BonusEx DM SehaLee

May 17, 2024

1 The dark matter halo of a galaxy from Illustris TNG

1.1 Seha Lee

1.1.1 Reading and plotting the data

```
[]: import numpy as np
     import matplotlib.pyplot as plt
     from matplotlib import colors
     import astropy.units as u
     import astropy.constants as const
[]: Array = np.loadtxt( "/Users/sehalee/Documents/1-Universität Potsdam/24SS/
      →CompAstro_Advanced/BonusExercise2022_DarkMatter/
      →GalaxyFromIllustrisTNG50Dark_DM_Subhalo852966.txt" )
     Pos = Array[:,0:3]
     Mass = Array[:,3]
     ####
     #The four columns are:
       # x coordinate of DM particle: in units of kpc
       # y coordinate of DM particle: in units of kpc
       # z coordinate of DM particle: in units of kpc
       # M: mass in units of Msun
     # The coordinates are chosen such that the galaxy centre is in (0,0,0)
     ####
[]: print("The shape of the array is: ", Array.shape)
     print("The first 5 rows of the array are: \n x,y,z coordinates and the mass⊔
      \rightarrow \n", Array[0:5,:])
    The shape of the array is: (2323050, 4)
    The first 5 rows of the array are:
     x,y,z coordinates and the mass
     [[ 9.64088456e-02 -6.46346007e-02 5.53424159e-02 5.38464142e+05]
     [ 1.58756977e-01 3.97111692e-02 -1.27772402e-02 5.38464142e+05]
     [ 1.81569442e-01 -2.05996550e-02 -1.74689210e-01 5.38464142e+05]
```

```
[ 1.07145711e-01 -1.99075073e-01 1.33866130e-01 5.38464142e+05]
[ 8.82361332e-02 -5.18074682e-04 4.26508561e-02 5.38464142e+05]]

[ ]: print("The maximum of each coordinates are: \n", np.max(Pos, axis=0),'\n') print("The minimum of each coordinates are: \n", np.min(Pos, axis=0),'\n') print("The size range of each coordinates are: \n", np.max(Pos, axis=0) - np.

-min(Pos, axis=0))

The maximum of each coordinates are: [348.125691 403.041627 304.655274]

The minimum of each coordinates are: [-254.37297 -287.058823 -311.243398]

The size range of each coordinates are: [602.498661 690.10045 615.898672]
```

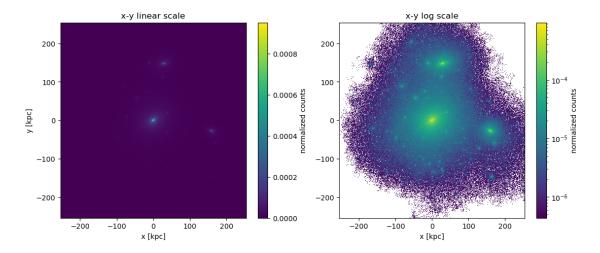
1.1.2 Task 1 Plot DM mass projections of the galaxy halo (in units of M kpc-2). Do (x, y), (x, z) and (y, z) projections. Choose a box size of ± 300 kpc. Hint: Use plt.hist2d to create the projections.

```
[]: r = int(np.abs(np.min(Pos[:,0]))) # x-axis minimum into positive integer print("The range of coordinates is from -", r, "to", r)
```

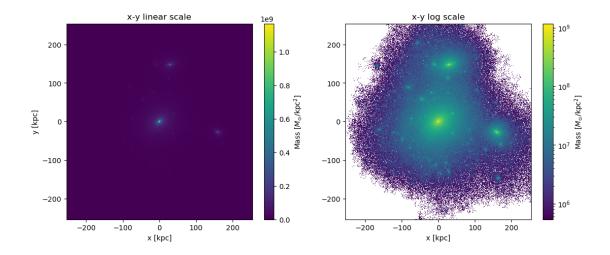
The range of coordinates is from - 254 to 254

```
[]:  # Trial 1
     #"density = True" makes normalized counts, not the physical density we_
      →want(mass per area)
     fig, axes = plt.subplots(1, 2, figsize=(13, 5))
     ranges = [[-r, r], [-r, r]]
     bins = r*2
     # linear scale
     hist1 = axes[0].hist2d(Pos[:,0], Pos[:,1], bins = bins, range= ranges,__
      weights=Mass, density=True, norm ='linear') # weights = Mass/Area
     axes[0].set_title('x-y linear scale')
     axes[0].set_xlabel('x [kpc]')
     axes[0].set_ylabel('y [kpc]')
     fig.colorbar(hist1[3], ax=axes[0], label='normalized counts')
     # log scale
     hist2 = axes[1].hist2d(Pos[:,0], Pos[:,1], bins = bins, range=ranges,_
      →weights=Mass, density=True, norm ='log')
     axes[1].set_title('x-y log scale')
     axes[1].set_xlabel('x [kpc]')
     fig.colorbar(hist2[3], ax=axes[1], label='normalized counts')
```

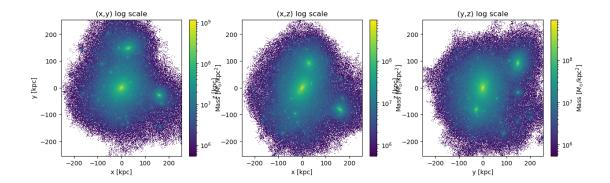
plt.show()



```
[]: # Trial 2
     # (x,y) projection of the galaxy in linear and log scale: log looks better
     fig, axes = plt.subplots(1, 2, figsize=(13, 5))
     r = int(np.abs(np.min(Pos[:,0]))) # x-axis minimum into positive integer
     ranges = [[-r, r], [-r, r]]
     bins = r*2
     # linear scale
     hist1 = axes[0].hist2d(Pos[:,0], Pos[:,1], bins = bins, range= ranges,__
      ⇒weights=Mass, density=False, norm ='linear') # weights = Mass/Area
     axes[0].set_title('x-y linear scale')
     axes[0].set_xlabel('x [kpc]')
     axes[0].set_ylabel('y [kpc]')
     fig.colorbar(hist1[3], ax=axes[0], label='Mass [M_{\odot}\/kpc$^2$]')
     # log scale
     hist2 = axes[1].hist2d(Pos[:,0], Pos[:,1], bins = bins, range=ranges,_u
      ⇔weights=Mass, density=False, norm ='log')
     axes[1].set_title('x-y log scale')
     axes[1].set xlabel('x [kpc]')
     fig.colorbar(hist2[3], ax=axes[1], label='Mass [$M_{\odot}$/kpc$^2$]')
     plt.show()
```



```
[]: ### Final Answer ###
     \# (x,y), (x,z), and (y,z) projection of the galaxy in linear and log scale
     fig, axes = plt.subplots(1, 3, figsize=(15, 4))
     r = int(np.abs(np.min(Pos[:,0])))
     ranges = [[-r, r], [-r, r]]
     bins = r*2
    hist_xy = axes[0].hist2d(Pos[:,0], Pos[:,1], bins = bins, range= ranges,__
      ⇔weights=Mass, density=False, norm ='log')
     axes[0].set_title('(x,y) log scale')
     axes[0].set_xlabel('x [kpc]')
     axes[0].set_ylabel('y [kpc]')
     fig.colorbar(hist_xy[3], ax=axes[0], label='Mass [$M_{\odot}\xspaces[0]')
     hist_xz = axes[1].hist2d(Pos[:,0], Pos[:,2], bins = bins, range= ranges,_u
      ⇔weights=Mass, density=False, norm ='log')
     axes[1].set_title('(x,z) log scale')
     axes[1].set xlabel('x [kpc]')
     axes[1].set_ylabel('z [kpc]')
     fig.colorbar(hist_xz[3], ax=axes[1], label='Mass [$M_{\odot}$/kpc$^2$]')
     hist_yz = axes[2].hist2d(Pos[:,1], Pos[:,2], bins = bins, range= ranges,__
      →weights=Mass, density=False, norm ='log')
     axes[2].set title('(y,z) log scale')
     axes[2].set_xlabel('y [kpc]')
     axes[2].set_ylabel('z [kpc]')
     fig.colorbar(hist_yz[3], ax=axes[2], label='Mass [M_{\cot}\, \dot\\, \pc\^2\)')
     plt.show()
```



1.1.3 Task 2 Mark the locations of these galaxies in the projections from Task 1. Use circles or "x" symbols as markers.

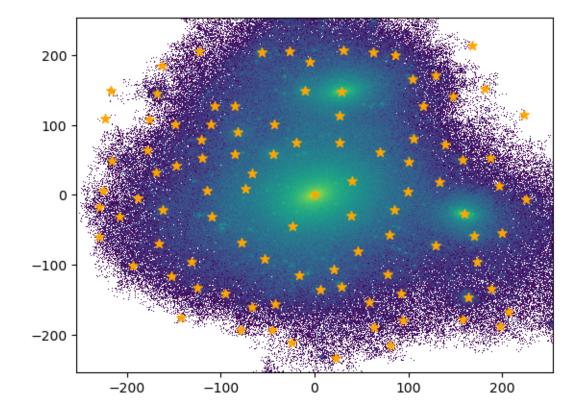
```
[]:  # Trial 1
     # Getting the locations of local maxima of the histogram by comparing with the
      →4 neighbors
     # Too many miniscule maxima are found!
     def local_max0(hist):
         maxima = np.zeros((0,2))
         for i in range(1, hist[0].shape[0]-1):
             for j in range(1, hist[0].shape[1]-1):
                 if hist[0][i,j] >= np.max([hist[0][i-1,j], hist[0][i+1,j],
      →hist[0][i,j-1], hist[0][i,j+1]]):
                     x_center = 0.5 * (hist[1][i] + hist[1][i+1])
                     y_center = 0.5 * (hist[2][j] + hist[2][j+1])
                     maxima = np.vstack([maxima, [x_center, y_center]])
         return maxima
     # first 20 maxima
     #print(local_max0(hist_xy)[0:20])
[]: # the location of the maxima using scatter plot
     \#plt.scatter(local\_max0(hist\_xy)[:,0], local\_max0(hist\_xy)[:,1], 
      ⇔color='skyblue', s=1)
[]: #Trial 2
     # The min_distance parameter is adjustable
     # Avoid finding too many miniscule maxima
     from skimage.feature import peak_local_max
     def local_max1(hist, min_distance=20):
```

```
# Find peaks
    coordinates = peak_local_max(hist[0], min_distance=min_distance)
    # Calculate the center of each peak bin
    maxima = np.zeros((len(coordinates), 2))
    for i, (r, c) in enumerate(coordinates):
        x_center = 0.5 * (hist[1][r] + hist[1][r+1])
        y_center = 0.5 * (hist[2][c] + hist[2][c+1])
        maxima[i] = [x_center, y_center]
    return maxima
#print(local_max1(hist_xy))
print(local_max1(hist_xy).shape)
plt.hist2d(Pos[:,0], Pos[:,1], bins = bins, range= ranges, weights=Mass,

density=False, norm ='log')

plt.scatter(local_max1(hist_xy)[:,0], local_max1(hist_xy)[:,1], color='orange',_
 →marker ='*', s=50)
(100, 2)
```

[]: <matplotlib.collections.PathCollection at 0x117d5f4d0>

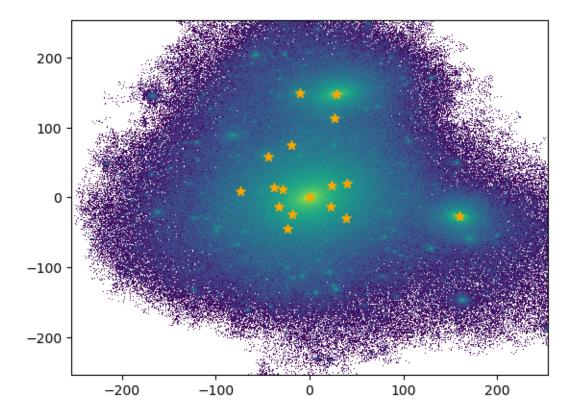


```
[]: # Trial 3
     # The threshold parameter is adjustable to avoid edge pixels
     from skimage.feature import peak_local_max
     min distance = 5
     threshold = 8E+7
     def local_max2(hist, min_distance= min_distance, threshold=threshold):
         # Find peaks
         coordinates = peak_local_max(hist[0], min_distance=min_distance)
         # Calculate the center of each peak bin
         maxima = np.zeros((len(coordinates), 2))
         for i, (r, c) in enumerate(coordinates):
             if hist[0][r, c] > threshold: # threshold here
                 x_{center} = 0.5 * (hist[1][r] + hist[1][r+1])
                 y_center = 0.5 * (hist[2][c] + hist[2][c+1])
                 maxima[i] = [x_center, y_center]
         # Remove zero rows
         maxima = maxima[~np.all(maxima == 0, axis=1)]
         return maxima
     print(local_max2(hist_xy))
     print(local_max2(hist_xy).shape)
     plt.hist2d(Pos[:,0], Pos[:,1], bins = bins, range= ranges, weights=Mass,

density=False, norm ='log')
     plt.scatter(local_max2(hist_xy)[:,0], local_max2(hist_xy)[:,1], color='orange',_
      →marker ='*', s=50)
    [[ 0.5
              0.5]
     [ 28.5 147.5]
     [159.5 - 27.5]
     [ 39.5 20.5]
     [-10.5 148.5]
     [-19.5 75.5]
     [-44.5 58.5]
     [-73.5 8.5]
     [ 23.5 16.5]
     [ 26.5 113.5]
     [-18.5 - 23.5]
     [-37.5 14.5]
```

```
[ 38.5 -29.5]
[ 22.5 -12.5]
[-23.5 -44.5]
[-28.5 11.5]
[-32.5 -12.5]]
(17, 2)
```

[]: <matplotlib.collections.PathCollection at 0x13fb1b4d0>



```
[]: ### Trial 4: Final Answer ###
# 6 subplots 2*3 for comparision * each projection

fig, axes = plt.subplots(3, 2, figsize=(10, 15))

axes[0,0].hist2d(Pos[:,0], Pos[:,1], bins = bins, range= ranges, weights=Mass,u odensity=False, norm ='log')
axes[0,1].hist2d(Pos[:,0], Pos[:,1], bins = bins, range= ranges, weights=Mass,u odensity=False, norm ='log')
axes[0,1].scatter(local_max2(hist_xy)[:,0], local_max2(hist_xy)[:,1],u ocolor='orange', marker ='x', s=50)
axes[0,0].set_title('(x,y)')
axes[0,1].set_title('(x,y) maxima')
```

```
axes[1,0].hist2d(Pos[:,0], Pos[:,2], bins = bins, range= ranges, weights=Mass,

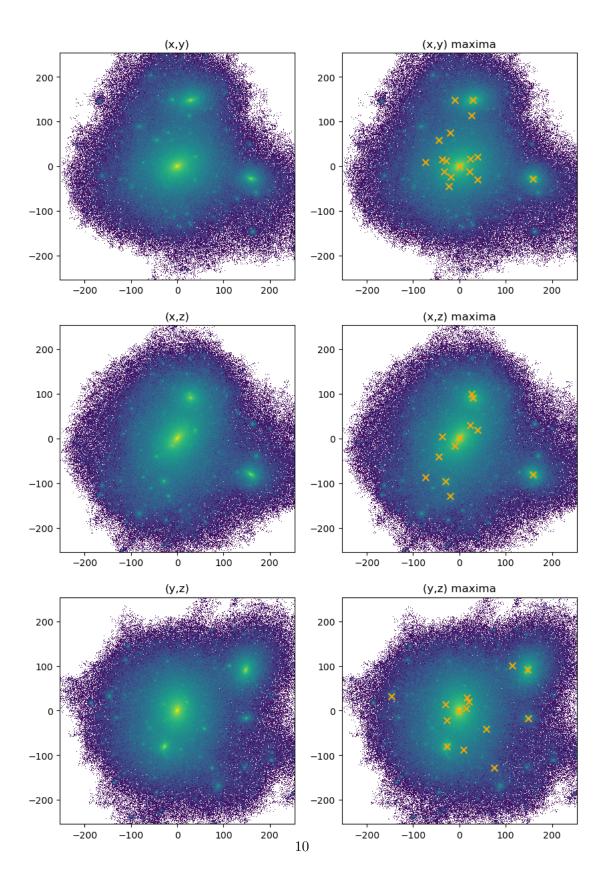
density=False, norm ='log')
axes[1,1].hist2d(Pos[:,0], Pos[:,2], bins = bins, range= ranges, weights=Mass,

density=False, norm ='log')

axes[1,1].scatter(local_max2(hist_xz)[:,0], local_max2(hist_xz)[:,1],__
⇔color='orange', marker ='x', s=50)
axes[1,0].set title('(x,z)')
axes[1,1].set_title('(x,z) maxima')
axes[2,0].hist2d(Pos[:,1], Pos[:,2], bins = bins, range= ranges, weights=Mass,

density=False, norm ='log')
axes[2,1].hist2d(Pos[:,1], Pos[:,2], bins = bins, range= ranges, weights=Mass,

density=False, norm ='log')
axes[2,1].scatter(local_max2(hist_yz)[:,0], local_max2(hist_yz)[:,1],__
⇔color='orange', marker ='x', s=50)
axes[2,0].set_title('(y,z)')
axes[2,1].set_title('(y,z) maxima')
plt.suptitle('Neighbor Size = %s & Threshold = %.0e' % (min_distance, __
 →threshold))
plt.show()
```



```
[]: print("xy:\n", local_max2(hist_xy).shape,"\n", local_max2(hist_xy))
    xy:
     (17, 2)
     [[ 0.5
              0.5]
     [ 28.5 147.5]
     [159.5 - 27.5]
     [ 39.5 20.5]
     [-10.5 148.5]
     [-19.5 75.5]
     [-44.5 58.5]
     [-73.5]
             8.5]
     [ 23.5 16.5]
     [ 26.5 113.5]
     [-18.5 -23.5]
     [-37.5 14.5]
     [38.5 - 29.5]
     [22.5 - 12.5]
     [-23.5 -44.5]
     [-28.5 11.5]
     [-32.5 -12.5]]
[]: print("xz:\n", local_max2(hist_xz).shape,"\n", local_max2(hist_xz))
    xz:
     (12, 2)
     [[
         0.5
                 0.5]
     [ 159.5 -80.5]
     [ 29.5
              91.5]
     [-10.5 -17.5]
     [ 26.5
              100.5]
     [-29.5 -95.5]
     [ 39.5
              19.5]
     [-44.5 - 40.5]
     [-37.5]
                4.5]
     [-19.5 - 129.5]
     [ -73.5 -86.5]
     [ 23.5
               29.5]]
[]: print("yz:\n", local_max2(hist_yz).shape,"\n", local_max2(hist_yz))
    yz:
     (14, 2)
     [[-0.5]
                -0.5]
     [ 147.5
               91.5]
     [-27.5 -80.5]
```

```
[ 20.5
          19.5]
[148.5 -17.5]
  58.5
        -40.5]
[ 14.5
           4.5]
[-29.5]
          14.5]
    8.5
        -87.5]
  75.5 -128.5]
[-26.5]
        -22.5]
[ 113.5
        100.5]
Γ 16.5
          29.5]
[-146.5]
          32.5]]
```

```
[]: # print the (x,y,z) coordinates of the center of the galaxy from
      \neglocal_max2(hist_xy) and local_max2(hist_xz) and local_max2(hist_yz)
     # if there are (a,b), (b,c), (c,a) coordinates, then the center of the galaxy.
      \hookrightarrow is (a,b,c)
     # save the coordinates of the center of the galaxy in a variable named centersu
      ⇔and print it
     # centers = []
     # for i in range(local_max2(hist_xy).shape[0]):
           for j in range(local max2(hist xz).shape[0]):
                for k in range(local_max2(hist_yz).shape[0]):
                    if (local max2(hist xy)[i][0] == local max2(hist xz)[i][0]) and
      \hookrightarrow (local_max2(hist_xy)[i][1] == local_max2(hist_yz)[k][0]) and
      \rightarrow (local_max2(hist_xz)[j][1] == local_max2(hist_yz)[k][1]):
                         centers.append([local_max2(hist_xy)[i][0], __
      \hookrightarrow local_max2(hist_xy)[i][1], local_max2(hist_xz)[j][1]])
     # print("The center of the galaxy is: \n", centers)
```

The result of the code above (it takes 7 minutes to run it): The center of the galaxy is: [[159.5, -27.5, -80.5], [39.5, 20.5, 19.5], [-10.5, 148.5, -17.5], [-44.5, 58.5, -40.5], [23.5, 16.5, 29.5], [26.5, 113.5, 100.5], [-37.5, 14.5, 4.5]]

```
[]: # append missed points to the centers manually centers = [[159.5, -27.5, -80.5], [39.5, 20.5, 19.5], [-10.5, 148.5, -17.5], [-44.5, 58.5, -40.5], [23.5, 16.5, 29.5], [26.5, 113.5, 100.5], [-37.5, 14. -5, 4.5]]

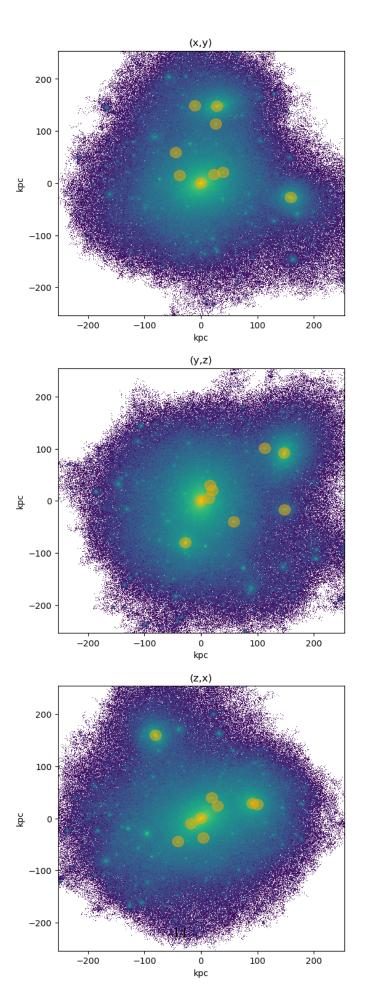
centers.insert(0,[0,0,0])
centers.append([28.5, 147.5, 91.5])
```

```
[]: # 10 kpc radius circle around the center of the galaxy # 2.5 kpc radius circle is not visible in the plot, so enlarged to 10 kpc
```

```
fig, axes = plt.subplots(3,1, figsize=(6, 19))

for i in range(3):
    axes[i].hist2d(Pos[:,i], Pos[:,(i+1)%3], bins = bins, range= ranges,
    weights=Mass, density=False, norm ='log')
    for j in range(len(centers)):
        circle = plt.Circle((centers[j][i], centers[j][(i+1)%3]), 10,
    color='orange', fill=True, alpha=0.5)
        axes[i].add_patch(circle)
    axes[i].set_xlabel('kpc')
    axes[i].set_ylabel('kpc')

axes[0].set_title('(x,y)')
    axes[1].set_title('(x,y)')
    plt.show()
```



1.1.4 Task 3 Calculate the DM mass in each of the spherical shells.

Calculate the mass in each shell by looping over all bins, and then sum the mass from the DM particles residing in each shell.

A fast method is to use the numpy.digitize function to calculate the bin of each DM particle, and numpy.bin_count to calculate the number of particles in each bin.

Note, that these functions use a convention, where the first bin is an underflow bin: it counts the number of particles at a radius smaller than R[0]. The last bin is an overflow bin with particles with radius larger than R[-1]. So these bins have to be removed from the out- put of numpy.bin_count to make it compatible with our bin definition (as used by e.g. MidpointShell).

2 Feedback #1

On page 15, there is a little mistake / bug in the way the bins are set up. You should replace the following

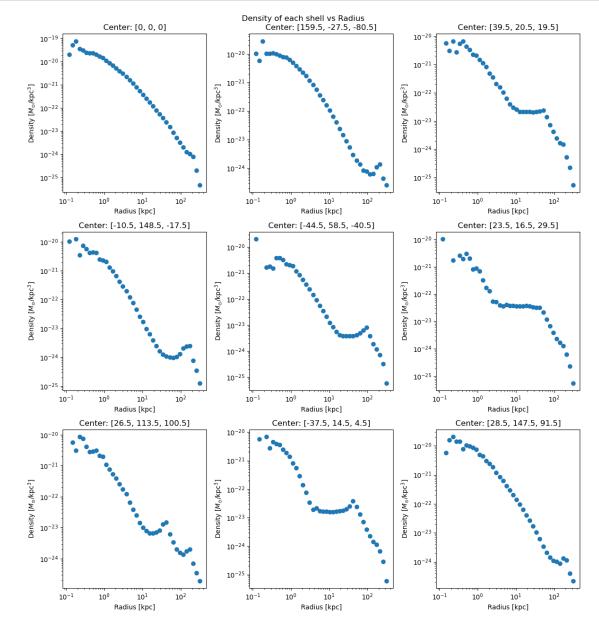
```
\begin{split} \log R &= \text{np.linspace(-1.0, np.log10(2.5), 41)} \\ \text{with} \\ \log R &= \text{np.linspace(-1.0, 2.5, 41)} \end{split}
```

... otherwise the bins do not reach high enough radii.

```
[]: MassInShell = np.zeros((len(centers), len(VolumeOfShell))) #in solar masses
     for i in range(len(centers)):
         indices = np.digitize(np.sqrt((Pos[:,0]-centers[i][0])**2 + (Pos[:
      4,1]-centers[i][1])**2 + (Pos[:,2]-centers[i][2])**2), R.value)
         MassInShell[i] = np.bincount(indices, weights=Mass,__
      →minlength=len(VolumeOfShell))[1:-1]
     print(MassInShell.shape)
     print(MassInShell[0])
    (9, 40)
    [1.07692828e+06 4.84617728e+06 1.34616036e+07 1.13077470e+07
     1.83077808e+07 2.58462788e+07 4.46925238e+07 8.45388703e+07
     1.33000643e+08 2.05693302e+08 3.21463093e+08 4.38848276e+08
     6.50464684e+08 9.35312215e+08 1.28908316e+09 1.79631638e+09
     2.54478154e+09 3.42624734e+09 4.47356009e+09 5.76156632e+09
     7.21380411e+09 9.07258233e+09 1.18693651e+10 1.48971490e+10
     1.84580123e+10 2.26036478e+10 2.80351356e+10 3.49242458e+10
     4.33959021e+10 5.22714066e+10 5.94566721e+10 6.29189965e+10
     6.88275636e+10 7.97363086e+10 8.97495878e+10 1.00882872e+11
     1.55596752e+11 2.15983890e+11 1.02546727e+11 4.23582817e+10
    2.0.1 Task 4 Calculate as a function of R, and plot log as a function of log R.
[]: rho_shell = np.zeros((len(centers), len(R)-1)) # SI units
     for i in range(len(centers)):
         rho_shell[i] = (MassInShell[i] / VolumeOfShell) * 6.772E-29
     print(rho_shell.shape)
     print(rho_shell[0][2])
    (9, 40)
    7.825988637549038e-20
[]: | # plot the density of each shell as a function of the radius
     # 9 subolots for 9 centers
     fig, axes = plt.subplots(3, 3, figsize=(12, 13))
     for i in range(3):
         for j in range(3):
             axes[i,j].plot(R[1:], rho_shell[i*3+j], 'o')
             axes[i,j].set_xscale('log')
             axes[i,j].set_yscale('log')
```

```
axes[i,j].set_xlabel('Radius [kpc]')
axes[i,j].set_ylabel('Density [$M_{\odot}$/kpc$^3$]')
axes[i,j].set_title('Center: %s' % centers[i*3+j])

plt.suptitle('Density of each shell vs Radius')
plt.tight_layout()
plt.show()
```



2.0.2 Task 5 Find the critical density, Ω crit,0, at redshift 0 in a Planck15 cosmology, for example by using the astropy package.

$$\rho_{crit,0} = \frac{3H^2}{8\pi G}$$

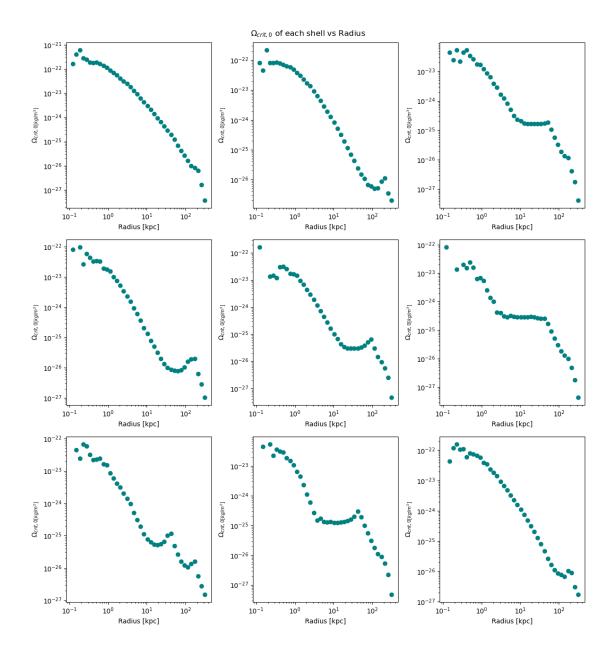
$$\Omega_{crit,0} = \frac{\rho}{\rho_{crit,0}}$$

```
[]: from astropy.cosmology import Planck15
  import astropy.units as u

rho_crit0 = Planck15.critical_density0.si
  print(rho_crit0)
```

8.619160453017514e-27 kg / m3

```
[]: # These are all about shell densities
     omega_crit0 = np.zeros((len(centers), len(R)-1))
     rho_shell_si = np.zeros((len(centers), len(R)-1))
     for i in range(len(centers)):
         rho_shell_si[i] = rho_shell[i] * 6.772E-29 # convert to kg/m^3
         omega_crit0[i] = rho_shell_si[i] / rho_crit0.value
     # 9 subplots for 9 centers
     fig, axes = plt.subplots(3, 3, figsize=(12, 13))
     for i in range(3):
         for j in range(3):
             axes[i,j].plot(R[1:], omega_crit0[i*3+j], 'o', color = 'teal')
             axes[i,j].set_xscale('log')
             axes[i,j].set yscale('log')
             axes[i,j].set_xlabel('Radius [kpc]')
             axes[i,j].set_ylabel('$\Omega_{crit,0 [kg/m^3]}$')
     plt.suptitle('$\Omega_{crit,0}$ of each shell vs Radius')
     plt.tight_layout()
     plt.show()
```



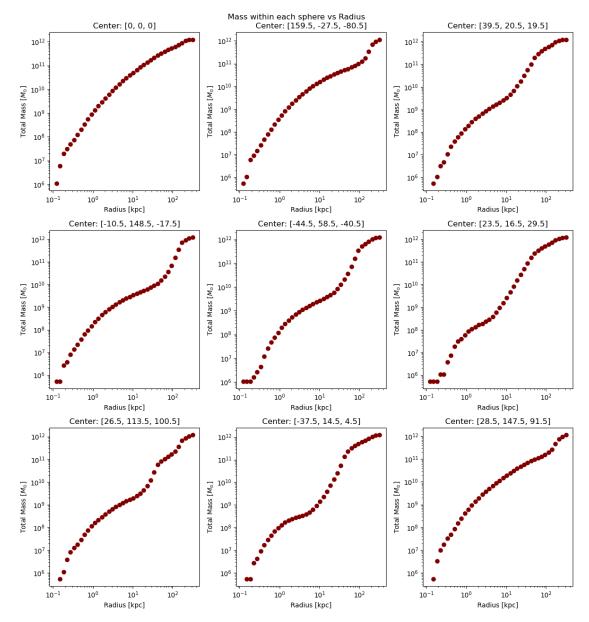
2.0.3 Task 6 Calculate the total mass (Mtot) inside a given radius (R) for the above dark matter halo.

```
[]: Mtot = np.zeros((len(centers),len(R)-1))
for i in range(len(centers)):
    Mtot[i] = np.cumsum(MassInShell[i]) # in solar masses

# 9 subplots for 9 centers
fig, axes = plt.subplots(3, 3, figsize=(12, 13))
```

```
for i in range(3):
    for j in range(3):
        axes[i,j].plot(R[1:], Mtot[i*3+j], 'o', color = 'maroon')
        axes[i,j].set_xscale('log')
        axes[i,j].set_yscale('log')
        axes[i,j].set_xlabel('Radius [kpc]')
        axes[i,j].set_ylabel('Total Mass [$M_{\odot}]')
        axes[i,j].set_title('Center: %s' % centers[i*3+j])

plt.suptitle('Mass within each sphere vs Radius')
plt.tight_layout()
plt.show()
```



2.0.4 Task 7 Solve the equation $200\Omega \text{crit}, 0 = \text{Mtot}/(34 \text{ R3})$ for the above halo (numerically solve for R). Determine M200 and R200.

An estimate of radius and mass of a cosmological halo (M200 and R200) A commonly used measure of a halo's radius is R200, which is the radius inside which the mean density is 200 times the critical density of the universe. M200 is the total mass inside R200.

3 Feedback #3

```
On page 21, I guess you should replace /200*omega_crit0[i][j] with /(200*omega_crit0[i][j])
When you have updated #1
```

```
[]: # first, plot to see the scale of the differences
     difference = np.zeros((len(centers), len(R)-1))
     for i in range(len(centers)):
         for j in range(len(R)-1):
             difference[i][j] = (200*omega_crit0[i][j] - Mtot[i][j]*6.772E-29/(4.0/3.
      →0*np.pi*R[j].value**3))/(200*omega_crit0[i][j])
             ### updated the error in calculation
         plt.scatter(R[1:],difference[i],label=i)
     plt.legend()
     plt.xscale('log')
     plt.yscale('log')
     plt.xlim(0, 300)
     plt.ylim(0, 1)
     plt.xlabel('Radius [kpc]')
     plt.ylabel('Relative Difference')
     plt.title('Difference vs Radius')
     plt.show()
```

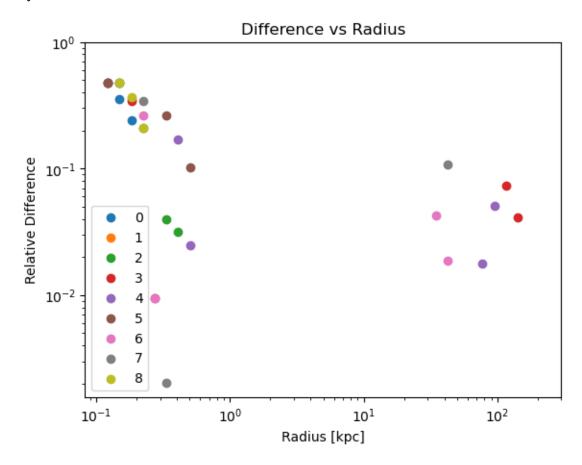
```
/var/folders/6m/zf_f5yss4dxc7yj9tl4kmfnc0000gn/T/ipykernel_26432/1334369147.py:6
: RuntimeWarning: invalid value encountered in scalar divide
    difference[i][j] = (200*omega_crit0[i][j] -
Mtot[i][j]*6.772E-29/(4.0/3.0*np.pi*R[j].value**3))/(200*omega_crit0[i][j])
/var/folders/6m/zf_f5yss4dxc7yj9tl4kmfnc0000gn/T/ipykernel_26432/1334369147.py:6
: RuntimeWarning: divide by zero encountered in scalar divide
    difference[i][j] = (200*omega_crit0[i][j] -
Mtot[i][j]*6.772E-29/(4.0/3.0*np.pi*R[j].value**3))/(200*omega_crit0[i][j])
/var/folders/6m/zf_f5yss4dxc7yj9tl4kmfnc0000gn/T/ipykernel_26432/1334369147.py:1
```

4: UserWarning: Attempt to set non-positive xlim on a log-scaled axis will be ignored.

plt.xlim(0, 300)

/var/folders/6m/zf_f5yss4dxc7yj9tl4kmfnc0000gn/T/ipykernel_26432/1334369147.py:1 5: UserWarning: Attempt to set non-positive ylim on a log-scaled axis will be ignored.

plt.ylim(0, 1)



Now I feel like the question is using Omega (density parameter, supposedly) when it should be using rho, the density. The equation given in the question does not make sense since Omega is dimensionless.

$$200\Omega_{crit,0} = \frac{M_{tot}}{\frac{4}{3}\pi R^3}???$$

$$\rightarrow 200\rho_{crit,0} = \frac{M_{tot}}{\frac{4}{3}\pi R^3}$$

I will use rho_crit0 instead of omega. The goal is to find M that satisfies the equation below.

$$M = 200\rho_{crit,0} \frac{4}{3}\pi R^3$$

```
[]: from scipy.optimize import fsolve
     from scipy.interpolate import interp1d
     R200_m = np.zeros(len(centers))
     M200_kg = np.zeros(len(centers))
     # convet to SI units
     R_m = R.to(u.m)
     Mtot_kg = Mtot * const.M_sun.si
     # interpolate and solve for R200
     for i in range(len(centers)):
         f = interp1d(R_m[1:] , Mtot_kg[i], kind='cubic',fill_value='extrapolate')
         R200_m[i] = (fsolve(lambda x: f(x) - 200*rho_crit0.value*4.0*np.pi*x**3/
      \hookrightarrow 3, R_m[-1])
         M200_kg[i] = f(R200_m[i])
     print('R200 in m:\n',R200_m)
     print('M200 in kg:\n',M200_kg)
    R200 in m:
     [6.77671102e+21 3.05599066e+21 6.72249288e+21 6.23674246e+21
     6.57315305e+21 6.72493426e+21 5.98567162e+21 6.64046361e+21
     3.98273088e+21]
    M200 in kg:
     [2.24719350e+42 2.06081800e+41 2.19368681e+42 1.75168900e+42
     2.05071262e+42 2.19607769e+42 1.54853930e+42 2.11435922e+42
     4.56169721e+41]
    3.0.1 Task 8 Add a circle indicating R200 to the figure from Task 2.
[]: # unit conversion
     R200_kpc = R200_m / 3.086E+19
     M200_Msun = (M200_kg / const.M_sun.si.value)
     print('R200 in kpc:\n',R200_kpc)
     print('M200 in Msun:\n',M200_Msun)
    R200 in kpc:
     [219.59530201 99.02756521 217.83839534 202.09794114 212.99912667
     217.91750678 193.96213923 215.18028538 129.05803246]
    M200 in Msun:
     [1.13014602e+12 1.03641509e+11 1.10323673e+12 8.80949661e+11
     1.03133295e+12 1.10443914e+12 7.78782746e+11 1.06334174e+12
```

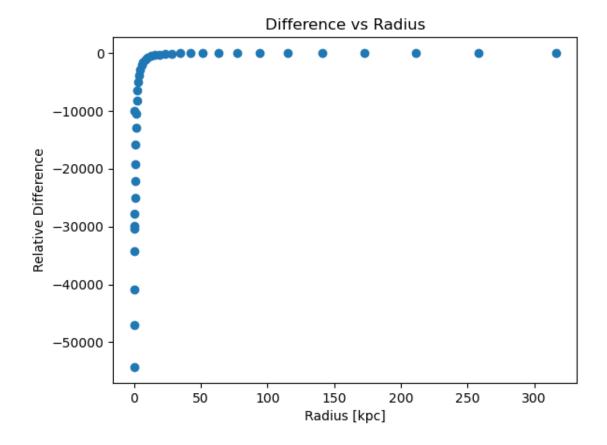
2.29414332e+11]

4 Feedback #2

Just calculate the M200 and R200 for the main cluster - it is not necessary for the subhalos.

4.0.1 Doing the above again (Feedback#2)

```
[]: # first, plot to see the scale of the differences
     difference_main = np.zeros(len(R)-1)
     for j in range(len(R)-1):
         difference_main[j] = (200*rho_crit0.value - Mtot[0][j]*6.772E-29/(4.0/3.
      →0*np.pi*R[j].value**3))/(200*rho_crit0.value)
         ### updated the error in calculation
     print(difference_main)
     print(R[1:])
     plt.scatter(R[1:],difference_main)
     plt.xlabel('Radius [kpc]')
     plt.ylabel('Relative Difference')
     plt.title('Difference vs Radius')
     plt.show()
    [-1.00989718e+04 -3.03506882e+04 -5.42731046e+04 -4.69521812e+04
     -4.09563226e+04 -3.41815901e+04 -2.98283054e+04 -2.78236286e+04
     -2.51100284e+04 -2.20917968e+04 -1.92195231e+04 -1.58335430e+04
     -1.29695217e+04 -1.04789665e+04 -8.28025043e+03 -6.46919654e+03
     -5.04008589e+03 -3.86115788e+03 -2.89952142e+03 -2.13993285e+03
     -1.54922703e+03 -1.10745854e+03 -7.91525995e+02 -5.60180834e+02
     -3.92381414e+02 -2.71989608e+02 -1.87498003e+02 -1.28769681e+02
     -8.80839150e+01 -5.96388359e+01 -3.95681518e+01 -2.54653649e+01
     -1.60300984e+01 -9.93164945e+00 -5.97328816e+00 -3.42451031e+00
     -1.93525937e+00 -9.96480670e-01 -1.92722267e-01 3.25320862e-01]
    [1.22320712e-01 1.49623566e-01 1.83020611e-01 2.23872114e-01
     2.73841963e-01 3.34965439e-01 4.09732110e-01 5.01187234e-01
     6.13055792e-01 7.49894209e-01 9.17275935e-01 1.12201845e+00
     1.37246096e+00 1.67880402e+00 2.05352503e+00 2.51188643e+00
     3.07255737e+00 3.75837404e+00 4.59726989e+00 5.62341325e+00
     6.87859912e+00 8.41395142e+00 1.02920053e+01 1.25892541e+01
     1.53992653e+01 1.88364909e+01 2.30409298e+01 2.81838293e+01
     3.44746607e+01 4.21696503e+01 5.15822165e+01 6.30957344e+01
     7.71791516e+01 9.44060876e+01 1.15478198e+02 1.41253754e+02
     1.72782598e+02 2.11348904e+02 2.58523484e+02 3.16227766e+02] kpc
```



```
[]: ### M200 and R200 for the main cluster
     M200_main = M200_Msun[0]
     R200_{main} = R200_{kpc}[0]
     print('M200 for the main cluster: ', "{:e}".format(M200_main), 'Msun')
     print('R200 for the main cluster: ', "{:e}".format(R200_main), 'kpc')
     fig, axes = plt.subplots(1,3, figsize=(13, 4))
     for i in range(3):
         axes[i].hist2d(Pos[:,i], Pos[:,(i+1)\%3], bins = bins, range= ranges,_{\sqcup}
      ⇔weights=Mass, density=False, norm ='log')
         circle = plt.Circle((centers[0][i], centers[0][(i+1)%3]), R200_main,__
      ⇔color='red', fill=False, linewidth=5, alpha=0.6)
         axes[i].add_patch(circle)
         axes[i].set_xlabel('kpc')
         axes[i].set_ylabel('kpc')
     axes[0].set_title('(x,y)')
     axes[1].set_title('(y,z)')
```

```
axes[2].set_title('(z,x)')
plt.suptitle('Main Cluster with R200')
plt.show()
```

M200 for the main cluster: 1.130146e+12 Msun R200 for the main cluster: 2.195953e+02 kpc

