

**Question 10****(15 marks)**

A football club records body measurements for all of their players. Shown below are the waistline measurements (cm) and percentage body fat for eleven players.

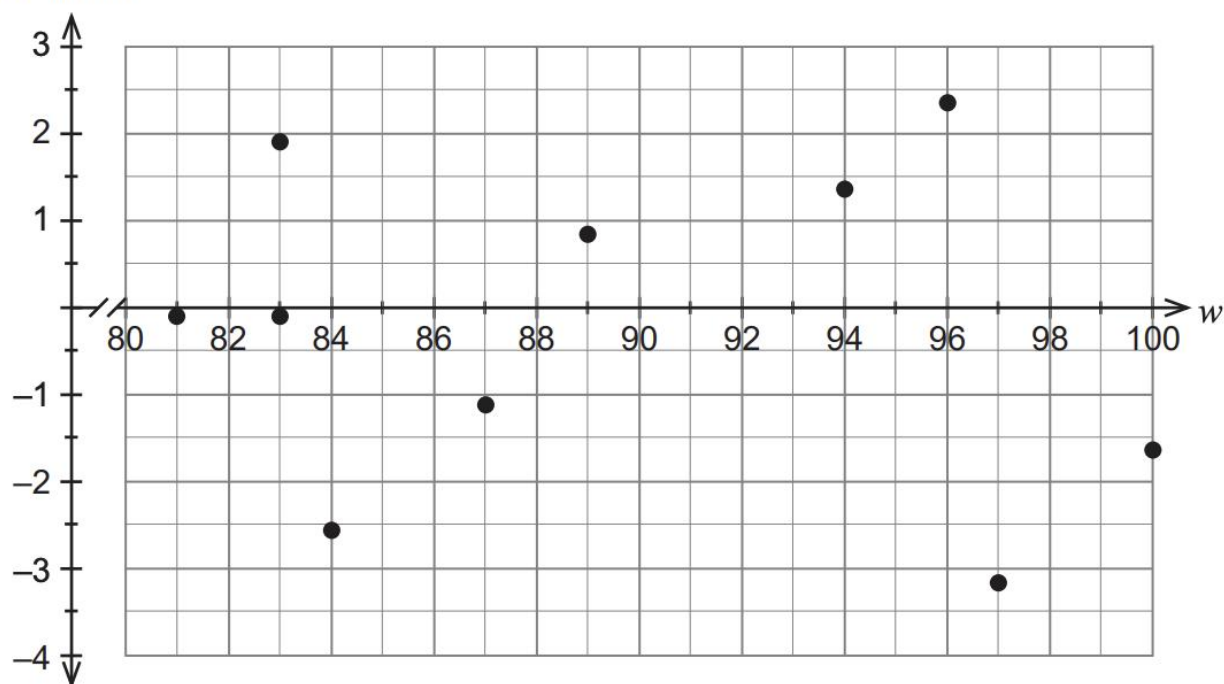
Player	1	2	3	4	5	6	7	8	9	10	11
Waistline measurement ( $w$ )	89	100	87	96	94	83	81	83	84	97	98
Percentage body fat ( $p$ )	14	17	11	19	17	12	9	10	8	14	19

Research has shown that estimates for percentage body fat can be determined by using waistline measurements.

- (a) Calculate the correlation coefficient  $r_{wp}$  for these data. (1 mark)
- (b) Determine the equation of the least-squares line for these data. (1 mark)
- (c) In the context of this question, interpret the slope of the line found in part (b). (2 marks)

- (d) The residual plot shown below is for the first 10 players' data. Calculate the residual for player number 11 and plot this point on the graph. (2 marks)

Residual



- (e) Comment on the appropriateness of fitting a linear model to the data. Justify your answer.  
(2 marks)
- (f) What percentage of the variation in the percentage body fat measurements is **unexplained** by the variation in the waistline measurements?  
(2 marks)
- (g) Wayne is player number 12 and has a waistline measurement of 105 cm.
- (i) Determine his predicted percentage of body fat.  
(1 mark)
- (ii) Comment on the validity of the prediction and give a justification for your answer.  
(2 marks)
- (h) Player number 13 has a residual of  $-2.6$ . What information does this provide about the percentage body fat for this player?  
(2 marks)