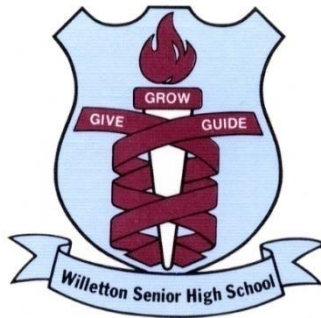


MATHEMATICS APPLICATIONS

YEAR 12 UNIT 3

TEST 2

2022



PART A

CALCULATOR FREE

TIME: 20 mins
MARKS: 25 marks

STUDENT'S NAME: _____

**CIRCLE YOUR
TEACHER'S NAME:**

Mr Galbraith

Mr Ismail

Mrs Kalotay

Mr Lee

Mrs Smirke

Ms Thompson

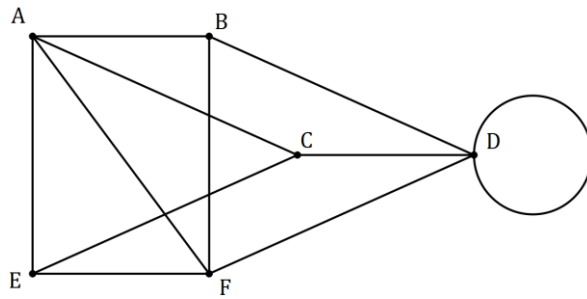
MATERIALS SUPPLIED: Formula Sheet

Question 1

(5 marks)

- (a) Re-draw the following graph to clearly demonstrate that it is planar.

(2 marks)



- (b) Draw a complete graph with five vertices.

(1 mark)

- (c) Do **all** complete graphs obey Euler's formula? Explain your answer.

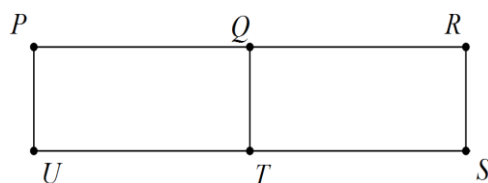
(2 marks)

Question 2

(4 marks)

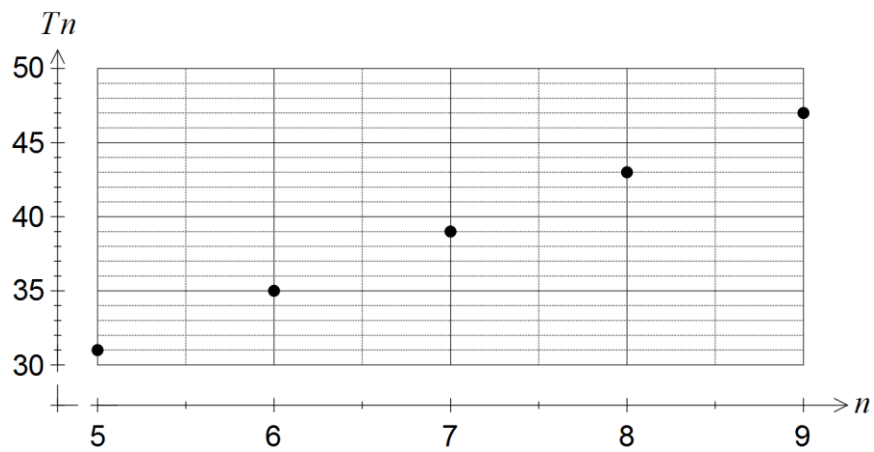
- (a) Three hikers were sharing tips about climbing the world's highest mountains. Alison had climbed Everest (E), K2 and Kangchenjunga (K), Ben had climbed Everest and Lhotse (L) and Chris had climbed Kangchenjunga and Lhotse. Display this information as a bipartite graph. (2 marks)

- (b) A bipartite graph is shown below, joining vertices in two disjoint sets. Redraw the graph, clearly showing the vertices that belong in each set. (2 marks)



Question 3**(8 marks)**

The terms of a sequence are shown in the graph below.

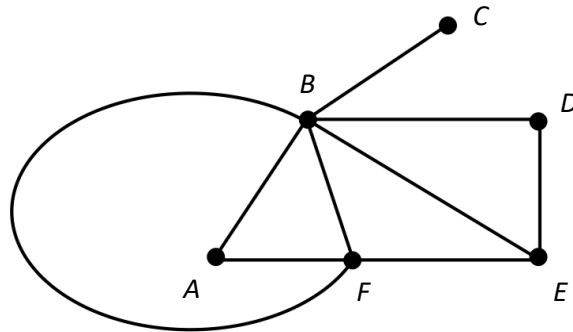


- (a) Choose the best description of the sequence from geometric, arithmetic or neither, explaining your choice. (2 marks)
- (b) Determine
- (i) T_{10} (1 mark)
- (ii) T_1 (1 mark)
- (c) Deduce a rule for the n^{th} term of the sequence, simplifying your answer. (2 marks)
- (d) Determine the value of n such that $T_n = 415$. (2 marks)

Question 4

(8 marks)

The edges in the graph below represent the roads in a park that meet at the given vertices.



(a) State a bridge that is found in this graph. (1 mark)

(b) Show that Euler's formula applies to this graph. (2 marks)

(c) Record the degree of each vertex shown in the graph in the table below. (2 marks)

Vertex	A	B	C	D	E	F
Degree						

(d) Without referring to the information in (c), clearly explain why the graph is semi-Eulerian. (2 marks)

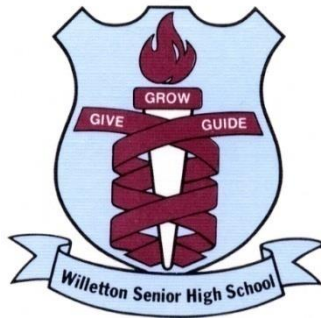
(e) A park ranger has to inspect every road in the park. List all possible starting points so that the ranger can complete this task without driving on the same road more than once. (1 mark)

MATHEMATICS APPLICATIONS

YEAR 12 UNIT 3

TEST 2

2022



PART B

CALCULATOR ASSUMED

TIME: 30 mins
MARKS: 30 marks

STUDENT'S NAME: _____

**CIRCLE YOUR
TEACHER'S NAME:**

Mr Galbraith

Mr Ismail

Mrs Kalotay

Mr Lee

Mrs Smirke

Ms Thompson

MATERIALS SUPPLIED: Formula Sheet

MATERIALS RECOMMENDED: Up to three approved calculators
One A4 single sided unfolded page of notes

Question 5**(7 marks)**

The number of votes still to count at the end of an election, decreased by 72 votes every minute after 6 pm. At 6 pm, 2955 votes still needed counting.

- (a) Show that by 6:02 pm, 2811 votes still needed counting. (1 mark)
- (b) Determine the n th term rule for the number of votes still needing counting n minutes after 6 pm. (2 marks)
- (c) Determine how many votes still needed counting at 6:30 pm. (1 mark)
- (d) At 6:30 pm, counting slowed so that only 36 votes were processed every minute. Determine the time, to the nearest minute, that counting finished. (3 marks)

Question 6**(6 marks)**

Sequence T is defined given by $T_{n+1} = 1.25T_n$, $T_1 = 50$.

- (a) Use the recursive rule to complete the table below, rounding values to one decimal place.

(2 marks)

n	1	2	3	4	5	6
T_n	50					

The first three terms of the geometric sequence U are 200, 160 and 128.

- (b) Determine a rule for the n^{th} term of sequence U . (2 marks)
- (c) Determine the largest value of n so that $U_n > T_n$ and justify your answer. (2 marks)

Question 7**(7 marks)**

A fish farmer initially stocked a tank with 50 small fish. Each month, the farmer caught some of the largest fish and sold them before adding more, smaller fish to the tank.

The number of fish in the tank at the start of the n^{th} month is given by the recurrence relation, F_n

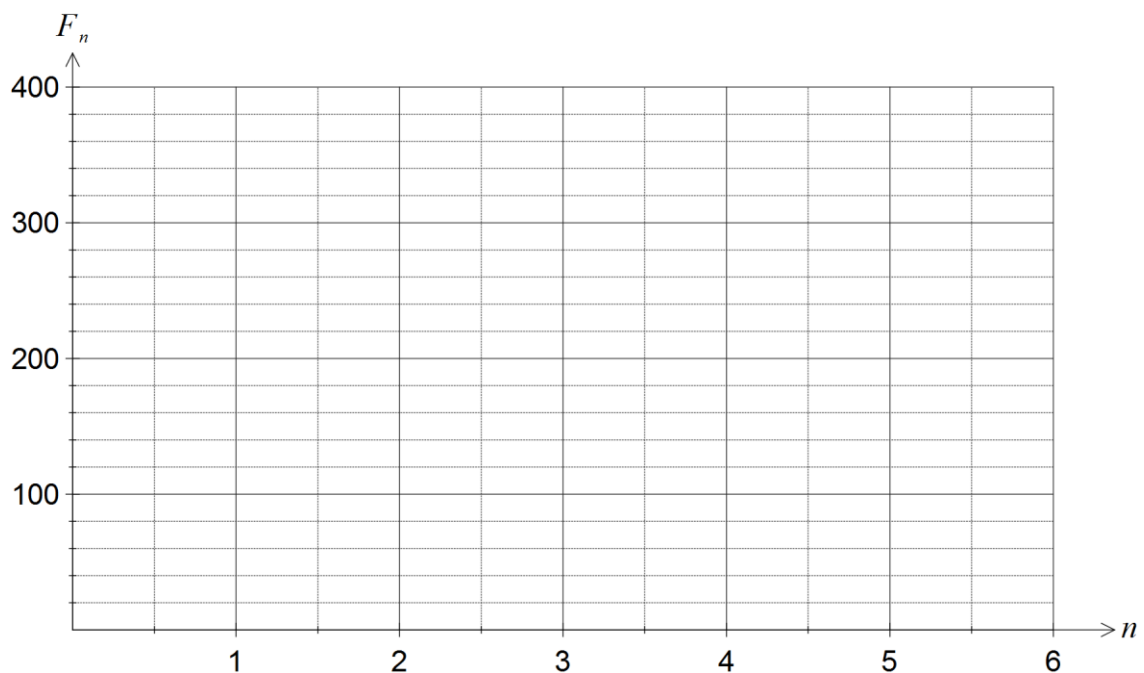
where $F_{n+1} = 0.7F_n + 120$, $F_1 = 50$.

(a) Use the recurrence relation to state

(i) the number of smaller fish added to the tank each month. (1 mark)

(ii) the percentage of the fish caught and sold each month. (1 mark)

(b) Graph F_n on the axes below for $1 \leq n \leq 6$. (3 marks)



Assuming this model continues, comment on how the number of fish in the tank changes

(c) over the next few months. (1 mark)

(d) in the long term. (1 mark)

Question 8**(5 marks)**

An art gallery records the value of all artworks at the start of each year for insurance purposes. The first valuation of a painting was \$4 800. The next two years the painting was valued at \$5 040 and \$5 292 respectively.

(a) Show that the painting values form a geometric sequence. (1 mark)

(b) Assuming that the value of the painting continues to increase in this way, and the insurance premium is 2.5% of the value of the painting,

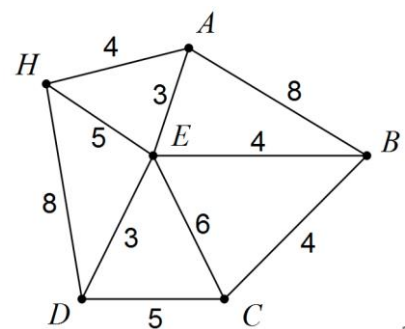
(i) calculate the insurance premium for the painting at the start of the tenth year. (2 marks)

(ii) determine at the start of which year the insurance premium will first exceed \$300. (2 marks)

Question 9**(5 marks)**

The vertex H on the graph to the right, represents a hotel and vertices A to E represent tourist attractions. The numbers on the edges of the graph represent the walking times, in minutes, between the various attractions.

A group of tourists plan to leave the hotel at 9 am and visit all the attractions, spending 45 minutes at each one. One member of the group suggests that the route that the group plan should be a Hamiltonian cycle.



(a) Explain what is meant by a Hamiltonian cycle. (2 marks)

(b) Determine the Hamiltonian cycle the group of tourists should walk and state the time they will arrive back at their hotel. (3 marks)