Question 1 **(4 marks)**

Using the identity $2\sin A \cos B = \sin(A + B) + \sin(A - B)$, evaluate exactly the definite integral

$$\int_0^{\frac{\pi}{2}} 6\sin\left(\frac{5x}{2}\right)\cos\left(\frac{x}{2}\right)\,dx.$$