

**Question 5****(4 marks)**

Using the substitution  $u = \cos(2x)$ , evaluate exactly the definite integral

$$\int_0^{\frac{\pi}{4}} \cos^{1008}(2x) \sin(2x) \, dx.$$