# **WILLETTON SENIOR HIGH SCHOOL**



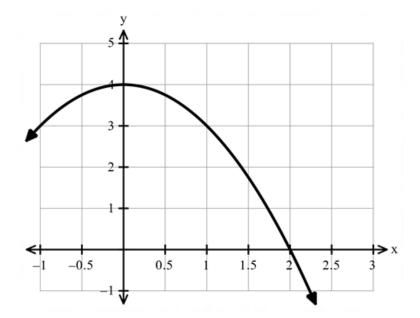
# YEAR 12 MATHEMATICS METHODS TEST 2 2023

**Section 1: Calculator Free** 

Student Name:							
Circle your teach	ner's name.						
Miss Ahern		Mr Galbraith					
Mrs Gatland		Mrs Sun					
Mark:	/ 28						
Time:	25 mins						
For section 1 of this test:							
No notes.							
No calculators.							
Formula sheet as provided.							
Show working.							

## **QUESTION ONE (5 MARKS)**

A graph of y = f(x) with a table of values of the function for given values of x, is shown below.



2	X	0	0.5	1	1.5	2
	У	4	15 4	3	$\frac{7}{4}$	0

a) Find the approximate area under the curve y = f(x) between x = 0 and x = 2 using the areas of four <u>circumscribed</u> rectangles of equal width.

[2]

b) Find the approximate area under the curve y = f(x) between x = 0 and x = 2 using the areas of four inscribed rectangles of equal width.

[2]

c) Using your answers from parts 'a' and 'b', find an improved estimate for the area under the curve y = f(x).

[1]

## **QUESTION TWO (5 MARKS)**

Determine the following:

a) 
$$\frac{d}{dx}[x^2e^{\sin(x)}]$$

[2]

b) 
$$\int (3e^{2x} - \cos 2x) dx$$

[2]

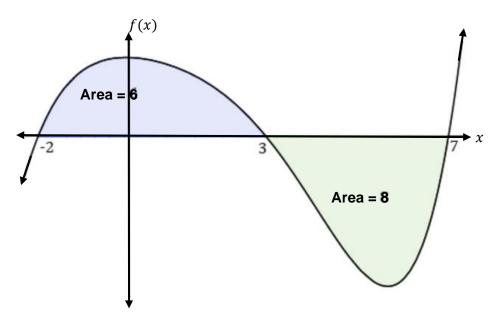
c) 
$$\frac{d}{dx} \left( \int_{\frac{\pi}{2}}^{x} \sin(t) \, dt \right)$$

[1]

## **QUESTION THREE (5 MARKS)**

The function f(x) is shown below.

The areas enclosed between the graph, the x-axis and the lines x = -2 and x = 7 are marked in the appropriate regions.



Determine:

a) 
$$\int_{-2}^{7} f(x) dx$$
. [1]

b) the area enclosed between the graph of f(x) and the x axis. [1]

c) 
$$\int_{3}^{7} (-f(x))dx$$
 [1]

d) 
$$\int_{3}^{-2} f(x)dx$$
 [1]

e) 
$$\int_{-2}^{7} |f(x)| dx$$
 [1]

QUESTION FOUR (4 MARKS)
Find the area between the graph of $y = \sin(x)$ and the x axis between $x = 0$ and $x = \frac{4\pi}{3}$ .

## **QUESTION FIVE (3 MARKS)**

A particle is moving in a straight line with acceleration a m/s<sup>2</sup> at time t seconds with equation  $a(t) = 40e^{0.4t}$ Find the total change in velocity between 0 and 5 seconds as an exact value.

## **QUESTION SIX (6 MARKS)**

a) Find  $\frac{dy}{dx}$  given that  $y = 3x \sin 2x$  [2]

b) Use your answer from part (a) to determine  $\int x \cos 2x \ dx$ . [4]

## **WILLETTON SENIOR HIGH SCHOOL**



# YEAR 12 MATHEMATICS METHODS TEST 2 2023

**Section 2: Calculator Allowed** 

Student Name:							
Circle your teacher's name.							
Miss Ahern		Mr Galbraith					
Mrs Gatla	and	Mrs Sun					
Mark:	/ 25						
Time:	25 mins						
For this test:							
Scientific calculators and Classpads are allowed							

One A4 single side of notes is allowed

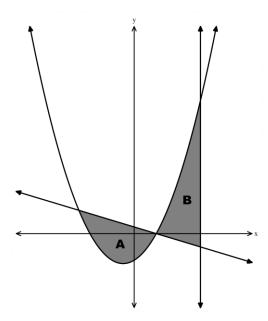
Show any working in the spaces provided

## **QUESTION SEVEN (5 MARKS)**

The graph below shows two shaded areas.

**A** is the area bounded by the curve  $y = 0.5x^2 + x - 4$  and the line y = -0.5x + 1.

**B** is the area bounded between the curve  $y = 0.5x^2 + x - 4$ , the line y = -0.5x + 1 and the line x = p.



a) Given that the area of 
$${\bf B}$$
 is  $\frac{116}{3}$  units<sup>2</sup>, determine the value of  $p$ .

[2]

[3]

#### **QUESTION EIGHT (7 MARKS)**

An initiall	ly full water tank is emptied in 125 minutes at a rate of $V'(t) = 0.02t^2 - 2.1t - 50$ litres per minutes	ute
a) D	Determine the flow rate of the water leaving the tank at $t=15$ mins.	[2]
b) D	Determine the capacity of the water tank to the nearest litre.	[2]
•	Determine the time, to the nearest 0.1 minute, that it will take to reduce the volume of water in the ank to a fifth of its capacity.	ne [3]

## **QUESTION NINE (4 MARKS)**

The number of bacteria (N) in a certain culture at time (t), weeks is modelled by the function  $N = N_0 e^{kt}$ , given N = 101 when t = 2 and N = 203 when t = 4.

Calculate the rate at which the bacteria is increasing when the number of bacteria in the culture reaches 500.

#### **QUESTION TEN (4 MARKS)**

When building a house, an optional feature is to have a heating system installed within the concrete slab. This system comprises of tubing installed within the concrete slab and water runs though the tubing to heat the concrete during winter.

The number of litres/ minute of water flowing through the tubing over t minutes can be modelled by the rule;  $\frac{dV}{dt} = 2[\cos\left(\frac{\pi t}{3}\right) + \sin\left(\frac{\pi t}{9}\right) + 3]$ . Determine the amount of water that runs through the pipes during the time period for one cycle.

[Hint: Consider the graph of the function to determine the time period for one cycle first]

## **QUESTION ELEVEN (5 MARKS)**

Given that  $F(x) = \int_1^x f(t) dt$ , with F(2) = 11 and F''(x) = 6x, find f(t)