Consider the function  $f(x) = \ln(x)$ . The function g(x) = f(x) + a is a vertical translation of f by a units.

(a) Express the function  $g(x) = \ln(4x)$  in terms of a vertical translation of f (i.e. in the form g(x) = f(x) + a), stating the number of units that f is translated. (2 marks)

The function h(x) = cf(x) is a vertical dilation of f by a scale factor of c.

(b) Express the function  $h(x) = \ln(\sqrt{x})$  in terms of a vertical dilation of f, stating the scale factor. (2 marks)

The function p(x) = f(bx) is a horizontal dilation of f by a scale factor of  $\frac{1}{b}$ .

(c) Express the function  $p(x) = \ln(x) + 4$  in terms of a horizontal dilation of f, stating the scale factor. (3 marks)