$$\begin{split} \Gamma^0_{00} &= \frac{(r\left(a^2 + r^2 - 2r\right) + (1 - r)\left(a^2 \cos^2\left(\theta\right) + r^2\right))\left(1.0a^2 + 1.0r^2 - 2.0r\right)}{\left(a^2 \cos^2\left(\theta\right) + r^2\right)\left(a^2 + r^2 - 2r\right)^2} \\ \Gamma^0_{01} &= -\frac{0.5a^2 \sin\left(2\theta\right)}{a^2 \cos^2\left(\theta\right) + r^2} \\ \Gamma^0_{02} &= 0 \\ \Gamma^0_{10} &= -\frac{0.5a^2 \sin\left(2\theta\right)}{a^2 \cos^2\left(\theta\right) + r^2} \\ \Gamma^0_{11} &= -\frac{1.0r\left(a^2 \sin^2\left(\theta\right) - 2r\right)}{a^2 \cos^2\left(\theta\right) + r^2} \\ \Gamma^0_{12} &= 0 \\ \Gamma^0_{13} &= 0 \\ \Gamma^0_{20} &= 0 \\ \Gamma^0_{21} &= 0 \\ \Gamma^0_{22} &= \frac{1.0\left(r\left(a^2 \cos^2\left(\theta\right) + r^2\right)^3 + \left(-a^2 - r^2 + 2r\right)\left(-2a^2r^2 \sin^2\left(\theta\right) + a^2\left(a^2 \cos^2\left(\theta\right) + r^2\right)\sin^2\left(\theta\right) - a^2 \cos^2\left(\theta\right) + r^2\right)}{\left(a^2 \cos^2\left(\theta\right) + r^2\right)^3} \\ \Gamma^0_{22} &= \frac{1.0a\left(a^2 \cos^2\left(\theta\right) - r^2\right)\left(a^2 + r^2 - 2r\right)\sin^2\left(\theta\right)}{\left(a^2 \cos^2\left(\theta\right) + r^2\right)^3} \\ \Gamma^0_{30} &= 0 \\ \Gamma^0_{31} &= 0 \\ \Gamma^0_{32} &= \frac{1.0a\left(a^2 \cos^2\left(\theta\right) - r^2\right)\left(a^2 + r^2 - 2r\right)\sin^2\left(\theta\right)}{\left(a^2 \cos^2\left(\theta\right) + r^2\right)^3} \\ \Gamma^0_{33} &= \frac{1.0a\left(a^2 \cos^2\left(\theta\right) - r^2\right)\left(-1.0a^2 - 1.0r^2 + 2.0r\right)}{\left(a^2 \cos^2\left(\theta\right) + r^2\right)^3} \\ \Gamma^1_{00} &= \frac{0.5a^2 \sin\left(2\theta\right)}{\left(a^2 \cos^2\left(\theta\right) + r^2\right)} \\ \Gamma^1_{01} &= -\frac{1.0a^2 \cos^2\left(\theta\right)}{r\left(a^2 \cos^2\left(\theta\right) + r^2\right)} \end{aligned}$$

$$\begin{split} \Gamma^1_{03} &= 0 \\ \Gamma^1_{03} &= 0 \\ \Gamma^1_{10} &= -\frac{1.0a^2 \cos^2(\theta)}{r(a^2 \cos^2(\theta) + r^2)} \\ \Gamma^1_{11} &= -\frac{0.5a^2 \sin{(2\theta)}}{a^2 \cos^2(\theta) + r^2} \\ \Gamma^1_{12} &= 0 \\ \Gamma^1_{13} &= 0 \\ \Gamma^1_{20} &= 0 \\ \Gamma^1_{21} &= 0 \\ \\ \Gamma^1_{22} &= -\frac{\left(2.0a^2r\left(a^2 + r^2\right)\sin^2{(\theta)} - 1.0\left(a^2 \cos^2{(\theta)} + r^2\right)^3 + 1.0\left(a^2 \cos^2{(\theta)} + r^2\right)\left(2a^2r\sin^2{(\theta)} + (a^2 \cos^2{(\theta)} + r^2)^3\right)}{\left(a^2 \cos^2{(\theta)} + r^2\right)^3} \\ \Gamma^1_{23} &= \frac{1.0ar\left(a^2 + r^2\right)\sin{(2\theta)}}{\left(a^2 \cos^2{(\theta)} + r^2\right)^3} \\ \Gamma^1_{30} &= 0 \\ \Gamma^1_{31} &= 0 \\ \Gamma^1_{32} &= \frac{1.0ar\left(a^2 + r^2\right)\sin{(2\theta)}}{\left(a^2 \cos^2{(\theta)} + r^2\right)^3} \\ \Gamma^1_{33} &= -\frac{1.0a^2r\sin{(2\theta)}}{\left(a^2 \cos^2{(\theta)} + r^2\right)^3} \\ \Gamma^2_{00} &= 0 \\ \Gamma^2_{01} &= 0 \\ \Gamma^2_{02} &= \frac{a^2\left(-1.0a^4\cos^4{(\theta)} - 2.0a^2r^2\cos^2{(\theta)} + 0.125a^2r\left(\cos{(4\theta)} - 1\right) + 2.0a^2r\cos^2{(\theta)} - 1.0r^4 - 3r^2\cos^2{(\theta)} + r^2\right)^2}{\left(a^2\cos^2{(\theta)} + r^2\right)^2\left(1.0a^2 + 1.0r^2 - 2.0r\right)} \\ \Gamma^2_{03} &= -\frac{1.0a\left(a^2\cos^2{(\theta)} + r^2\right)^2\left(1.0a^2 + 1.0r^2 - 2.0r\right)}{\left(a^2\cos^2{(\theta)} + r^2\right)^2\left(a^2 + r^2 - 2r\right)} \\ \Gamma^2_{10} &= 0 \\ \Gamma^2_{11} &= 0 \end{split}$$

$$\Gamma^2_{12} = \frac{2.0a^2 r \sin{(2\theta)}}{2.0a^4 \cos^4{(\theta)} + 4.0a^2 r^2 \cos^2{(\theta)} + 2.0r^4}$$

$$\Gamma^2_{13} = -\frac{2.0ar}{(a^2 \cos^2{(\theta)} + r^2)^2 \tan{(\theta)}}$$

$$\Gamma^2_{20} = \frac{a^2 \left(-1.0a^4 \cos^4{(\theta)} - 2.0a^2 r^2 \cos^2{(\theta)} + 0.125a^2 r \left(\cos{(4\theta)} - 1\right) + 2.0a^2 r \cos^2{(\theta)} - 1.0r^4 - 3r^2 \cos^2{(\theta)} + r^2\right)^2 \left(1.0a^2 + 1.0r^2 - 2.0r\right)}{r (a^2 \cos^2{(\theta)} + r^2)^2 (1.0a^2 + 1.0r^2 - 2.0r)}$$

$$\Gamma^2_{21} = \frac{2.0a^2 r \sin{(2\theta)}}{2.0a^4 \cos^4{(\theta)} + 4.0a^2 r^2 \cos^2{(\theta)} + 2.0r^4}$$

$$\Gamma^2_{22} = 0$$

$$\Gamma^2_{23} = 0$$

$$\Gamma^2_{30} = -\frac{1.0a (a^2 \cos^2{(\theta)} - r^2)}{(a^2 \cos^2{(\theta)} + r^2)^2 (a^2 + r^2 - 2r)}$$

$$\Gamma^2_{31} = -\frac{2.0ar}{(a^2 \cos^2{(\theta)} + r^2)^2 \tan{(\theta)}}$$

$$\Gamma^2_{32} = 0$$

$$\Gamma^3_{33} = 0$$

$$\Gamma^3_{00} = 0$$

$$\Gamma^3_{01} = 0$$

$$\Gamma^3_{02} = -\frac{a \left(-1.0a^4 \cos^2{(\theta)} + 1.0a^2 r^2 \cos^2{(\theta)} + 1.0a^2 r^2 + 3.0r^4 \right) \sin^2{(\theta)}}{(a^2 \cos^2{(\theta)} + r^2)^2 (1.0a^2 + 1.0r^2 - 2.0r)}$$

$$\Gamma^3_{03} = \frac{1.0 \left(a^4 \sin^2{(\theta)} - a^4 + a^2 r^2 \sin^2{(\theta)} + r^4\right)}{(a^2 \cos^2{(\theta)} + r^2)^2 (a^2 + r^2 - 2r)}$$

$$\Gamma^3_{10} = 0$$

$$\Gamma^3_{11} = 0$$

$$\Gamma^3_{12} = \frac{2.0a^3 r \sin^3{(\theta)} \cos{(\theta)}}{(a^2 \cos^2{(\theta)} + r^2)^2 \cos^2{(\theta)} + 4.0r^4}$$

$$\Gamma^3_{20} = -\frac{4.0a^2 r \sin{(2\theta)}}{4.0a^4 \cos^4{(\theta)} + 8.0a^2 r^2 \cos^2{(\theta)} + 4.0r^4}$$

$$\Gamma^3_{20} = -\frac{a \left(-1.0a^4 \cos^2{(\theta)} + 1.0a^2 r^2 \cos^2{(\theta)} + 1.0a^2 r^2 + 3.0r^4\right) \sin^2{(\theta)}}{(a^2 \cos^2{(\theta)} + r^2)^2 (1.0a^2 + 1.0r^2 - 2.0r)}$$

$$\Gamma^{3}_{21} = \frac{2.0a^{3}r\sin^{3}(\theta)\cos(\theta)}{\left(a^{2}\cos^{2}(\theta) + r^{2}\right)^{2}}$$

$$\Gamma^{3}_{22} = 0$$

$$\Gamma^{3}_{23} = 0$$

$$\Gamma^{3}_{30} = \frac{1.0\left(a^{4}\sin^{2}(\theta) - a^{4} + a^{2}r^{2}\sin^{2}(\theta) + r^{4}\right)}{\left(a^{2}\cos^{2}(\theta) + r^{2}\right)^{2}\left(a^{2} + r^{2} - 2r\right)}$$

$$\Gamma^{3}_{31} = -\frac{4.0a^{2}r\sin(2\theta)}{4.0a^{4}\cos^{4}(\theta) + 8.0a^{2}r^{2}\cos^{2}(\theta) + 4.0r^{4}}$$

$$\Gamma^{3}_{32} = 0$$

$$\Gamma^{3}_{33} = 0$$