# Package 'qrng'

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Title (Randomized) Quasi-Random Number Generators
<b>Description</b> Functionality for generating (randomized) quasi-random numbers in high dimensions.
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Compute Quasi-Random Sequences

## **Description**

Computing Korobov, generalize Halton and Sobol' quasi-random sequences.

# Usage

#### **Arguments**

n number n of points to be generated  $\geq 2$ .

d dimension d.

generator numeric of length d or length 1 (in which case it is appropriately extended to

length d). All numbers must be in  $\{1, \ldots, n\}$  and must be (coercible to) integers.

randomize character string indicating the type of randomization for the point set.

korobov() one of the following:

"none" no randomization.

"shift" a uniform random variate modulo 1.

sobol() one of the following:

"none" no randomization.

"digital.shift" a digital shift.

"Owen", "Faure.Tezuka", "Owen.Faure.Tezuka" calls sobol() from package randtoolbox with scrambling being 1, 2 and 3, respectively.

If randomize is a logical, then it is interpreted as "none" if FALSE and "digital.shift" if TRUE.

method character string indicating which sequence is generated, generalized Halton or

(plain) Halton.

seed if provided, an integer used within set.seed() for the non-scrambling randomize

methods (so "none" or "digital.shift") or passed to the underlying sobol() from package **randtoolbox** for the scrambling methods. If not provided, the non-scrambling methods respect a global set.seed() but the scrambling methods do not (they then use 4711 as default); see sobol() from package **randtool**-

box for details.

skip number of initial points in the sequence to be skipped (skip = 0 means the se-

quence starts with at the origin). Note that for the scrambling methods this

simply computes n + skip points and omits the first skip-many.

... additional arguments passed to sobol() from package randtoolbox.

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#### **Details**

For sobol() examples see demo(sobol\_examples). In particular, be careful when using skip > 0 and randomize = TRUE; in this case, choosing a wrong seed (or no seed) might lead to a bad sequence.

Note that these procedures call fast C code. The following restrictions apply:

```
\label{eq:korobov} \mbox{korobov}() \ \ \mbox{n,d must be} \leq 2^{31}-1. \mbox{ghalton}() \ \mbox{n must be} \leq 2^{32}-1 \mbox{ and d must be} \leq 360. \mbox{sobol}() \ \mbox{if randomize} = "\mbox{none}" \mbox{ or randomize} = "\mbox{digital.shift"}, \mbox{n must be} \leq 2^{31}-1 \mbox{ and d must be} \leq 16510.
```

The choice of parameters for korobov() is crucial for the quality of this quasi-random sequence (only basic sanity checks are conducted). For more details, see l'Ecuyer and Lemieux (2000).

The generalized Halton sequence uses the scrambling factors of Faure and Lemieux (2009).

#### Value

```
korobov() and ghalton() return an (n, d)-matrix; for d = 1 an n-vector is returned.
```

#### Author(s)

Marius Hofert and Christiane Lemieux

#### References

Faure, H., Lemieux, C. (2009). Generalized Halton Sequences in 2008: A Comparative Study. *ACM-TOMACS* **19**(4), Article 15.

l'Ecuyer, P., Lemieux, C. (2000). Variance Reduction via Lattice Rules. *Stochastic Models and Simulation*, 1214–1235.

Lemieux, C., Cieslak, M., Luttmer, K. (2004). RandQMC User's guide. See https://www.math.uwaterloo.ca/~clemieux/randc

# **Examples**

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Test Functions

# **Description**

Functions for testing low-discrepancy sequences.

# Usage

# Arguments

method

below).

u	$(n,d)$ -matrix containing $n$ $d$ -dimensional realizations (of a potential quasi-random number generator). For $sum\_of\_squares()$ these need to be marginally standard uniform and for $sobol\_g()$ they need to follow the copula specified by copula.
copula	Copula object for which the inverse Rosenblatt transformation exists.
alpha	vector of parameters of Sobol's g test function.
	additional arguments passed to the underlying cCopula().
x	(n, d)-matrix containing $n$ $d$ -dimensional realizations.
q	<b>"indicator"</b> <i>d</i> -vector containing the componentwise thresholds; if a number it is recycled to a <i>d</i> -vector.
	"individual.given.sum.exceeds", "sum.given.sum.exceeds" threshold for the sum (row sums of $x$ ).
р	If q is not provided, the probability p is used to determine q.
	<b>"indicator"</b> <i>d</i> -vector containing the probabilities determining componentwise thresholds via empirical quantiles; if a number, it is recycled to a <i>d</i> -vector.
	<b>"individual.given.sum.exceeds"</b> , <b>"sum.given.sum.exceeds"</b> probability determining the threshold for the sum (row sums of x) via the corresponding empirical quantile.

character string indicating the type of exceedance computed (see Section Value

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#### **Details**

For examples see the demo man\_test\_functions.

See ES\_np(<matrix>) from **qrmtools** for another test function.

#### Value

sum\_of\_squares() returns an *n*-vector (numeric(n)) with the rowwise computed scaled sum of squares (theoretically integrating to 1).

 $sobol_g()$  returns an n-vector (numeric(n)) with the rowwise computed Sobol' g functions. exceedance()'s return value depends on method:

"indicator" returns indicators whether, componentwise, x exceeds the threshold determined by q.

"individual.given.sum.exceeds" returns all rows of x whose sum exceeds the threshold determined by q.

"sum.given.sum.exceeds" returns the row sums of those rows of x whose sum exceeds the threshold determined by q.

#### Author(s)

Marius Hofert and Christiane Lemieux

#### References

Radovic, I., Sobol', I. M. and Tichy, R. F. (1996). Quasi-Monte Carlo methods for numerical integration: Comparison of different low discrepancy sequences. *Monte Carlo Methods and Applications* **2**(1), 1–14.

Faure, H., Lemieux, C. (2009). Generalized Halton Sequences in 2008: A Comparative Study. *ACM-TOMACS* **19**(4), Article 15.

Owen, A. B. (2003). The dimension distribution and quadrature test functions. *Stat. Sinica* **13**, 1–17.

Sobol', I. M. and Asotsky, D. I. (2003). One more experiment on estimating high-dimensional integrals by quasi-Monte Carlo methods. *Math. Comput. Simul.* **62**, 255—263.

# **Examples**

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```
## Compute an exceedance probability
X <- qnorm(U)
mean(exceedance(X, q = qnorm(0.99))) # fixed threshold q
mean(exceedance(X, p = 0.99)) # empirically estimated marginal p-quantiles as thresholds
## Compute 99% expected shortfall for the sum
mean(exceedance(X, p = 0.99, method = "sum.given.sum.exceeds"))
## Or use ES_np(X, level = 0.99) from 'qrmtools'</pre>
```

to\_array

Compute Matrices to Arrays

# **Description**

Converting higher-dimensional matrices of quasi-random numbers to arrays of specific formats.

# Usage

```
to_array(x, f, format = c("(n*f,d)", "(n,f,d)"))
```

#### **Arguments**

x (n,fd)-matrix of quasi-random numbers to be converted.

f factor  $f \ge 1$  dividing  $ncol\{x\}$ .

format character string indicating the output format to which x should be converted.

# **Details**

to\_array() is helpful for converting quasi-random numbers to time series paths.

#### Value

```
(n * f, d)-matrix or (n, f, d)-array depending on the chosen format.
```

# Author(s)

Marius Hofert

## See Also

```
korobov(), ghalton(), sobol().
```

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# **Examples**

```
## Basic call
N <- 4 # replications
n <- 3 # time steps
d <- 2 # dimension
set.seed(271) # note: respected for the choice of 'randomize'
x <- sobol(N, d = n * d, randomize = "digital.shift") # higher-dim. Sobol'
stopifnot(dim(to_array(x, f = n)) == c(N * n, d)) # conversion and check
stopifnot(dim(to_array(x, f = n, format = "(n,f,d)")) == c(N, n, d))

## See how the conversion is done
(x <- matrix(1:(N * n * d), nrow = N, byrow = TRUE))
to_array(x, f = n) # => (n * d)-column x was blocked in n groups of size d each
```

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