

$$Q2) U(a,b) = \begin{cases} \frac{1}{b-a} & a \leq x \leq b \\ 0 & \text{otherwise} \end{cases}$$

$$\mu = \int_{-\infty}^{\infty} x U(x) dx \Rightarrow \mu = \int_a^b \frac{1}{(b-a)} x dx = \frac{b+a}{2}$$

$$\sigma^2 = \left(\int_{-\infty}^{\infty} x^2 U(x) dx - \mu^2 \right) \Rightarrow$$

$$\sigma^2 = E(x^2) - (E(x))^2 = \frac{1}{b-a} \int_a^b x^2 dx - \left(\frac{b+a}{2} \right)^2 = \frac{b^3 - a^3}{3(b-a)} - \left(\frac{b+a}{2} \right)^2 = \frac{(b-a)^2}{12}$$