

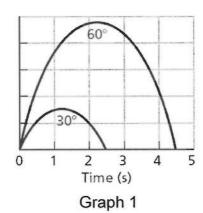
12 ATAR Physics

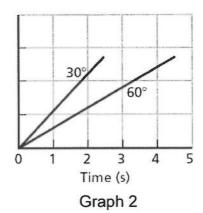
Projectile and Circular Motion Test 2016

Name: _	MARKING	KEY	Score:	/ 56
	ons: e negligible air resis er for real situations			asks you to
1. Two b 25 ms	paseballs in the figure s ⁻¹ .	below were hit with	the same initia	Il speed of
	30	$A = x_{A} = x_{B}$	J J J J J J J J J J J J J J	4
(a) F (i	•	nine the magnitude conent of the initial $60^\circ = 12$	velocity	[1]
(ii		nent of the initial velocity $60^{\circ} = 2$		[1]
(b) F	or trajectory B, determ) horizontal accele	eration.	of the	[1]
(ii		ms -Z		[1]

Question 1 (continued)

(c) For both trajectories, which graph shows





(i) the horizontal distance travelled versus time.

[1]

Graph 2

(ii) the vertical distance travelled versus time.

[1]

Graph 1

(iii) **using equations of motion**, calculate the time of flight of trajectory A (projected at 60°)

[2]

For A, end of flight $s_{Y} = 0$ $s = ut + 5at^{2}$ $0 = 21.7t - 4.9t^{2}$ 0 = t(21.7 - 4.9t)t = 0 or $t_{A} = 4.42s$

1 as the fine of flight ta = 4.42 s

(iv) **using equations of motion**, calculate the maximum height reached in trajectory A (projected at 60°) [2]

/

Af max height

$$v^2 = u^2 + 2as$$

 $0 = 21.7^2 + 2(-9.8)8$
 $8 = 24.025m$

- 2. An athlete whirls a 7 kg hammer of radius 1.8 m from the axis of rotation in a horizontal circle as shown right.
 - (a) If the hammer makes one revolution in 1.0 s,
 - (i) calculate the centripetal acceleration of the hammer? [3]

$$a = \frac{V^2}{r}$$

$$= \left(\frac{2\pi r}{t}\right)^2 \div f$$

$$= \frac{4\pi^2 f^2}{t^2 r}$$



$$= \frac{4\pi^2 r}{t^2} = \frac{4\pi^2 (1.8)}{1^2} = 71 \, \text{ms}^{-2}$$

(ii) state the direction of the centripetal acceleration? [1]

(b) Determine the tension in the chain?

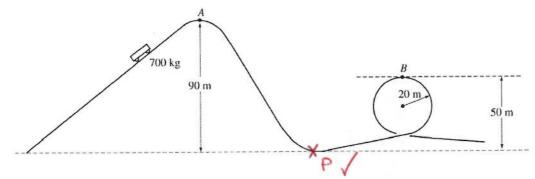
$$T = F_{c}$$

$$= m\frac{V^{2}}{\Gamma}$$

$$= 7(71)$$

$$= 497$$

3.



A roller coaster at an amusement park lifts a car of mass M kg to point A at a height of 90 m above the lowest point on the track, as shown above.

The car starts from rest at point A, rolls with negligible friction down the incline and follows the track around a loop of radius 20m.

Point B, the highest point on the loop, is at a height of 50 m above the lowest point on the track.

(a)(i) Indicate on the figure the point P at which the maximum speed of the car is attained. [1]

Shown

(ii) Calculate the value of this maximum speed.

[3]

Using conservation of energy
$$TE_{A} = TE_{P}$$

$$PE_{A} + KE_{A} = PE_{B} + KE_{B}$$

$$mgh_{A} + 0 = 0 + \frac{1}{2}mV_{B}^{2}$$

$$9.8(90) = \frac{1}{2}V_{B}^{2}$$

$$V_{B}^{2} = 2(9.8)(90)$$

$$V_{B} = 1764$$

$$V_{B} = 42 \text{ ms}^{-1}$$

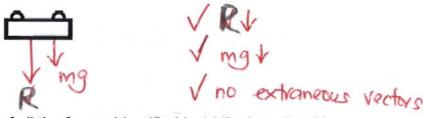
equation //
of motion
anything
falling from
A to P
will achieve
same speed
as something

Question (continued)

(b) Calculate the speed of the car at point B.

$$TE_A = TE_B$$
 $M(9.8)(90) = M(9.8)50 + \frac{1}{2}MV_B^2$
 $V_B = 28 \text{ ms}^{-1}$

(c)(i) On the figure of the car below, draw and label vectors to represent the forces acting on the car when it is upside down at point B. [3]



[3]

(ii) Calculate the magnitude of all the forces identified in (c)(i) given that M is 700 kg

$$W = mg = 700 (9.8)$$

$$= 6860 N$$

$$F_{net} = R + mg$$

$$F_{c} = R + 6860$$

$$\frac{mV^{2}}{c} = R + 6860$$

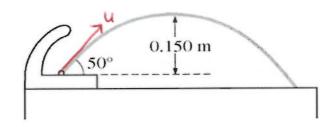
$$\frac{700(28)^{2}}{20} = R + 6860$$

(d) Assume that friction is not negligible. How could the loop be modified to maintain the same speed at the top of the loop as found in (b)?

Lower the height of B

Work done by friction will reduce the total mechanical energy available at B

so KEB remains some 5, PEB must be reduced



A drinking fountain projects water at an initial angle of 50° above the horizontal. The water reaches a maximum height of 0.150 m above the point of exit.

(a) Calculate the speed at which the water leaves the fountain.

[4]

Vertical Motion (Take 1 as +ve)

$$u_{\gamma} = u \sin 50^{\circ}$$

 $a_{\gamma} = -9.8$

At maximum height
$$V_Y = 0$$

 $V_Y^2 = u_Y^2 + 2qs_Y$
 $0 = (usin50)^2 - 2(9.8)0.15$

$$2.94 = (usin 50)^2$$

$$u = \frac{1.71}{\sin 50^{\circ}} = 2.24 \text{ ms}^{-1} /$$

(b) The radius of the fountain's exit hole is 4.00 x 10⁻³ m. Calculate the rate of volume flow of the water.

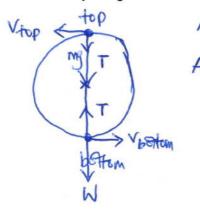
Rate of Volume flow = Area × distance
time
$$= \pi r^2 V$$

$$= \pi (4.15-3)^2 (5.21)$$

$$= \pi (4 \times 10^{-3})^{2} (2.24)$$

$$6 = 1.13 \times 10^{-4} \text{ m}^{3}/\text{s}$$

5. A ball on a light string moves in a vertical circle. Analyse and describe the motion of this system considering the effects of gravity and tension using free body diagrams. Is the system in uniform circular motion? Explain.

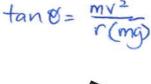


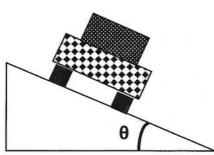
At top Fc = T+mg At bettom Fc = T-mg with mand r constant

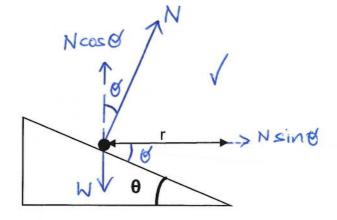


- Non uniform arcular motion / (as speed is not constant)
- 6. A car is travelling with speed v around a curve of radius r (shown left).
 - (a) Determine a formula for the angle θ at which a road should be banked

$$tan 8 = \frac{\sqrt{2}}{rq} \sqrt{$$







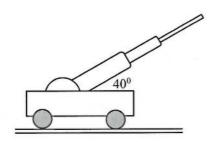
Free Body Diagram

(b) Calculate the angle for a road which has a curve of radius 50 m with a design speed of 50 km h⁻¹.

$$\theta = \tan^{-1} \left(\frac{v^2}{rg} \right)$$

$$= \tan^{-1} \left(\frac{13.89^2}{50 \times 9.8} \right) = 21.5^{\circ}$$
 $\sqrt{}$

7.



Big Bertha was the name of a huge cannon used by the Germans in the First World War to fire across the Channel to England. This gun was mounted on a train and could be moved to different positions. The shell's muzzle velocity was 750 kmh⁻¹.

[2]

a) What would be the maximum height that the shell reached above the ground? [2]

nd?

$$U_Y = 208.3 \sin 40^\circ = 133.9 \text{ ms}^{-1}$$

 $V^2 = u^2 + 2as$
 $0 = 133.9^2 - 19.6s$
 $S = 9.5 \text{ m}$

b) What is the range of the gun if the angle of elevation is 40°?

$$U_{H} = 208.3 \cos 40^{\circ}$$

$$= 160 \text{ ms}$$

$$= 160 (27.32)$$

$$= 4371.2 \text{ m} = 4.37 \times 10^{3} \text{ m}$$

$$= 27.32 \text{ s}$$

$$= 27.32 \text{ s}$$

c) What would be the gun's maximum range when its angle of elevation can be increased or decreased? [2]

vertically

$$S = ut + \frac{1}{2}at^2$$

 $0 = 147.3t - 4.942$
 $t = 30.055$

Honzowtally

$$s = ut = 147.3 \times 30.05$$

= 4.43×10^3 m

Question 7 (continued)

d) What would be the velocity and angle of the shell 5 seconds after firing? Assume angle of elevation is 40° [2]

$$V_{f} = 133.9 - 9.8 \times 5$$

= 84.9 ms⁻¹

$$V_R^2 = \sqrt{160^2 + 84.9^2}$$

= 181 ms

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