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# Baba and a Hard Problem

Input file:            `standard input`  
Output file:          `standard output`  
Time limit:          2 seconds  
Memory limit:        256 megabytes

Baba, with his teammates, was giving ASC (Andrew Stankevich Contest) as a part of their regular practice sessions. They came across this really hard problem which none of them had any clue how to solve. The problem was as follows:

Given  $N$  boys and  $N$  girls in a class, each boy and a girl has an IQ level. The IQ of the  $i$ 'th boy is given by  $b_i$  and of the  $i$ 'th girl is given by  $g_i$ . We need to create  $N$  pairs of boys and girls for an upcoming quiz such that the following conditions are satisfied.

- Every boy must be matched with exactly one girl
- Every girl must be matched with exactly one boy
- Let  $M_i$  represent the index of the girl matched with the  $i$ 'th boy. We define a function  $f$  as follows :

$$f = \sum_{i=1}^n |b_i - g_{M_i}|$$

What is the minimum value the function  $f$  can attain over all  $n!$  possible matchings?

Baba knows this problem can be solved using Min-Cost Max Bipartite Matching but the complexity of that algorithm is  $O(N^3)$  and hence would time out. Since ASC contests do not have any editorials available, they come to you for help. Can you help them come up with a faster solution that solves this problem ?

## Input

First line will contain single integer  $t$  ( $1 \leq t \leq 5 * 10^5$ ) denoting the number of test cases.

Next  $3 * t$  lines describe the test cases in the following format.

First line contains a single integer  $N$  ( $1 \leq N \leq 5 * 10^5$ ) denoting number of boys and girls in the class.

The next line contains  $N$  space separated integers, where the  $i$ 'th integer denotes the value of  $b_i$  ( $1 \leq b_i \leq 10^9$ ).

The next line contains  $N$  space separated integers, where the  $i$ 'th integer denotes the value of  $g_i$  ( $1 \leq g_i \leq 10^9$ ).

## Output

For every test case, output a single integer, the minimum value that the function  $f$  can attain.

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## Example

standard input	standard output
3	12
3	14
2 3 3	30
11 5 4	
5	
15 3 3 2 6	
8 3 7 13 8	
5	
3 2 4 2 10	
11 7 14 9 10	

## Note

It is not necessary that each array has only distinct integers. Sum of  $n$  over all test files  $\leq 5 * 10^5$ .  $M$  represents an  $n$  length permutation of numbers  $1, 2, 3..n$  such that  $M_i$  corresponds to the index of the girl matched with  $i$ 'th boy. It is easy to see that the total number of matchings = total number of permutations  $M$  possible =  $n!$