Question 11 (8 marks)

Judith monitors the water quality in her garden pond at the same time every day. She likes to maintain the concentration of algae at between 200 and 250 units per 100 litres (L). Her measurements show that the concentration increases daily according to the recursive rule  $C_{n+1} = 1.025 C_n$ , where  $C_1 = 200$  units per 100 L (the minimum concentration).

When the concentration gets above the 250 units per 100 L limit, she treats the water to bring the concentration back to the minimum 200 units per 100 L.

- (a) If Judith treated the water on Sunday, 6 December 2020, determine
  - (i) the concentration on Wednesday, 9 December 2020. (2 marks)

(ii) the day and date when she next treated the water. (2 marks)

(b) During the first week of January 2021, Judith monitored the water and recorded the following readings.

Day	1	2	3	4	5	6	7
Concentration (C)	200	206	212.18	218.55	225.10	231.85	238.81

(i) Determine the revised recursive rule. (2 marks)

(ii)	If she treated the water on 10 January and went on holiday until 20 January, when she next treated the water, calculate the concentration of the water on her return, assuming the recursive rule from part (b)(i) is used. (2 marks)