ , the second finds it to be  $30^\circ$ . If the tower is 28m high, how far apart are the observers? (ans to 1 d.p.)



### QUESTION 11 (8 marks)

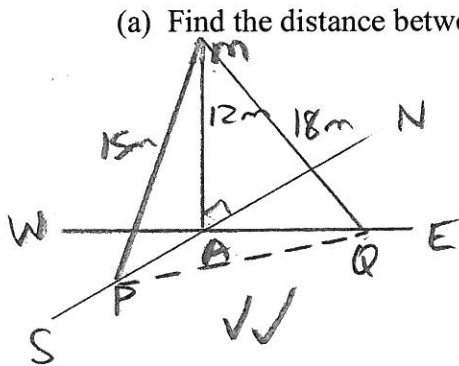
At 7pm a ship heading North and travelling at 18 km/hr observes a lighthouse on a bearing of  $030^\circ$ . At 8pm the lighthouse is observed on a bearing of  $055^\circ$ . At what time will the ship be due West of the lighthouse – and how close will it be at this time?



### QUESTION 12 (5, 2 marks)

A wireless mast is supported by two wires MP and MQ, each attached to it at the point M, 12m from the base A of the mast. Q, P and A are all on level ground, Q being due East and P due South of the mast. If MP and MQ are respectively 15m and 18m long:

(a) Find the distance between P and Q



$$\text{In } \triangle MAP, AP = \sqrt{15^2 - 12^2} = 9\text{m} \checkmark$$

$$\text{In } \triangle MAQ, AQ = \sqrt{18^2 - 12^2} = 13.4\text{m} \checkmark$$

$$\text{In } \triangle PAQ, PQ = \sqrt{9^2 + 13.4^2} = 16.2\text{m} \checkmark$$

(b) Find the angle QMP between the wires

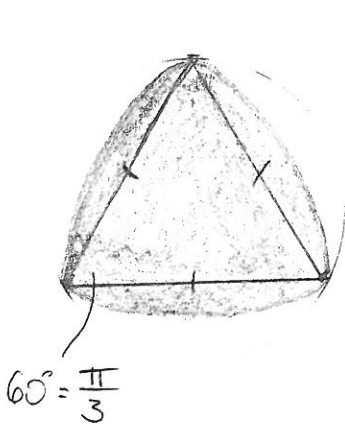
$$\text{In } \triangle MQP, 261 = 15^2 + 18^2 - 2 \times 15 \times 18 \times \cos \theta$$

$$\cos \theta = 0.53$$

$$\angle \theta = 57.8^\circ \checkmark \checkmark$$

### QUESTION 13 (6 marks)

An equilateral triangle of side length 9 cm has circles with centres at each of the vertices drawn to pass through the other two vertices. Find the area common to the three circles.



$$\theta = \frac{\pi}{3}$$

$$\text{Area (sector)} = \frac{1}{2} r^2 \theta$$

$$= \frac{1}{2} \times 9^2 \times \frac{\pi}{3}$$

$$= 42.4\text{cm}^2 \checkmark$$

$$\text{Area (segment)} = \frac{1}{2} r^2 (\theta - \sin \theta)$$

$$= \frac{1}{2} \times 9^2 \left( \frac{\pi}{3} - \sin \frac{\pi}{3} \right)$$

$$= 7.34\text{cm}^2 \checkmark$$

$$\therefore \text{Total Area} = 42.4 + 2 \times 7.34 \checkmark \checkmark$$

$$= 57.1\text{cm}^2 \checkmark$$

**QUESTION 14 (3 marks)**

The owner of a shop that sells computers calculates that his total weekly profit is given by the rule:

$$\text{Total profit in dollars} = mx - c,$$

where \$m\$ is the profit per computer sold, \$x\$ is the number of computers sold in the week and \$c\$ is the fixed weekly cost of running the shop.

If he sells ten computers in a week his total profit is \$360.

If he only sells five computers in the week he makes a loss of \$190.

(a) Calculate \$m\$ and \$c\$.

$$(10, 360) \quad (5, -190)$$

$$m = \frac{360 - (-190)}{10 - 5}$$

$$\text{Profit} = 110x - c$$

$$\text{sub } (10, 360)$$

$$m = \frac{550}{5}$$

$$360 = 110(10) - c$$

$$360 = 1100 - c$$

$$\underline{m = 110}$$

$$c = 1100 - 360$$

$$\underline{c = 740}$$

✓✓

↓↓

(b) What is the least number of computers he can sell and still make a profit?

$$P = 110x - 740$$

$$740 = 110x$$

$$\frac{740}{110} = x$$

$$6.73 = x$$

$$\therefore \underline{x = 7 \text{ computers}} \quad \checkmark$$