

Question 16**(12 marks)**

Plane Π_1 has Cartesian equation $z = 2x + y + 4$.

(a) Determine a vector that is normal to plane Π_1 .

(2 marks)

Line L has equation $\vec{r} = \begin{pmatrix} 2 \\ 0 \\ 3 \end{pmatrix} + \lambda \begin{pmatrix} 1 \\ 2 \\ -1 \end{pmatrix}$.

(b) Determine the point of intersection between line L and plane Π_1 .

(3 marks)

Plane Π_2 contains line L and is perpendicular to plane Π_1 .

- (c) Determine the vector equation for plane Π_2 . (4 marks)

Sphere S has vector equation $|\underline{r} - (3\underline{i} + \underline{j} + 4\underline{k})| = \sqrt{35}$.

- (d) Determine whether line L is a tangent to sphere S . Justify your answer. (3 marks)