

Question 10**(4 marks)**

Consider the complex number $z = \sqrt{3} + i$.

Show that, for all positive integers n , $(z)^n - (\bar{z})^n = 2^{n+1} \sin\left(\frac{n\pi}{6}\right) i$.