

**Question 14****(5 marks)**

- (a) The table below examines the values of  $\frac{a^h - 1}{h}$  for various values of  $a$  as  $h$  approaches zero. Complete the table, rounding your values to five decimal places. (2 marks)

$h$	$a = 2.60$	$a = 2.70$	$a = 2.72$	$a = 2.80$
0.1	1.00265		1.05241	1.08449
0.001	0.95597	0.99375		
0.00001	0.95552			1.02962

It can be shown that  $\frac{d}{dx}(a^x) = a^x \lim_{h \rightarrow 0} \left( \frac{a^h - 1}{h} \right)$ .

- (b) What is the exact value of  $a$  for which  $\frac{d}{dx}(a^x) = a^x$ ? Explain how the above definition and the table in part (a) support your answer. (3 marks)