

High School Mathematics Test 2013

Year

Surds

Non Calculator

Skills and Knowledge Assessed:

- Define rational and irrational numbers and perform operations with surds and fractional indices (ACMNA264)

Name _____

Section 1 Short Answer Section

Write all working and answers in the spaces provided on this test paper.

1. Simplify $9\sqrt{2} \times 4\sqrt{7}$.

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2. Simplify $8\sqrt{5} - 3\sqrt{5} + \sqrt{5}$.

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3. Simplify $7\sqrt{6} + 8\sqrt{2} + 4\sqrt{6} - \sqrt{2}$.

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.....

4. Simplify $\sqrt{128}$.

.....

5. Simplify $\sqrt{50} - \sqrt{18}$.

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.....

6. Simplify $\frac{8\sqrt{26}}{4\sqrt{2}}$.

.....

.....

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7. Express with a rational denominator $\frac{4\sqrt{3}}{3\sqrt{5}}$.

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8. Expand $4\sqrt{6} (3\sqrt{3} + 7\sqrt{5})$.

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9. Expand and simplify $24 + 5\sqrt{3} - 4\sqrt{6} (5\sqrt{2} - \sqrt{6})$.

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10. Express $\frac{2\sqrt{5} - 3\sqrt{2}}{3\sqrt{5}}$ with a rational denominator.

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11. Expand and simplify $(2\sqrt{3} - 4)(\sqrt{3} + 5)$.

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12. Express $6\sqrt{5}$ as a complete surd. (i.e as \sqrt{x} .)

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Section 2 Multiple Choice Section

Mark all your answers on the accompanying multiple choice answer sheet, not on this test paper. You may do any working out on this test paper. Calculators are allowed for this section.

1. $(-2\sqrt{6})^2 = ?$

A. $-12\sqrt{6}$

B. -12

C. 12

D. 24

2. Completely simplify $\sqrt{192}$.

A. $8\sqrt{3}$

B. $16\sqrt{3}$

C. $2\sqrt{48}$

D. $4\sqrt{48}$

3. If $9\sqrt{6} = \sqrt{x}$ then $x = ?$

A. 54

B. 324

C. 486

D. $2\,916$

4. $3\sqrt{5} - 2\sqrt{6} + \sqrt{5} - 5\sqrt{6} =$

A. $3\sqrt{5} - 7\sqrt{6}$

B. $4\sqrt{5} - 7\sqrt{6}$

C. $3\sqrt{5} - 4\sqrt{6}$

D. $4\sqrt{5} - 3\sqrt{6}$

5. Express $2\sqrt{6} \times 6\sqrt{10}$ in simplest form.

A. $12\sqrt{16}$

B. $12\sqrt{60}$

C. $24\sqrt{15}$

D. $24\sqrt{60}$

6. $\frac{8\sqrt{15}}{4\sqrt{3}} =$

A. $2\sqrt{3}$

B. $2\sqrt{5}$

C. $4\sqrt{3}$

D. $4\sqrt{5}$

7. Simplify $5\sqrt{162} + 3\sqrt{128}$.

A. $8\sqrt{34}$

B. $39\sqrt{2}$

C. $69\sqrt{2}$

D. $8\sqrt{290}$

8. Expand and simplify $5\sqrt{2} (3\sqrt{5} - 4\sqrt{2})$.

- A. $15\sqrt{10} - 40$ B. $15\sqrt{10} - 80$ C. $30\sqrt{5} - 40$ D. $30\sqrt{5} - 80$
-

9. $\frac{2\sqrt{2} - 5\sqrt{6}}{4\sqrt{2}} =$

- A. $\frac{2 - 10\sqrt{3}}{8}$ B. $\frac{2 - 10\sqrt{3}}{4}$ C. $\frac{2 - 5\sqrt{3}}{8}$ D. $\frac{2 - 5\sqrt{3}}{4}$
-

10. Expand $(3\sqrt{6} - 5\sqrt{5})^2$.

- A. $71 - 15\sqrt{30}$ B. $71 - 30\sqrt{30}$ C. $179 - 15\sqrt{30}$ D. $179 - 30\sqrt{30}$
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Section 3 Longer Answer Section

Write all working and answers in the spaces provided on this test paper.

Marks

1. a) Express $\frac{2\sqrt{6} - 3\sqrt{10}}{3 - \sqrt{10}}$ with a rational denominator.

2

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.....

- b) Arrange the numbers below in ascending order.
 $\sqrt{65}$, $2\sqrt{15}$, $\sqrt{61}$, 8, $3\sqrt{7}$.

2

.....

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High School Mathematics Test 2013

Multiple Choice Answer Sheet

Name _____

Completely fill the response oval representing the most correct answer.

- | | | | | | | | | |
|-----|---|-----------------------|---|-----------------------|---|-----------------------|---|-----------------------|
| 1. | A | <input type="radio"/> | B | <input type="radio"/> | C | <input type="radio"/> | D | <input type="radio"/> |
| 2. | A | <input type="radio"/> | B | <input type="radio"/> | C | <input type="radio"/> | D | <input type="radio"/> |
| 3. | A | <input type="radio"/> | B | <input type="radio"/> | C | <input type="radio"/> | D | <input type="radio"/> |
| 4. | A | <input type="radio"/> | B | <input type="radio"/> | C | <input type="radio"/> | D | <input type="radio"/> |
| 5. | A | <input type="radio"/> | B | <input type="radio"/> | C | <input type="radio"/> | D | <input type="radio"/> |
| 6. | A | <input type="radio"/> | B | <input type="radio"/> | C | <input type="radio"/> | D | <input type="radio"/> |
| 7. | A | <input type="radio"/> | B | <input type="radio"/> | C | <input type="radio"/> | D | <input type="radio"/> |
| 8. | A | <input type="radio"/> | B | <input type="radio"/> | C | <input type="radio"/> | D | <input type="radio"/> |
| 9. | A | <input type="radio"/> | B | <input type="radio"/> | C | <input type="radio"/> | D | <input type="radio"/> |
| 10. | A | <input type="radio"/> | B | <input type="radio"/> | C | <input type="radio"/> | D | <input type="radio"/> |

High School Mathematics Test 2013 Surd

ANSWERS

Section 1	
1.	$9\sqrt{2} \times 4\sqrt{7} = 36\sqrt{14}$
2.	$8\sqrt{5} - 3\sqrt{5} + \sqrt{5} = 6\sqrt{5}$
3.	$7\sqrt{6} + 8\sqrt{2} + 4\sqrt{6} - \sqrt{2} = 11\sqrt{6} + 7\sqrt{2}$
4.	$\sqrt{128} = \sqrt{64} \times \sqrt{2} = 8\sqrt{2}$
5.	$\sqrt{50} - \sqrt{18} = \sqrt{25} \times \sqrt{2} - \sqrt{9} \times \sqrt{2} = 5\sqrt{2} - 3\sqrt{2} = 2\sqrt{2}$
6.	$\frac{8\sqrt{26}}{4\sqrt{2}} = 2\sqrt{13}$
7.	$\frac{4\sqrt{3}}{3\sqrt{5}} = \frac{4\sqrt{3}}{3\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}} = \frac{4\sqrt{15}}{3 \times 5} = \frac{4\sqrt{15}}{15}$
8.	$4\sqrt{6} (3\sqrt{3} + 7\sqrt{5}) = 12\sqrt{18} + 28\sqrt{30}$ $= 12 \times \sqrt{9} \times \sqrt{2} + 28\sqrt{30}$ $= 36\sqrt{2} + 28\sqrt{30}$
9.	$24 + 5\sqrt{3} - 4\sqrt{6} (5\sqrt{2} - \sqrt{6}) = 24 + 5\sqrt{3} - 20\sqrt{12} + 4\sqrt{36}$ $= 24 + 5\sqrt{3} - 40\sqrt{3} + 24$ $= 48 - 35\sqrt{3}$
10.	$\frac{2\sqrt{5} - 3\sqrt{2}}{3\sqrt{5}} = \frac{2\sqrt{5} - 3\sqrt{2}}{3\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}}$ $= \frac{10 - 3\sqrt{10}}{15}$
11.	$(2\sqrt{3} - 4)(\sqrt{3} + 5) = 2\sqrt{9} + 10\sqrt{3} - 4\sqrt{3} - 20$ $= 6 + 6\sqrt{3} - 20$ $= -14 + 6\sqrt{3}$
12.	$6\sqrt{5} = \sqrt{36} \times \sqrt{5}$ $= \sqrt{180}$

	Section 2
1.	D
2.	A
3.	C
4.	B
5.	C
6.	B
7.	C
8.	A
9.	D
10.	D

	Section 3
1.	$\begin{aligned} \text{a) } \frac{2\sqrt{6} - 3\sqrt{10}}{3 - \sqrt{10}} &= \frac{2\sqrt{6} - 3\sqrt{10}}{3 - \sqrt{10}} \times \frac{3 + \sqrt{10}}{3 + \sqrt{10}} \\ &= \frac{6\sqrt{6} + 2\sqrt{60} - 9\sqrt{10} - 30}{9 - 10} \\ &= \frac{6\sqrt{6} + 4\sqrt{15} - 9\sqrt{10} - 30}{-1} \\ &= 9\sqrt{10} + 30 - 6\sqrt{6} - 4\sqrt{15} \end{aligned}$
	$\begin{aligned} \text{b) } &\sqrt{65} \\ 2\sqrt{15} &= \sqrt{4} \times \sqrt{15} = \sqrt{60} \\ &\sqrt{61} \\ 8 &= \sqrt{64} \\ 3\sqrt{7} &= \sqrt{9} \times \sqrt{7} = \sqrt{63} \\ \text{In order } &2\sqrt{15}, \sqrt{61}, 3\sqrt{7}, 8, \sqrt{65}. \end{aligned}$

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Multiple Choice Answer Sheet

Name _____ Marking Sheet

Completely fill the response oval representing the most correct answer.

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|-----|---|----------------------------------|---|----------------------------------|---|----------------------------------|---|----------------------------------|
| 1. | A | <input type="radio"/> | B | <input type="radio"/> | C | <input type="radio"/> | D | <input checked="" type="radio"/> |
| 2. | A | <input checked="" type="radio"/> | B | <input type="radio"/> | C | <input type="radio"/> | D | <input type="radio"/> |
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| 9. | A | <input type="radio"/> | B | <input type="radio"/> | C | <input type="radio"/> | D | <input checked="" type="radio"/> |
| 10. | A | <input type="radio"/> | B | <input type="radio"/> | C | <input type="radio"/> | D | <input checked="" type="radio"/> |