

$$\begin{aligned}
 \frac{\text{pr}(H_1 | D_2, D_1)}{\text{pr}(H_2 | D_2, D_1)} &= \\
 \frac{\text{pr}(H_1 | D_2 \cap D_1)}{\text{pr}(H_2 | D_2 \cap D_1)} &= \frac{\text{pr}(H_1 | D_2 \cap D_1)}{\text{pr}(H_2 | D_2 \cap D_1)} = \frac{\text{pr}(D_2 \cap D_1 | H_1) * \text{pr}(H_1)}{\text{pr}(D_2 \cap D_1)} * \frac{\text{pr}(D_2 \cap D_1)}{\text{pr}(D_2 \cap D_1 | H_2) * \text{pr}(H_2)} = \\
 \frac{\text{pr}(D_2 \cap D_1 | H_1)}{\text{pr}(D_2 \cap D_1 | H_2)} * \frac{\text{pr}(H_1)}{\text{pr}(H_2)} &= \frac{\text{pr}(D_2 | H_1) P(D_1 | H_1)}{\text{pr}(D_2 | H_2) P(D_1 | H_2)} * \frac{\text{pr}(H_1)}{\text{pr}(H_2)}
 \end{aligned}$$