

# Baldivis Secondary College

WAEP Semester Two Examination, 2016

Question/Answer booklet

## MATHEMATICS METHODS UNITS 3 AND 4

Section One:  
Calculator-free

If required by your examination administrator, please  
place your student identification label in this box

Student number: In figures

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In words

\_\_\_\_\_

Your name

\_\_\_\_\_

### Time allowed for this section

Reading time before commencing work: five minutes

Working time for section: fifty minutes

### Materials required/recommended for this section

#### *To be provided by the supervisor*

This Question/Answer booklet

Formula sheet

#### *To be provided by the candidate*

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

### Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

## Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	7	7	50	52	35
Section Two: Calculator-assumed	13	13	100	97	65
<b>Total</b>					100

## Instructions to candidates

1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
4. Additional working space pages at the end of this Question/Answer booklet are for planning or continuing an answer. If you use these pages, indicate at the original answer, the page number it is planned/continued on and write the question number being planned/continued on the additional working space page.
5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you do not use pencil, except in diagrams.
7. The Formula sheet is not to be handed in with your Question/Answer booklet.

**Section One: Calculator-free****35% (52 Marks)**

This section has **seven (7)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time for this section is 50 minutes.

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**Question 1****(6 marks)**

A particle leaves the origin when  $t = 1$  and moves in a straight line with velocity at any time  $t$  seconds, where  $t \geq 1$ , given by

$$v(t) = \frac{t^2}{4} + \frac{4}{t} - \frac{7}{4} \text{ ms}^{-1}$$

- (a) Determine the time when the acceleration of the particle is zero. (2 marks)

- (b) Determine the exact displacement of the particle from the origin when  $t = 4$ . (4 marks)

**Question 2****(7 marks)**

(a) Calculate  $f'(0)$  when  $f(x) = e^{2x}(1 + 5x)^3$ .

(3 marks)

(b) Determine  $\frac{d}{dx} \int_x^5 \sqrt{t^2 + 1} dt$ .

(2 marks)

(c) Given  $f'(x) = (1 - 2x)^4$  and  $f(1) = -1$ , determine  $f(x)$ .

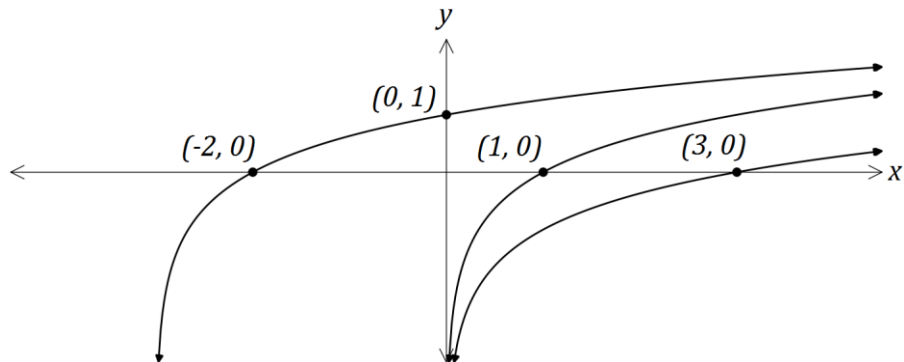
(2 marks)

**Question 3**

**(7 marks)**

- (a) The function  $f$  is defined by  $f(x) = \log_a x$ ,  $x > 0$ , where  $a$  is a constant,  $a > 1$ .

The graphs shown below have equations  $y = f(x)$ ,  $y = f(x + b)$  and  $y = f(x) + c$ , where  $b$  and  $c$  are constants.



Determine the values of the constants  $a$ ,  $b$  and  $c$ .

**(4 marks)**

- (b) Determine

- (i) the equation of the asymptote of the graph of  $y = \log_e(x - 3) - 2$ . **(1 mark)**

- (ii) the coordinates of the y-intercept of the graph of  $y = \log_2(x + 8) - 5$ . **(2 marks)**

**Question 4****(8 marks)**

A curve has equation  $y = 2x^5 - 5x^4 + 10$ .

- (a) Point  $A$  lies on the curve at  $(-1, 3)$ . Use the increments formula  $\delta y \approx \frac{dy}{dx} \times \delta x$  to estimate the  $y$ -coordinate of point  $B$  that has an  $x$ -coordinate of  $-0.99$ .

**(4 marks)**

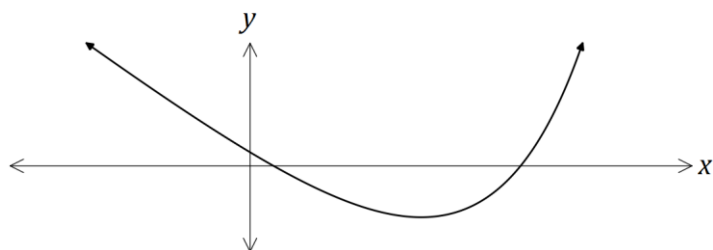
- (b) Point  $C$  also lies on the curve, at  $(2, -6)$ . Verify that  $C$  is either a minimum or maximum point of the curve. **(4 marks)**

**Question 5**

**(8 marks)**

- (a) Determine the coordinates of the root of the graph of  $y = \log_3(2x + 1) - 2$ . (3 marks)

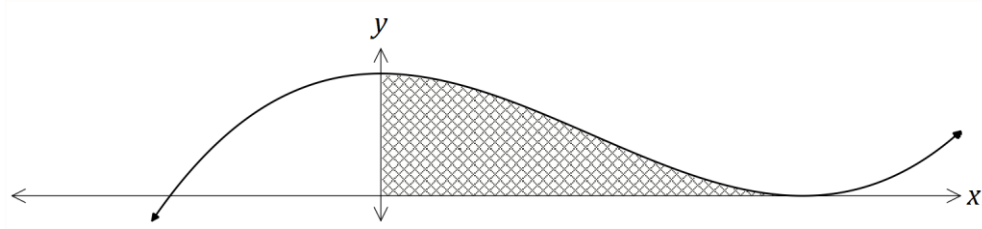
- (b) The graph of  $y = e^{2x-1} - 4x$  has a single stationary point, as shown on the graph below.



Determine the exact coordinates of the stationary point. (5 marks)

**Question 6****(8 marks)**

The diagram below shows the curve  $y = x^3 - 3x^2 + k$ , where  $k$  is a constant. The curve has a turning point on the  $y$ -axis.



- (a) Determine the value of  $k$ . (3 marks)

- (b) Determine the set of values of  $x$  for which  $\frac{dy}{dx}$  is increasing. (2 marks)

- (c) Calculate the area of the shaded region. (3 marks)



**Question 7****(8 marks)**

The discrete random variable  $X$  is defined by  $P(X = x) = k \log x$  for  $x = 2, 5$  and  $10$ .

(a) Determine the value of  $k$ . (3 marks)

(b) Determine  $P(X = 2 \mid X < 10)$ . (2 marks)

(c)  $E(X) = a(b + \log \sqrt{c})$ , where the constants  $a$ ,  $b$  and  $c$  are prime numbers. Determine the values of  $a$ ,  $b$  and  $c$ . (3 marks)

**Additional working space**

Question number: \_\_\_\_\_

**Additional working space**

Question number: \_\_\_\_\_

