



**CSE251**  
**Basics of Computer Graphics**  
**Module: Visibility and Culling Module**

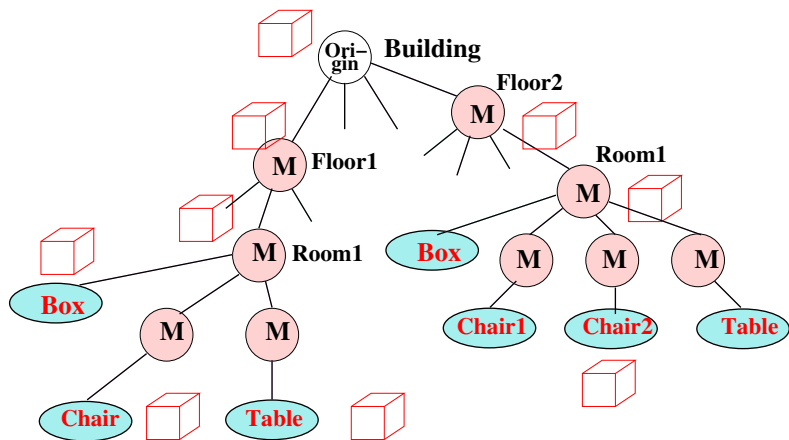
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# Visible Surface Determination (VSD)

- ▶ Multiple object points can project to the same image pixel in 3D. Which one gives the colour to the pixel?
- ▶ **Visible line/surface determination** or **Hidden line/surface elimination**.
- ▶ Consider objects to be drawn or pixels to be painted.
- ▶ Need to analyze the scene from the camera.
- ▶ We will look at 3 types: **Broad or Object** level, **Medium or Primitive** level, and **Fine or Pixel** level

# Good Hierarchical Model



# Hierarchical Model: Properties

- ▶ Leaf level: objects with geometry/shape, like table/chair
  - ▶ **Bounding Box** encloses the object completely
- ▶ Intermediate level: Create a bounding box that encloses the child nodes completely
- ▶ Bounding box of a node covers geometry below it totally!
  - ▶ Root bounding box covers the whole scene!
- ▶ Question: If cameras **View Frustum does not intersect a bounding box: .....**

# Hierarchical Model: Properties

- ▶ Leaf level: objects with geometry/shape, like table/chair
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- ▶ Bounding box of a node covers geometry below it totally!
  - ▶ Root bounding box covers the whole scene!
- ▶ Observation: If View Frustum doesn't intersect the BBox,  
**no object in it can be visible to the camera!**

# View Frustum Culling

- ▶ Eliminate objects that are outside the view volume.
- ▶ Large parts of the scene will be eliminated this way.

Compare bounding volume of `node` with view volume

If intersection is null, eliminate tree from root

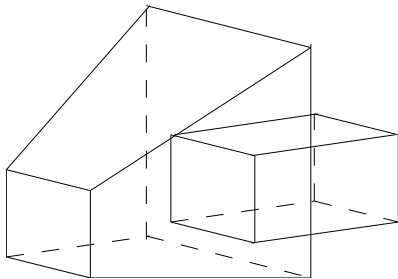
If volume contained in frustum, render without clipping

Else, recursively check for each child of `node` till leaf

- ▶ Object hierarchy **really** helps. Whole campus, each building, each floor, each room, etc., in the hierarchy.

# Box-Frustum Intersection

- ▶ Orthographic: Intersection of two boxes. Simultaneous X-Y-Z overlaps.
- ▶ Perspective: Clip against 6 planes of the frustum.
- ▶ **AABB**: Axis-Aligned Bounding Box  
**OBB**: Oriented Bounding Box
- ▶ AABB: Easy to find the box, but not efficient  
OBB: More accurate, but more computation



# AABB vs OBB

- ▶ Calculating the AABB of a model: How?



# AABB vs OBB

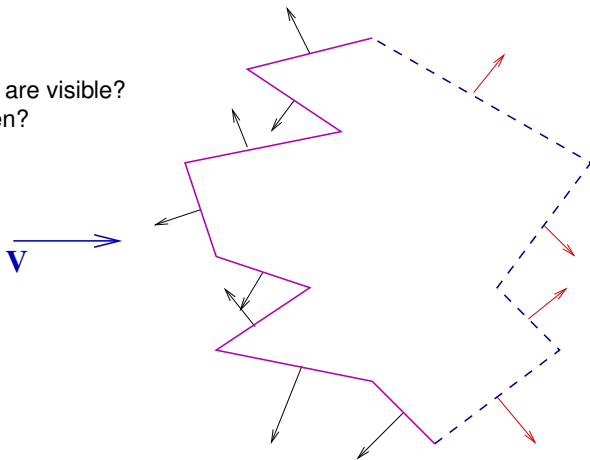
- ▶ Calculating the AABB of a model: How?
- ▶ In ORC, find separately the minimum and maximum values of X, Y, and Z
- ▶ What are the plusses and minuses of AABB?
- ▶ How can we calculate the OBB of a given model?
  - ▶ Find the smallest bounding volume: somewhat involved
- ▶ Find the major/minor axes for the shape and fit a box

# View Frustum Culling: VFC

- ▶ Efficient frustum-box intersection methods exist
- ▶ Large portions of the scene eliminated from consideration
- ▶ Note: **Drawing the discarded objects will still yield the correct picture!**
- ▶ VFC is primarily for speed, reducing the number of objects to be drawn
- ▶ This is done before drawing, at the start of the pipeline

# Viewing a Solid Object

- ▶ Which polygons are visible?  
Which are hidden?



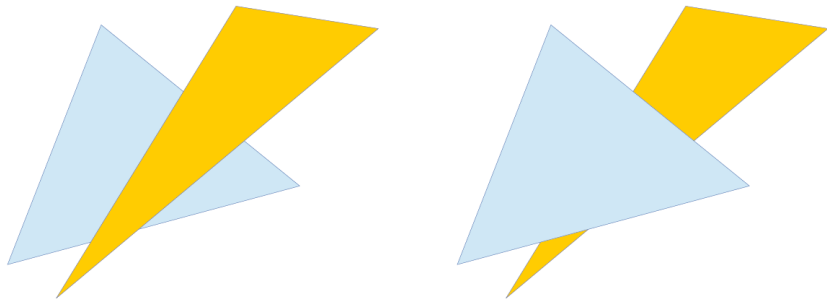
# Back-Face Culling

- ▶ Only the front side can be seen of solid, opaque objects.
- ▶ If surface normals point out of the object, polygons with normals pointing away from the viewer cannot be seen.
- ▶ If  $\mathbf{v} \cdot \mathbf{n} < 0$ , draw. Else discard.  $\mathbf{v}$  is a vector from CoP to any point on the polygon and  $\mathbf{n}$  the surface normal.
- ▶ After projection normalizing, DoP is  $[0 \ 0 \ -1]^T$ . Eliminate polygons with negative  $z$  component in the normal vector (in RHS).
- ▶ Half the polygons eliminated on the average.
- ▶ If there is only one object, no other VSD necessary.

# Culling vs Visibility

- ▶ View Frustum Culling (VFC): Identify and ignore entire objects outside the current view volume.
- ▶ Back Face Culling (BFC): Identify and ignore triangles facing away.
- ▶ Eliminating portions that are guaranteed to be not visible. Improves efficiency or speed.
- ▶ Visibility between triangles inside the view frustum involve their relative arrangement.
  - ▶ **Pixel-level visibility needs to be determined.**

# Which of the two cases?



- ▶ Parts of one primitive is in front. Need correct picture
- ▶ Back-to-front drawing gives correct picture, when possible

# Object-Precision Algorithm

```
for each object in the world {  
    Determine unobstructed parts of the object  
    Draw those parts with appropriate colours  
}
```

- ▶ Complexity depends on the number of objects.
- ▶ If the image size changes, only the drawing step needs to be redone.
- ▶ Works in the original continuous object space.

# Image-Precision Algorithm

```
for each pixel in the image {  
    Determine closest object in the direction of projector  
    Draw the pixel with appropriate colours  
}
```

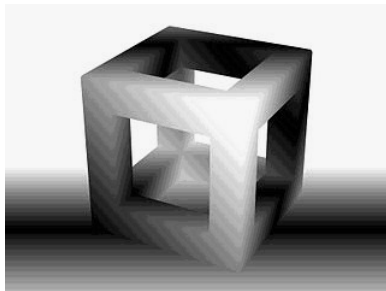
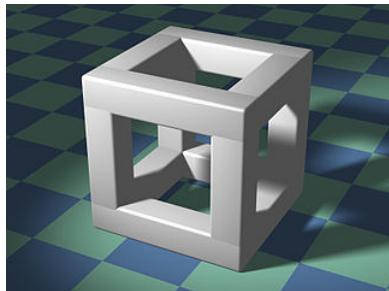
- ▶ Works in the discrete image space.
- ▶ Complexity depends on the number of pixels.
- ▶ A natural choice for raster graphics.
- ▶ Image resizing involves repeating the entire work.



# Z-buffer or Depth-buffer Algorithm

- ▶ An image-precision algorithm that needs a z-buffer parallel to the frame buffer.
- ▶  $z$  values after the normalizing transformation is stored into the z-buffer along with colour info to the frame buffer. We have  $0 \geq z \geq -1$ .
- ▶ Larger  $z$  implies a closer 3D point in any direction
- ▶ Write to frame buffer and z-buffer only when the  $z$  value is larger than previously stored value.
- ▶ **FrameBuffer + DepthBuffer**

# Colour and Depth



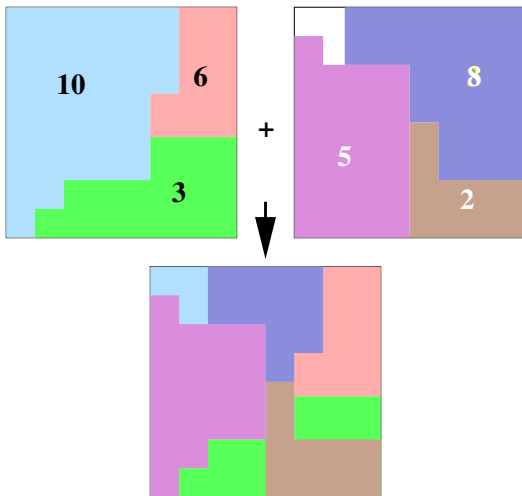
- ▶ `Color[i, j]` holds the colour and `Depth[i, j]` the distance (or z-value) of the **nearest** object encountered in the direction of pixel  $(i, j)$  at *any point of time*, during the rendering

# Pseudocode

```
for  $0 \leq y \leq Y_{\max}$   
    for  $0 \leq x \leq X_{\max}$   
        WritePixel (x, y, bgnd_colour)  
        WriteZ (x, y, -1)    // Farthest value
```

```
for each polygon  
    for each pixel in polygon's projection  
        pz = polygon's z-value at pixel (x, y)  
        if (pz > ReadZ(x, y))  
            WriteZ()  
            WritePixel()
```

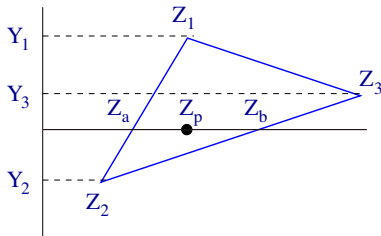
# Depth Buffer



# Computing $z$ for Interior Points

- ▶ Exploit coherence in depth values over the plane to compute interior  $z$  values given the vertex values.
- ▶  $z_a = z_1 + \dots$   
 $z_b = ??$   $z_p = ???$
- ▶ When  $x$  or  $y$  increments by 1 along a side or a scan line,  $z$  changes by a constant  $\Delta z$ .

$\Delta z = ??$  along edge 12

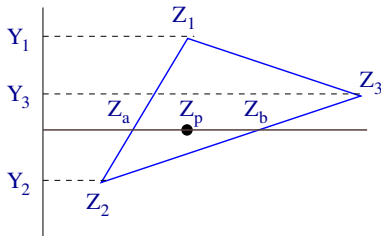


# Computing $z$ for Interior Points

- ▶  $z_a = z_1 + (z_2 - z_1) \frac{(y_a - y_1)}{(y_2 - y_1)}$   
 $z_b = z_2 + (z_3 - z_2) \frac{(y_b - y_2)}{(y_3 - y_2)}$   
 $z_p = z_a + (z_b - z_a) \frac{(x_p - x_a)}{(x_b - x_a)}$
- ▶ When  $x$  or  $y$  increments along a side or a scan line,  $z$  changes by a constant  $\Delta z$

$$\Delta z = (z_2 - z_1) / (y_2 - y_1) \text{ along edge 12}$$

$$\Delta z = (z_b - z_a) / (x_b - x_a) \text{ along scan line}$$



# List Priority Algorithms

- ▶ Reorder objects such that the correct picture results if you draw them in that order. If objects do not overlap in  $z$ , draw them from back to front.
- ▶ Objects may need splitting if no unique ordering exists.
- ▶ **Needs expensive sorting/reordering every frame!!**
- ▶ Ordering and splitting polygons: Object-precision operation.
- ▶ Overwriting farther points while scan conversion: Image-precision operation.

# A Difficult Case for Ordering

