

Unit 1
Semester 1 2018
Mathematics Methods Test 1

Name	Score	Resource Free	
		Resource Assisted	
		Total	

Attempt all questions and full working out must be shown to get full marks.

Total Time: 60 minutes

- | | | |
|------------------------------------|------------|----------|
| • Section 1 (Calculator Free): | 25 minutes | 24 marks |
| • Section 2 (Calculator Assisted): | 35 minutes | 31 marks |

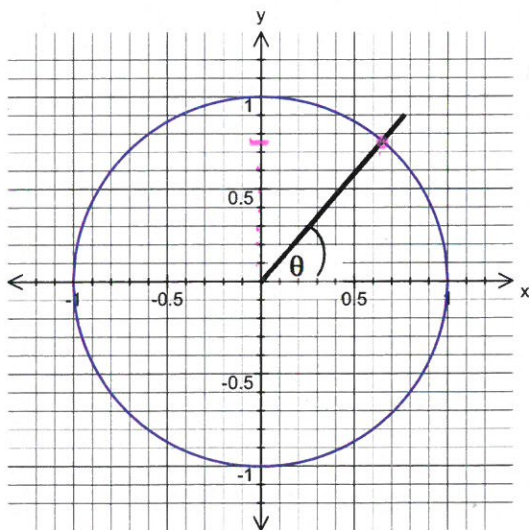
Calculator Free

Question 1

3
(4 marks)

Using the unit circle supplied

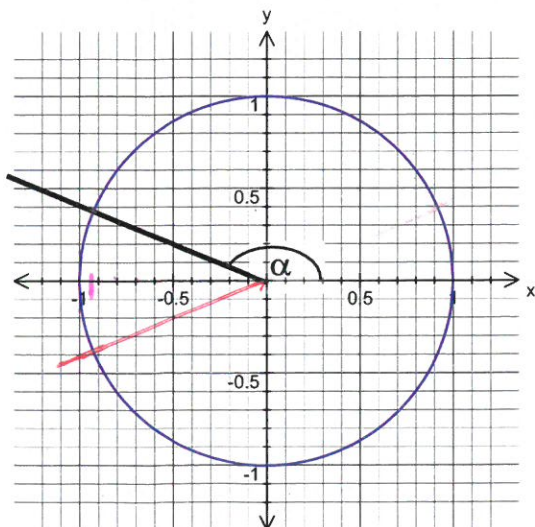
(a)



(i) find $\sin \theta$

$\sin \theta = 0.75$ ✓

(b)



(i) find $\cos \theta$

$\cos \theta = -0.92$ ✓

iii) draw the other angle with the same

Question 2**(7 marks -1,1,1,1,1,2,)**

(a) Convert these angles into degrees:

(i) $\frac{2\pi}{3} \times \frac{180}{\pi} = 120^\circ$ ✓

(ii) $\frac{5\pi}{6} \times \frac{180}{\pi} = 150^\circ$ ✓

(b) Express these angles in radians

(i) $30^\circ \times \frac{\pi}{180} = \frac{\pi}{6}$ ✓

(ii) $210^\circ \times \frac{\pi}{180} = \frac{7\pi}{6}$ ✓

(c) State the exact value of $\sin(2\pi)$

$\sin 360^\circ = 0$ ✓

(d) Write down the exact values of $\sin\left(\frac{11\pi}{4}\right)$ $\left(\frac{2\pi}{3}\right)$ $\frac{11\pi}{4} \times \frac{180}{\pi}$ ✓
 $\sin(120^\circ) = \frac{\sqrt{3}}{2}$ ✓

Question 3**(2 marks)**

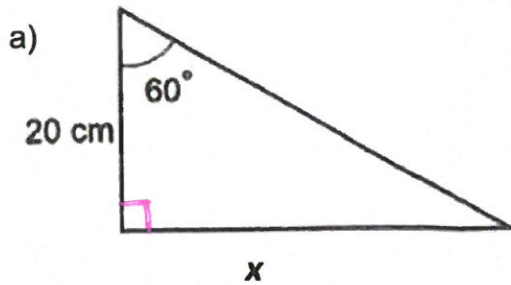
Simplify and express with a rational denominator: $\frac{\sqrt{7}-6}{\sqrt{7}+6}$

$$\begin{aligned} \frac{\sqrt{7}-6}{\sqrt{7}+6} \times \frac{\sqrt{7}-6}{\sqrt{7}-6} &= \frac{(\sqrt{7}-6)(\sqrt{7}-6)}{(\sqrt{7}+6)(\sqrt{7}-6)} \\ &= \frac{7-12\sqrt{7}+36}{7-36} \\ &= \frac{43-12\sqrt{7}}{-29} \end{aligned}$$
 ✓

Question 4

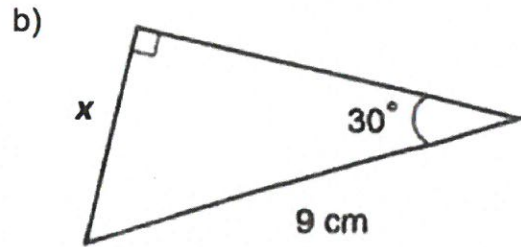
9
(8 marks)

i) Find x in simplified exact form in each of these two diagrams:



$$\tan 60^\circ = \frac{x}{20}$$

$$x = 20\sqrt{3} \text{ cm}$$



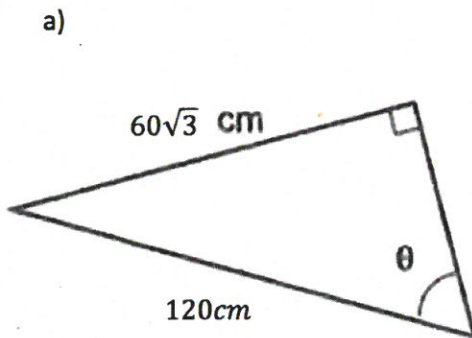
$$\sin 30^\circ = \frac{x}{9}$$

$$x = 9 \sin 30^\circ$$

$$= 9 \times \frac{1}{2}$$

$$= 4.5 \text{ cm}$$

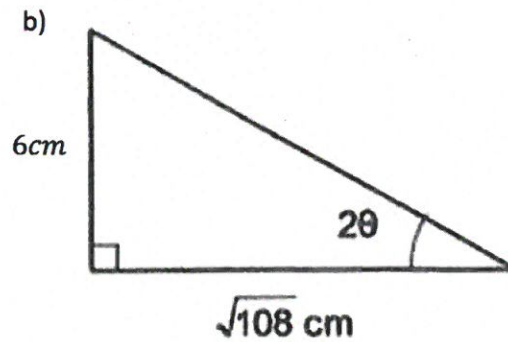
ii) Find θ in each of the following two diagrams.



$$\sin \theta = \frac{60\sqrt{3}}{120}$$

$$= \frac{\sqrt{3}}{2}$$

$$\theta = 60^\circ$$



$$\tan 2\theta = \frac{6}{\sqrt{108}}$$

$$\tan 2\theta = \frac{6}{6\sqrt{3}}$$

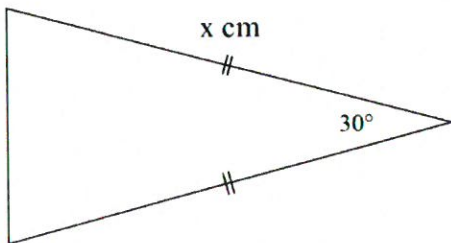
$$\tan 2\theta = \frac{1}{\sqrt{3}}$$

$$2\theta = 30^\circ$$

$$\theta = 15^\circ$$

Question 5**(3 marks)**

The triangle shown below has an area of 36 cm^2 , determine the value of x .



$$\text{Area} = \frac{1}{2} a(b) \sin C$$

$$36 = \frac{1}{2} x^2 \sin 30^\circ \checkmark$$

$$36 = \frac{1}{2} \times x^2 \times \frac{1}{2}$$

$$36 = \frac{1}{4} x^2 \checkmark$$

$$x^2 = 144$$

$$x = \sqrt{144}$$

$$= \underline{12 \text{ cm}} \checkmark$$