

3-dimensional Boolean functions

Question 1

How many 3-dimensional Boolean functions are there?

256

Because $2^8 = 256$

Count the number of symmetries of 3-dimensional Boolean functions that map 4 of the possible input patterns to 1

One symmetry with a square.

One with deux points side to side and the others two to the other side.

And 4 for 3 points on the same side and the other point on a different location.

So answer is : 6

How many linearly separable 3-dimensional Boolean functions are there?

- $k = 0|8$ and $k = 8|0$
 - 2 patterns linearly separable
- $k = 1|7$ and $k = 7|1$
 - 16 patterns linearly separable
- $k = 2|6$ and $k = 6|2$
 - 24 patterns linearly separable
- $k = 3|5$ and $k = 5|3$
 - 48 patterns linearly separable
- $k = 4|4$
 - 6 patterns and 8 patterns = 14 patterns linearly separable

The total is **104**