Вариант 12

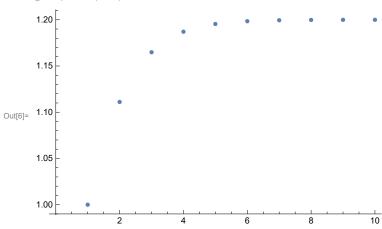
a)
$$\lim_{n\to\infty} \frac{1+\frac{1}{3}+\dots+\frac{1}{3^n}}{1+\frac{1}{5}+\dots+\frac{1}{5^n}} = \lim_{n\to\infty} \frac{\frac{1-\left(\frac{1}{3}\right)^n}{1-\frac{1}{3}}}{\frac{1-\left(\frac{1}{5}\right)^n}{1-\frac{1}{5}}} = \frac{4/5}{2/3} = \frac{6}{5}$$

In[5]:= data = Table
$$\left[\frac{\frac{1 - \left(\frac{1}{3}\right)^n}{1 - \frac{1}{3}}}{\frac{1}{2} \left(\frac{1}{5}\right)^n}, \{n, 1, 10\} \right];$$

$$\frac{1}{1 - \frac{1}{5}}$$

ListPlot[data]

диаграмма разброса данных



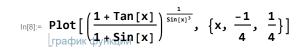
a)
$$\lim_{x\to 0} \left(\frac{1+tgx}{1+\sin x}\right)^{\frac{1}{\sin^3 x}} = \lim_{x\to 0} e^{\frac{1}{\sin^3 x} \ln \left(\frac{1+tgx}{1+\sin x}\right)} =$$

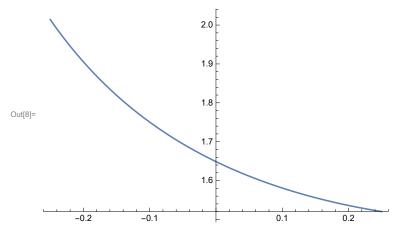
$$\lim_{x\to 0} \ \ e^{\frac{1}{\sin^3 x} \star \ln\left(1 + \frac{1 + \operatorname{tg} x}{1 + \sin x} - 1\right)} = \lim_{x\to 0} \ \ e^{\frac{1}{x^3} \star \ln\left(1 + \frac{\sin x \left(1 - \cos x\right)}{\cos x \left(1 + \sin x\right)}\right)} = \lim_{x\to 0} \ \ e^{\frac{1}{x^3} \star \frac{\sin x \left(1 - \cos x\right)}{\cos x \left(1 + \sin x\right)}} = \lim_{x\to 0} \ \ e^{\frac{1}{x^3} \star \frac{x \times 2}{2 \cos x \left(1 + \sin x\right)}} = e^{1/2}$$

In[9]:= $e^{1/2}$ // N

численное приближение

Out[9]= 1.64872





B)
$$y = ctg \pi x + arccos 2^x$$

$$\sin \pi x \neq 0$$
 $|2^x| \leq 1$

$$\pi x \neq \frac{\pi}{2} + \pi k$$
, $k \in \mathbb{Z}$ $\forall x \leq 0$

$$x \in \left(\frac{-1}{2}; 0\right] \cup \left(\bigcup_{k=0}^{\infty} \left(-\frac{1}{2} - k - 1; -\frac{1}{2} - k\right)\right)$$