

$$H = -p \ln(p) - (1-p) \ln(1-p) =$$

$$= -\frac{1+\Delta}{2} \ln\left(\frac{1+\Delta}{2}\right) - \left(\frac{1-\Delta}{2}\right) \ln\left(\frac{1-\Delta}{2}\right) =$$

$$\frac{1}{2} \left(\ln(4) - (1-\Delta) \ln(1-\Delta) - (1+\Delta) \ln(1+\Delta) \right) =$$

$$\frac{1}{2} \left(\ln(4) - (1-\Delta) \sum_{n=1}^{\infty} \frac{(-1)^{n+1} (-\Delta)^n}{n} - (1+\Delta) \sum_{n=1}^{\infty} \frac{(-1)^{n+1} \Delta^n}{n} \right) =$$

$$\frac{1}{2} \left(\ln(4) - \sum_{n=1}^{\infty} \frac{(-1)^{n+1} (-\Delta)^n}{n} + \sum_{n=1}^{\infty} \frac{(-1)^{n+1} (-\Delta)^n \Delta}{n} - \sum_{n=1}^{\infty} \frac{(-1)^{n+1} \Delta^n}{n} - \sum_{n=1}^{\infty} \frac{(-1)^{n+1} \Delta^{n+1}}{n} \right) =$$

$$\frac{1}{2} \left(\ln(4) + \sum_{n=1}^{\infty} \frac{(\Delta)^{2n}}{n} + \sum_{n=1}^{\infty} \frac{(-1)^{n+1} (-\Delta)^n \Delta}{n} - \sum_{n=1}^{\infty} \frac{(-1)^{n+1} \Delta^{n+1}}{n} \right) =$$

$$\frac{1}{2} \left(\ln(4) + \sum_{n=1}^{\infty} \frac{(\Delta)^{2n}}{n} - 2 \sum_{n=1}^{\infty} \frac{\Delta^{2n}}{(2n-1)} \right) =$$

$$\ln(2) \left(1 - \frac{1}{\ln(4)} \sum_{n=1}^{\infty} \frac{(\Delta)^{2n}}{n(2n-1)} \right)$$