

Common Code

main.cpp:

```
//-----+
// John Call - A01283897
// Driver for ENGR 2450 homework
//-----+
#include "assign3\assign3.h"
#include <iostream>

int main() {
    assign3::main();

    system("pause");
    return 0;
}
```

assign3.h:

```
#pragma once

namespace assign3 {
    enum MatrixError {
        GOOD = 0,
        INV_DIM = 1,
        SINGULAR = 2
    };

    void main();
}
```

assign3.cpp:

```
#include "assign3.h"
#include "a3p1.h"
#include "a3p3.h"

void assign3::main() {
    assign3::Problem1();
    assign3::Problem3();
    assign3::Problem4();
}
```

matrix.cpp:

```
#include "matrix.h"

Matrix<double> Identity(int n) {
    Matrix<double> a(n, n, 0);
    for (int i = 0; i < n; ++i) {
        a[i][i] = 1;
    }
    return a;
}
```

matrix.h:

```
#pragma once
#include <vector>
#include <complex>
#include <iostream>
#include <type_traits>
#include <initializer_list>

template <typename T>
class Matrix {
private:
    T** _array;
    static T _default;

public:
    // Important properties
    int Rows, Cols;

    bool isSingular() { return _array == nullptr; };

    static void setDefault(T val) { _default = val; };

    // public access to _array
    T* operator [](int r) { return _array[r]; };

    // Common operations
    Matrix<T> Transpose() { return Transpose(*this); };
    T Trace() { return Trace(*this); };

    // Constructors and destructor
    Matrix(int m, int n) {
        Rows = m;
        Cols = n;
        _array = new T*[Rows];
        for (int i = 0; i < Rows; ++i) {
            _array[i] = new T[Cols];
            for (int j = 0; j < Cols; ++j) {
                _array[i][j] = _default;
            }
        }
    };

    // Allow initialized values
    Matrix(int m, int n, T val) {
        Rows = m;
        Cols = n;
        _array = new T*[Rows];
        for (int i = 0; i < Rows; ++i) {
            _array[i] = new T[Cols];
            for (int j = 0; j < Cols; ++j) {
                _array[i][j] = val;
            }
        }
    };

    // Allow for C++11 initializer_list
    Matrix(std::initializer_list<std::initializer_list<T>> s) {
```

```

        // Take advantage of vector handling initializer_list
        std::vector<std::initializer_list<T>> init = s;
        std::vector<std::vector<T>> data;
        for (auto i = init.begin(); i != init.end(); ++i) {
            data.push_back(std::vector<T>(*i));
        }

        Rows = data.size();
        Cols = data[0].size();
        _array = new T*[Rows];
        for (int i = 0; i < Rows; ++i) {
            _array[i] = new T[Cols];
            for (int j = 0; j < Cols; ++j) {
                _array[i][j] = data[i][j];
            }
        }
    };

    // Override default operator=, constructors, and destructor
    Matrix<T>& operator=(const Matrix<T> &a) {
        clean();
        copy(a);
        return *this;
    };

    Matrix() {
        Rows = 0;
        Cols = 0;
        _array = nullptr;
    };

    Matrix(const Matrix<T> &a) { copy(a); }
    ~Matrix() { clean(); };

private:
    void clean() {
        for (int i = 0; i < Cols; ++i) {
            delete _array[i];
        }
        delete _array;
        _array = nullptr;
    };

    void copy(const Matrix<T> &a) {
        this->Rows = a.Rows;
        this->Cols = a.Cols;
        this->_array = new T*[this->Rows];
        for (int i = 0; i < this->Rows; ++i) {
            this->_array[i] = new T[this->Cols];
            for (int j = 0; j < this->Cols; ++j) {
                this->_array[i][j] = a._array[i][j];
            }
        }
    };

public:
    // friend templates

```

```

template <typename f_T>
friend Matrix<f_T> Transpose(const Matrix<f_T>&);

template <typename f_T>
friend f_T Trace(const Matrix<f_T>&, bool&);

template <typename f_T>
friend std::ostream& operator<<(std::ostream&, const Matrix<f_T>&);

template <typename f_T>
friend std::vector<f_T> operator*(const Matrix<f_T>&, const
std::vector<f_T>&);

template <typename f_T1, typename f_T2>
friend Matrix<f_T1> operator*(const Matrix<f_T1>&, const Matrix<f_T2>&);

template <typename f_T1, typename f_T2>
friend Matrix<f_T1>& operator+=(Matrix<f_T1>&, const Matrix<f_T2>&);
};

template<typename T>
T Matrix<T>::_default = 0;

// common operations and helpers
template <typename f_T>
Matrix<f_T> Transpose(const Matrix<f_T> &a) {
    Matrix<f_T> trans(a.Cols, a.Rows);
    for (int i = 0; i < a.Rows; ++i) {
        for (int j = 0; j < a.Cols; ++j) {
            trans[i][j] = a._array[j][i];
        }
    }
    return trans;
}

template <typename f_T>
f_T Trace(const Matrix<f_T> &a, bool& error) {
    f_T sum = a._default;

    if (a.Rows != a.Cols) {
        error = true;
    } else {
        error = false;
        for (int i = 0; i < a.Rows; ++i) {
            sum += a._array[i][i];
        }
    }

    return sum;
}

// iostream handlers
template <typename T>
std::istream& operator>>(std::istream &in, Matrix<T> &obj) {
    int m, n;
    in >> m;
    in >> n;

```

```

    obj = Matrix<T>(m, n);
    for (int i = 0; i < m; ++i) {
        for (int j = 0; j < n; ++j) {
            in >> obj[i][j];
        }
    }
    return in;
}

template <typename f_T>
std::ostream& operator<<(std::ostream &out, const Matrix<f_T> &obj) {
    out << std::endl;
    for (int i = 0; i < obj.Rows; ++i) {
        out << "[";
        for (int j = 0; j < obj.Cols; ++j) {
            out << obj._array[i][j];
            if (j < obj.Cols - 1) {
                out << ", ";
            }
        }
        out << "]" << std::endl;
    }
    out << std::endl;
    return out;
}

template <typename T>
std::ostream& operator<<(std::ostream &out, const std::vector<T> &obj) {
    out << "[";
    for (auto i = obj.begin(); i < obj.end(); ++i) {
        out << *i;
        if (i < obj.end() - 1) {
            out << ", ";
        }
    }
    out << "];";
    return out;
}

// scalar multiplication
template <typename T, typename N,
    typename std::enable_if<std::is_arithmetic<N>::value>::type* = nullptr>
Matrix<T> operator*(const N &c, const Matrix<T> &a) {
    Matrix<T> b(a);
    for (int i = 0; i < b.Rows; ++i) {
        for (int j = 0; j < b.Cols; ++j) {
            b[i][j] *= c;
        }
    }
    return b;
}

template <typename T, typename N,
    typename std::enable_if<std::is_arithmetic<N>::value>::type* = nullptr>
Matrix<T> operator*(const Matrix<T> &a, const N &c) { return c * a; }

// complex scalar multiplication

```

```

template <typename T, typename N, typename C,
        typename std::enable_if<std::is_arithmetic<N>::value>::type* = nullptr,
        typename std::enable_if<std::is_same<C, std::complex<N>>::value>::type* =
nullptr>
Matrix<T> operator*(const C &c, const Matrix<T> &a) {
    Matrix<T> b(a);
    for (int i = 0; i < b.Rows; ++i) {
        for (int j = 0; j < b.Cols; ++j) {
            b[i][j] *= c;
        }
    }
    return b;
}

template <typename T, typename N, typename C,
        typename std::enable_if<std::is_arithmetic<N>::value>::type* = nullptr,
        typename std::enable_if<std::is_same<C, std::complex<N>>::value>::type* =
nullptr>
Matrix<T> operator*(const Matrix<T> &a, const C &c) { return c * a; }

// vector multiplication
template <typename f_T>
std::vector<f_T> operator*(const Matrix<f_T> &a, const std::vector<f_T> &x) {
    std::vector<f_T> b(a.Rows);
    for (int i = 0; i < a.Rows; ++i) {
        b[i] = a._default;
        for (int j = 0; j < a.Cols; ++j) {
            b[i] += a._array[i][j] * x[j];
        }
    }
    return b;
}

// matrix multiplication
template <typename T1, typename T2>
Matrix<T1>& operator*=(Matrix<T1> &a, const Matrix<T2> &b) {
    // Matrix multiplication is more complicated than numeric addition
    // Because 'a' would need to be resized, it is more efficient
    // To use operator* here than to use '*' in 'operator*'
    return a = a * b;
}

template <typename f_T1, typename f_T2>
Matrix<f_T1> operator*(const Matrix<f_T1> &a, const Matrix<f_T2> &b) {
    Matrix<f_T1> c(a.Rows, b.Cols, a._default);
    for (int i = 0; i < a.Rows; ++i) {
        for (int j = 0; j < a.Cols; ++j) { // a.Cols = b.Rows (or error)
            for (int k = 0; k < b.Cols; ++k) {
                c[i][k] += a._array[i][j] * b._array[j][k];
            }
        }
    }
    return c;
}

// matrix addition
template <typename f_T1, typename f_T2>

```

```

Matrix<f_T1>& operator+=(Matrix<f_T1> &a, const Matrix<f_T2> &b) {
    for (int i = 0; i < a.Rows; ++i) {
        for (int j = 0; j < a.Cols; ++j) {
            a._array[i][j] += b._array[i][j];
        }
    }

    return a;
}

template <typename T1, typename T2>
Matrix<T1> operator+(const Matrix<T1> &a, const Matrix<T2> &b) {
    Matrix<T1> c(a);
    c += b;
    return c;
}

// matrix subtraction
template <typename f_T1, typename f_T2>
Matrix<f_T1>& operator-=(Matrix<f_T1> &a, const Matrix<f_T2> &b) {
    for (int i = 0; i < a.Rows; ++i) {
        for (int j = 0; j < a.Cols; ++j) {
            a._array[i][j] -= b._array[i][j];
        }
    }

    return a;
}

template <typename T1, typename T2>
Matrix<T1> operator-(const Matrix<T1> &a, const Matrix<T2> &b) {
    Matrix<T1> c(a);
    c -= b;
    return c;
}

// prototypes defined in cpp file
Matrix<double> Identity(int);

```

Problem 1

9.18 Develop, debug, and test a program in either a high-level language or macro language of your choice to solve a system of equations with Gauss elimination with partial pivoting. Base the program on the pseudocode from Fig. 9.6. Test the program using the following system (which has an answer of $x_1 = x_2 = x_3 = 1$).

$$\begin{aligned}x_1 + 2x_2 - x_3 &= 2 \\ 5x_1 + 2x_2 + 2x_3 &= 9 \\ -3x_1 + 5x_2 - x_3 &= 1\end{aligned}$$

a3p1.h:

```
#pragma once
#include <vector>
#include "assign3.h"
#include "../shared/matrix.h"

namespace assign3 {
    namespace p1 {
        void Substitute(Matrix<double>&, std::vector<double>&,
std::vector<double>&);
        void Pivot(Matrix<double>&, std::vector<double>&,
std::vector<double>&, int);
        void Eliminate(Matrix<double>&, std::vector<double>&,
std::vector<double>&, double, MatrixError&);
        std::vector<double> Gauss(Matrix<double>, std::vector<double>&,
double, MatrixError&);
    }

    void Problem1();
}
```

a3p1.cpp:

```
#include "a3p1.h"
#include <iostream>
#include <iomanip>
#include <cmath>

using namespace assign3::p1;

void assign3::p1::Substitute(
    Matrix<double> &a,
    std::vector<double> &b,
    std::vector<double> &x)
{
    x[a.Rows - 1] = b[a.Rows - 1] / a[a.Rows - 1][a.Cols - 1];
    for (int i = a.Rows - 2; i > -1; --i) {
        double sum = 0;
        for (int j = i + 1; j < a.Rows; ++j) {
            sum += a[i][j] * x[j];
        }
        x[i] = (b[i] - sum) / a[i][i];
    }
}
```

PROBLEM [1]. Solve problem 9.18 (p. 273) in the Chapra & Canale textbook -- write the required program in your favorite computer language, and show your solution and your code.

Output:

The result is: [1, 1, 1]


```

void assign3::p1::Pivot(
    Matrix<double> &a,
    std::vector<double> &b,
    std::vector<double> &s,
    int k)
{
    int p = k;
    double temp;
    double max = abs(a[k][k] / s[k]);
    for (int i = k + 1; i < a.Rows; ++i) {
        temp = abs(a[i][k] / s[i]);
        if (temp > max) {
            max = temp;
            p = i;
        }
    }

    if (p != k) {
        for (int j = k; j < a.Rows; ++j) {
            temp = a[p][j];
            a[p][j] = a[k][j];
            a[k][j] = temp;
        }

        temp = b[p];
        b[p] = b[k];
        b[k] = temp;

        temp = s[p];
        s[p] = s[k];
        s[k] = temp;
    }
}

void assign3::p1::Eliminate(
    Matrix<double> &a,
    std::vector<double> &b,
    std::vector<double> &s,
    double tolerance,
    MatrixError &error)
{
    int k = 0;
    for (; k < a.Rows - 1; ++k) {
        Pivot(a, b, s, k);
        if (abs(a[k][k] / s[k]) < tolerance) {
            // Make sure the diagonals are all non-zero
            error = MatrixError::SINGULAR;
            return;
        }

        for (int i = k + 1; i < a.Rows; ++i) {
            double factor = a[i][k] / a[k][k];
            for (int j = k + 1; j < a.Rows; ++j) {
                a[i][j] -= factor * a[k][j];
            }
            b[i] -= factor * b[k];
        }
    }
}

```

```

    }
}

// Not sure what exactly this is checking
if (abs(a[a.Rows - 1][a.Rows - 1]) < tolerance) {
    error = MatrixError::SINGULAR;
}
}

std::vector<double> assign3::p1::Gauss(
    Matrix<double> a,
    std::vector<double> &b,
    double tolerance,
    MatrixError& error)
{
    if (a.Rows != a.Cols || a.Rows != b.size()) {
        error = MatrixError::INV_DIM;
        return b;
    }

    double temp;
    std::vector<double> x(a.Rows), s(a.Rows);

    // Determine the largest coefficient of a in a given column
    for (int i = 0; i < a.Rows; ++i) {
        s[i] = 0;
        for (int j = 0; j < a.Cols; ++j) {
            temp = abs(a[i][j]);
            if (temp > s[j]) {
                s[i] = temp;
            }
        }
    }

    // I have no idea what this does anymore; it's someone else's code
    Eliminate(a, b, s, tolerance, error);
    if (error == MatrixError::GOOD) {
        Substitute(a, b, x);
    }

    return x;
}

void assign3::Problem1() {
    Matrix<double> a{
        {1, 2, -1},
        {5, 2, 2},
        {-3, 5, -1},
    };
    std::vector<double> b{2, 9, 1};
    std::vector<double> x;
    MatrixError error = MatrixError::GOOD;

    x = Gauss(a, b, .0001, error);

    // Output the result of Gaussian elimination with partial pivoting
    if (error == MatrixError::GOOD) {

```

```
        std::cout << "The result is: " << x << std::endl;
    } else if (error == MatrixError::INV_DIM) {
        std::cout << "The matrix a and the solution vector b have invalid
dimensions..." << std::endl;
    } else if (error == MatrixError::SINGULAR) {
        std::cout << "The matrix a is singular, and ax = b has no
solution..." << std::endl;
    } else {
        std::cout << "An unkown error has occured..." << std::endl;
    }
}
```

Problem 2

9.18 Develop, debug, and test a program in either a high-level language or macro language of your choice to solve a system of equations with Gauss elimination with partial pivoting. Base the program on the pseudocode from Fig. 9.6. Test the program using the following system (which has an answer of $x_1 = x_2 = x_3 = 1$),

$$\begin{aligned}x_1 + 2x_2 - x_3 &= 2 \\ 5x_1 + 2x_2 + 2x_3 &= 9 \\ -3x_1 + 5x_2 - x_3 &= 1\end{aligned}$$

matlab:

```
>> a = [  
    1,2,-1  
    5,2,2  
   -3,5,-1  
];  
>> b = [  
    2  
    9  
    1  
];  
>> inv(a)*b
```

ans =

```
1.0000  
1.0000  
1.0000
```

```
>>
```

Oh look, it's the same 😊

PROBLEM [2]. Solve the system of problem 9.18 (p. 273) in the Chapra & Canale textbook using matrices, the inverse matrix, and matrix multiplication in SCILAB, MATLAB, Excel, SMath Studio, or Maxima. Compare your results with those of problem [1]. They should be the same. Recall, the matrix equation is $[A]\{x\} = \{b\}$, so $\{x\} = \text{inv}(A)*\{b\}$.

Problem 3

9.18 Develop, debug, and test a program in either a high-level language or macro language of your choice to solve a system of equations with Gauss elimination with partial pivoting. Base the program on the pseudocode from Fig. 9.6. Test the program using the following system (which has an answer of $x_1 = x_2 = x_3 = 1$).

$$\begin{aligned}x_1 + 2x_2 - x_3 &= 2 \\ 5x_1 + 2x_2 + 2x_3 &= 9 \\ -3x_1 + 5x_2 - x_3 &= 1\end{aligned}$$

```
#include <vector>
#include "assign3.h"
#include "../shared/matrix.h"

namespace assign3 {
    namespace p3 {
        void Substitute(Matrix<double>&, std::vector<double>&,
std::vector<double>&, std::vector<int>&);
        void Pivot(Matrix<double>&, std::vector<double>&, std::vector<int>&,
int);
        void Decompose(Matrix<double>&, std::vector<double>&,
std::vector<int>&, double, MatrixError&);
        std::vector<double> LuDecomp(Matrix<double>, std::vector<double>&,
double, MatrixError&);
    }

    void Problem3();
}
```

a3p3.cpp:

```
#include "a3p3.h"
#include <iostream>
#include <iomanip>
#include <cmath>

#include "../shared/matrix.h"

using namespace assign3::p3;

void assign3::p3::Substitute(
    Matrix<double> &a,
    std::vector<double> &b,
    std::vector<double> &x,
    std::vector<int> &o)
{
    for (int i = 1; i < a.Rows; ++i) {
        double sum = b[o[i]];
        for (int j = 0; j <= i - 1; ++j) {
            sum -= a[o[i]][j] * b[o[j]];
        }
        b[o[i]] = sum;
    }
}
```

10.18 Develop a user-friendly program for LU decomposition based on the pseudocode from Fig. 10.2.

PROBLE

M [3]. Write the code for solving Problem 10.18, and solve the linear system of Problem [1] using this code.

Output: **The result is: [1, 1, 1]**

a3p3.h:

`#pragma once`

```

x[a.Rows - 1] = b[o[a.Rows - 1]] / a[o[a.Rows - 1]][a.Rows - 1];
for (int i = a.Rows - 2; i >= 0; --i) {
    double sum = 0;
    for (int j = i + 1; j < a.Rows; ++j) {
        sum += a[o[i]][j] * x[j];
    }
    x[i] = (b[o[i]] - sum) / a[o[i]][i];
}
}

void assign3::p3::Pivot(
    Matrix<double> &a,
    std::vector<double> &s,
    std::vector<int> &o,
    int k)
{
    int p = k;
    double temp;
    double max = abs(a[o[k]][k] / s[o[k]]);
    for (int i = k + 1; i < a.Rows; ++i) {
        temp = abs(a[o[i]][k] / s[o[i]]);
        if (temp > max) {
            max = temp;
            p = i;
        }
    }

    int t_int = o[p];
    o[p] = o[k];
    o[k] = t_int;
}

void assign3::p3::Decompose(
    Matrix<double> &a,
    std::vector<double> &s,
    std::vector<int> &o,
    double tolerance,
    MatrixError &error)
{
    for (int i = 0; i < a.Rows; ++i) {
        double temp;
        o[i] = i;
        s[i] = abs(a[i][0]);
        for (int j = 1; j < a.Rows; ++j) {
            temp = abs(a[i][j]);
            if (temp > s[i]) {
                s[i] = temp;
            }
        }
    }

    int k = 0;
    for (; k < a.Rows - 1; ++k) {
        Pivot(a, s, o, k);
        if (abs(a[o[k]][k] / s[o[k]]) < tolerance) {
            error = MatrixError::SINGULAR;
            // print a[o[k]][k] / s[o[k]]

```

```

        return;
    }

    for (int i = k + 1; i < a.Rows; ++i) {
        double factor = a[o[i]][k] / a[o[k]][k];
        a[o[i]][k] = factor;
        for (int j = k + 1; j < a.Rows; ++j) {
            a[o[i]][j] -= factor * a[o[k]][j];
        }
    }
}

// Not sure what exactly this is checking
if (abs(a[o[k]][k] / s[o[k]]) < tolerance) {
    error = MatrixError::SINGULAR;
    // print a[o[k]][k] / s[o[k]]
}
}

std::vector<double> assign3::p3::LuDecomp(
    Matrix<double> a,
    std::vector<double> &b,
    double tolerance,
    MatrixError& error)
{
    if (a.Rows != a.Cols || a.Rows != b.size()) {
        error = MatrixError::INV_DIM;
        return b;
    }

    std::vector<double> x(a.Rows), s(a.Rows);
    std::vector<int> o(a.Rows);

    // I have no idea what this does anymore; it's someone else's code
    Decompose(a, s, o, tolerance, error);
    if (error == MatrixError::GOOD) {
        Substitute(a, b, x, o);
    }

    return x;
}

void assign3::Problem3() {
    Matrix<double> a{
        {1, 2, -1},
        {5, 2, 2},
        {-3, 5, -1},
    };
    std::vector<double> b{2, 9, 1};
    std::vector<double> x;
    MatrixError error = MatrixError::GOOD;

    x = LuDecomp(a, b, .0001, error);

    // Output the result of LU Decomposition
    if (error == MatrixError::GOOD) {
        std::cout << "The result is: " << x << std::endl;
    }
}

```

```
    } else if (error == MatrixError::INV_DIM) {
        std::cout << "The matrix a and the solution vector b have invalid
dimensions..." << std::endl;
    } else if (error == MatrixError::SINGULAR) {
        std::cout << "The matrix a is singular, and ax = b has no
solution..." << std::endl;
    } else {
        std::cout << "An unkown error has occured..." << std::endl;
    }
}
```


Problem 4

PROBLEM [4]. Write the code for calculating the inverse of square matrix (see Problem 10.19), and find the inverse matrix for the matrix of coefficients of Problem [1].

- **How to modify the pseudocode of Figure 10.2 to calculate an inverse:**
 - Start with the pseudocode of Figure 10.2
 - Replace the segment of the pseudocode for *SUB Ludecomp* starting with the line *Call Decompose(a, n, tol, o, s, er)* up to the line immediately before *END Ludecomp* with the pseudocode of Figure 10.5
 - Change the first line of *Ludecomp*, i.e., the line *SUB Ludecomp(a, b, n, tol, x, er)* to *SUB MatrixInverse(a, ai, n, tol, er)* where *ai* is the inverse matrix (a matrix of dimensions $n \times n$)
- **What your main program should do:**
 - Read matrix **A**
 - Copy matrix **A** to **AA**
 - Call *SUB MatrixInverse(AA, AI, n, tol, er)*
 - Output inverse matrix **AI**
 - Calculate matrix **B** = **A*****AI**
 - Output matrix **B** (it should be the $n \times n$ identity matrix)

Output:

```
ai:
[0.266667, 0.0666667, -0.133333]
[0.0222222, 0.0888889, 0.155556]
[-0.688889, 0.244444, 0.177778]

b = a * ai:
[1, -5.55112e-017, -2.77556e-017]
[0, 1, -5.55112e-017]
[0, 2.77556e-017, 1]
```

a3p4.h:

```
#pragma once
#include <vector>
#include "assign3.h"
#include "../shared/matrix.h"

namespace assign3 {
    namespace p4 {
        Matrix<double> MatrixInverse(Matrix<double>, double, MatrixError&);
    }

    void Problem4();
}
```

a3p4.cpp:

```
#include "a3p4.h"
#include <iostream>
#include <iomanip>
#include <cmath>

#include "../shared/matrix.h"

// No need to duplicate code
#include "a3p3.h"

using namespace assign3::p4;

Matrix<double> assign3::p4::MatrixInverse(
    Matrix<double> a, // copy by value
    double tolerance,
    MatrixError& error)
{
    if (a.Rows != a.Cols) {
        error = MatrixError::INV_DIM;
```

```

        return a;
    }

    int n = a.Rows;
    Matrix<double> ai(a);
    std::vector<double> b(n), x(n), s(n);
    std::vector<int> o(n);

    // I have no idea what this does anymore; it's someone else's code
    assign3::p3::Decompose(a, s, o, tolerance, error);
    if (error == MatrixError::GOOD) {
        for (int i = 0; i < n; ++i) {
            for (int j = 0; j < n; ++j) {
                b[j] = i == j ? 1 : 0;
            }
            assign3::p3::Substitute(a, b, x, o);
            for (int j = 0; j < n; ++j) {
                ai[j][i] = x[j];
            }
        }
    }

    return ai;
}

void assign3::Problem4() {
    Matrix<double> a{
        {1, 2, -1},
        {5, 2, 2},
        {-3, 5, -1},
    };
    MatrixError error = MatrixError::GOOD;

    Matrix<double> ai = MatrixInverse(a, .0001, error);
    Matrix<double> b = a * ai;

    // Output the inverse and product of the two matrices (identity)
    if (error == MatrixError::GOOD) {
        std::cout << "ai: " << ai << "b = a * ai:" << b;
    } else if (error == MatrixError::INV_DIM) {
        std::cout << "The matrix a and the solution vector b have invalid
dimensions..." << std::endl;
    } else if (error == MatrixError::SINGULAR) {
        std::cout << "The matrix a is singular, and ax = b has no
solution..." << std::endl;
    } else {
        std::cout << "An unkown error has occured..." << std::endl;
    }
}

```